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DEPARTMENT OF SCHOOL EDUCATION AND LITERACY

DISTRICT INSTITUTE OF EDUCATION AND TRAINING
CHITRADURGA

LESSON BASED ASSESSMENT MATERIAL

2025-26

MATHEMATICS

10

TENTH STANDARD

ENGLISH MEDIUM

DEPARTMENT OF STATE EDUCATIONAL RESEARCH AND TRAINING

BANASHANKARI 3rd STAGE, BENAGALURU-560085

ಪರಿಕಲ್ಪನೆ ಮತ್ತು ಮಾರ್ಗದರ್ಶನ	
<p>ಶ್ರೀಮತಿ ರಶ್ಮಿ ಮಹೇಶ್ ಭಾ.ಆ.ಸೇ ಸರ್ಕಾರದ ಪ್ರಧಾನ ಕಾರ್ಯದರ್ಶಿಗಳು, ಶಾಲಾ ಶಿಕ್ಷಣ ಮತ್ತು ಸಾಕ್ಷರತಾ ಇಲಾಖೆ</p>	
<p>ಡಾ. ತ್ರಿಲೋಕ್ ಚಂದ್ರ KV., ಭಾ.ಆ.ಸೇ ಆಯುಕ್ತರು, ಶಾಲಾ ಶಿಕ್ಷಣ ಇಲಾಖೆ, ಬೆಂಗಳೂರು</p>	<p>ಶ್ರೀ ಗೋಪಾಲಕೃಷ್ಣ H N, ನಿರ್ದೇಶಕರು, DSERT, ಬೆಂಗಳೂರು</p>
ಡಯಟ್ ಸಹಕಾರ	
<p>ಪ್ರಾಂಶುಪಾಲರು ಶ್ರೀ ಎಂ.ನಾಸೀರುದ್ದೀನ್ ಪ್ರಾಂಶುಪಾಲರು ಹಾಗೂ ಪದನಿಮಿತ್ತ ಉಪನಿರ್ದೇಶಕರು (ಡಯಟ್) ಚಿತ್ರದುರ್ಗ</p>	<p>ಮೆಂಟರ್ ಶ್ರೀ ಬಿ.ಎಸ್.ನಿತ್ಯಾನಂದ್ ಉಪನ್ಯಾಸಕರು, ಡಯಟ್, ಚಿತ್ರದುರ್ಗ</p>
ಸಂಯೋಜನೆ	
<p>ಶ್ರೀಮತಿ ರಾಧಾ P, ಹಿರಿಯ ಸಹಾಯಕ ನಿರ್ದೇಶಕರು, DSERT, ಬೆಂಗಳೂರು</p>	
ಗಣಿತ ಪಾಠ ಆಧಾರಿತ ಮೌಲ್ಯಾಂಕನ ಸಾಮಗ್ರಿ ರಚನಾ ಸಂಪನ್ಮೂಲ ತಂಡ	
<ol style="list-style-type: none"> 1. ಶ್ರೀ ರಂಗನಾಥ್ ಜಿ. ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ ರೇಖಲಗರೆ ಲಂಬಾಣಿಹಟ್ಟಿ, ಚಳ್ಳಕೆರೆ ತಾ. 2. ಶ್ರೀಮತಿ ಅರುಣ ಬಿ ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ ಚವಳಿಹಳ್ಳಿ ಗೊಲ್ಲರಹಟ್ಟಿ, ಚಿತ್ರದುರ್ಗ ತಾ. 3. ಶ್ರೀ ಪ್ರಕಾಶ್ ಎಲ್ ಸ.ಶಿ ಸ.ಪ.ಪೂ.ಕಾಲೇಜು (ಪ್ರೌ.ಶಾ.ವಿಭಾಗ) ವಿ.ವಿ.ಪುರ ಹಿರಿಯೂರು ತಾ. 4. ಶ್ರೀ ವಾದಿರಾಜ್ ಪಿ.ವಿ ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ ಕೋಟೆ, ಚಿತ್ರದುರ್ಗ 5. ಶ್ರೀ ಮಂಜುನಾಥ್ ಜಿ ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ, ಆಲೂರು, ಹಿರಿಯೂರು ತಾ. 6. ಶ್ರೀಮತಿ ಸಲ್ಮಾತಬಸುನ್ ಸ.ಶಿ ಕೆ.ಪಿ.ಎಸ್ ಅನ್ನೇಹಾಳ್ ಜಂಪಯ್ಯನಹಟ್ಟಿ, ಚಿತ್ರದುರ್ಗ ತಾ. 7. ಶ್ರೀ ವೀರಭದ್ರಪ್ಪ ಜಿ.ಎಂ ಸ.ಶಿ ಆದರ್ಶ ವಿದ್ಯಾಲಯ ಚಳ್ಳಕೆರೆ 8. ಶ್ರೀ ರಮೇಶ್ ಎಂ.ಎಸ್ ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ ನಾಗತಿಹಳ್ಳಿ ಹೊಸದುರ್ಗ ತಾ. 9. ಶ್ರೀ ತಿಮ್ಮೇಶ್ ವಿ ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ ವಸಂತ ನಗರ, ಹಿರಿಯೂರು ತಾ. 10. ಶ್ರೀ ಝಹೀರ್ ಅಹ್ಮದ್ ಸ.ಶಿ ಸ.ಪ.ಪೂ.ಕಾಲೇಜು (ಪ್ರೌ.ಶಾ.ವಿಭಾಗ) ಚಿತ್ರದುರ್ಗ 11. ಶ್ರೀಮತಿ ತಾರಾಕುಮಾರಿ ಕೆ ಸ.ಶಿ ಸ.ಪ್ರೌ.ಶಾಲೆ ಸಿದ್ದೇಶ್ವರನದುರ್ಗ ಚಳ್ಳಕೆರೆ ತಾ. 12. ಶ್ರೀ ಬಸವಂತಕುಮಾರ್ ಎಂ.ಟಿ ಸ.ಶಿ ಡಾನ್ ಬಾಸ್ಕೋ ಪ್ರೌ.ಶಾಲೆ ಚಿತ್ರದುರ್ಗ 13. ಶ್ರೀ ಲೋಕೇಶ್ ಸ.ಶಿ ವಿಶ್ವಮಾನವ ಪ್ರೌ.ಶಾಲೆ ಸೀಬಾರ, ಚಿತ್ರದುರ್ಗ ತಾ. 14. ಶ್ರೀಮತಿ ರಶ್ಮಿ ಹೆಚ್.ಕೆ ಸ.ಶಿ ಚಿಂತಾಮಣೇಶ್ವರ ಪ್ರೌ.ಶಾಲೆ, ಹಿರೇಹಳ್ಳಿ, ಚಳ್ಳಕೆರೆ ತಾ. 	
ಮಾರ್ಗದರ್ಶಕರು ಹಾಗೂ ಪರಿಶೀಲಕರು	
<p>ಶ್ರೀಮತಿ ಶಾರದ ಹೆಚ್.ಎಸ್ ಸಹ ಶಿಕ್ಷಕರು ಸರ್ಕಾರಿ ಪ್ರೌಢಶಾಲೆ, ಎಂ.ಸಿ ತಳಲು, ಹೆಗ್ಗಡದೇವನಕೋಟೆ ತಾ ಮೈಸೂರು</p>	<p>ಶ್ರೀ ಅನಿಲ್ ಕುಮಾರ್ ಸಿ.ಎನ್ ಸಹ ಶಿಕ್ಷಕರು ಸರ್ಕಾರಿ ಪ್ರೌಢಶಾಲೆ, ಅರಳಾಳುಸಂದ್ರ, ರಾಮನಗರ ತಾ ಬೆಂಗಳೂರು ದಕ್ಷಿಣ</p>

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UNIT1: REAL NUMBERS

Learning Points

- ❖ Prime numbers, Composite numbers and Fundamental theorem of arithmetic
- ❖ H.C.F and L.C.M of numbers
- ❖ The relationship between two numbers and their H.C.F and L.C.M
- ❖ Proof for irrational numbers

Number of questions	Easy	Average	Difficult
63	28	30	5

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

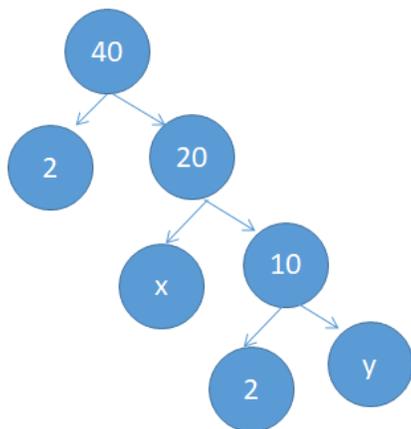
- $\sqrt{2}$ is a/an (Easy)
(A) Rational number (B) Irrational number
(C) Integer (D) Natural number
- $5 - \sqrt{3}$ is a/an (Easy)
(A) Irrational number (B) Rational number
(C) Composite number (D) Prime number
- Rational number in the following is, (Easy)
(A) 5 (B) π (C) $\sqrt{3}$ (D) $3\sqrt{3}$
- Which of the following is not an irrational number? (Easy)
(A) $\sqrt{2}$ (B) $\sqrt{3}$ (C) $\sqrt{9}$ (D) $\sqrt{5}$
- Rational number in the following is, (MQP-2025:Easy)
(A) $\sqrt{3}$ (B) $\sqrt{4}$ (C) $\sqrt{5}$ (D) $\sqrt{7}$
- π is a/an (Easy)
(A) Irrational number (B) Rational number
(C) Prime number (D) Composite number
- $7 \times 11 \times 13 + 13$ is a/an (Aug - 2024 : Easy)
(A) Prime number (B) composite number
(C) Irrational number (D) odd number
- Prime factorization of 91 is, (SLP-2024 : Easy)
(A) $2 \times 13 \times 7$ (B) 13×7 (C) 91×1 (D) $13 \times 7 \times 1$
- The number of primes between 1 and 10 is, (Easy)
(A) 2 (B) 3 (C) 4 (D) 12

10. Any composite number can be expressed as the product of (Average)
 (A) even numbers (B) odd numbers
 (C) prime numbers (D) square numbers
11. The prime factorization of 120 is, (MQP-2019 : Easy)
 (A) $2^3 \times 3^2 \times 5^1$ (B) $2^2 \times 3^1 \times 5^1$
 (C) $2^3 \times 3^1 \times 5^2$ (D) $2^3 \times 3^1 \times 5^1$
12. The prime factors of 30 is, (Easy)
 (A) 2, 3, 5 (B) 5, 3 (C) 15, 2 (D) 6, 5
13. The L.C.M of 2 and 3 (Easy)
 (A) 2 (B) 3 (C) 5 (D) 6
14. The H.C.F of 3 and 5 is, (SLP-2023 : Easy)
 (A) 1 (B) 3 (C) 5 (D) 15
15. The H.C.F of any two consecutive natural numbers is, (Easy)
 (A) 0 (B) 1 (C) 2 (D) 3
16. The H.C.F of any two prime numbers is, (June-2023 : Easy)
 (A) 0 (B) 2 (C) 1 (D) -1
17. If 'a' and 'b' are co-primes, then their H.C.F is, (Easy)
 (A) 0 (B) a x b (C) 1 (D) a + b
18. The H.C.F of the smallest composite number and the smallest prime number is, (September-2020: Average)
 (A) 4 (B) 2 (C) 1 (D) 8
19. For any two positive integers, 'a' and 'b', H.C.F (a, b) \times L.C.M (a, b) is equal to (April-2019 : Easy)
 (A) (a + b) (B) (a - b) (C) (a \times b) (D) (a \div b)
20. The H.C.F of (12, 15) is 3. The L.C.M of (12, 15) is, (Average)
 (A) 60 (B) 45 (C) 36 (D) 90
21. The H.C.F of $5^2 \times 2$ and $2^5 \times 5$ is, (MQP-1,2024 : Easy)
 (A) 2×5 (B) $2^5 \times 5$ (C) $5^2 \times 2^6$ (D) $2^5 \times 5^2$
22. Two positive integers a and b are expressed as, $a = x^3 y^2$ and $b = x y^3$ If x and y are prime numbers, then the H.C.F of (a, b) is, (Average)
 (A) xy (B) $x y^2$ (C) $x^3 y^3$ (D) $x^2 y^2$
23. The L.C.M of a and 18 is 36 and H.C.F of a and 18 is 2. The value of a is, (Average)
 (A) 2 (B) 3 (C) 4 (D) 1
24. If p and q are co-primes, then the H.C.F of p^2 and q^2 is, (Easy)
 (A) pq (B) 1 (C) p + q (D) $p^2 q^2$
25. If $180 = 2^x \times 3^2 \times 5$ then the value of x is, (SLP-2020 : Difficult)
 (A) 1 (B) 2 (C) 3 (D) 4

26. The product of H.C.F and L.C.M of the numbers 15 and 20 is, (April-2024 : Average)
 (A) 15 (B) 20 (C) 300 (D) 35
27. 'a' is an odd number and 'b' is a number divisible by 3. If the L.C.M of 'a' and 'b' is 'p' then the L.C.M of 3a and 2b is, (Difficult)
 (A) p^2 (B) 5p (C) 6p (D) 3p
28. The H.C.F and L.C.M of two numbers a and b are 5 and 200, then the product of a and b is, (Average)
 (A) 205 (B) 1000 (C) 200 (D) 195

II. Answer the following questions. (1 Mark)

29. Express 140 as the product of prime numbers. (Easy)
30. State the fundamental theorem of arithmetic. (MQP 2024:Easy)
31. If the H.C.F of the numbers 24 and 36 is 12, then find their L.C.M (Easy)
32. Express 96 as its product of prime factors. (June-2019 : Easy)
33. Express 156 as its product of prime factors. (Easy)
34. If $200 = 2^m \times 5^n$, then find the value of m and n. (April-2024 : Difficult)
35. Find the maximum length of the rod which can measure the rods of length 24m and 36m exactly. (Average)
36. Write the number which has only 7 and 3 as its prime factors. (Average)
37. Observe the given factor tree and find the value of x and y. (Easy)



III. Answer the following questions. (2 Marks)

38. If the H.C.F. of (306, 657) is 9 then find the L.C.M of (306, 657). (Easy)
39. $7 \times 11 \times 13 + 13$ is a composite number. Justify this statement. (Average)
40. If the L.C.M of (91, 26) is 182, then find the H.C.F of (91, 26) (Easy)
41. What is a composite number? Which is the composite number among 23 and 24? (MQP 2024:Easy)
42. Find the largest number that divides 438 and 606 without leaving any remainder. (MTE 2024:Average)
43. Prove that $\sqrt{3} + 5$ is an irrational number. (MQP,2024 : Average)
44. Prove that $\sqrt{5} - 7$ is an irrational number. (Average)
45. Prove that $2 + \sqrt{5}$ is an irrational number. (April 2018:Average)
46. Prove that $6 + \sqrt{2}$ is an irrational number. (June 2025:Average)
47. Prove that $5 - \sqrt{3}$ is an irrational number. (Average)
48. Prove that $3 + 2\sqrt{5}$ is an irrational number. (Average)
49. Prove that $2\sqrt{3} - 4$ is an irrational number. (Average)
50. There is a circular path around a sports field. A takes 18 minutes to drive one round of the field, while B takes 24 minutes for the same. Suppose they both start at the same point and at the same time, and go in the same direction, after how many minutes will they meet again at the starting point? (Average)
51. According to fundamental theorem of arithmetic, if $40 = x^y z$, then find the value of x, y and z (April 2025:Average)
52. The length and breadth of a rectangular field are 147m and 56m respectively. Calculate the maximum length of a rod that can be used to measure both length and breadth exactly. How many times this rod has to be used to measure the length of the field? (May 2025 Average)
53. A sweet seller has 420 kaju barfis and 130 badam barfis. She wants to stack them in such a way that each stack has the same number of barfis, and they take up the least area of the tray. What is the number of barfis that can be placed in each stack for this purpose? (Average)

IV. Answer the following questions. (3 Marks)

54. Prove that $\sqrt{2}$ is an irrational number. (Average)
55. Prove that $\sqrt{3}$ is an irrational number. (September-2020 : Average)
56. Prove that $\sqrt{5}$ is an irrational number. (June-2020 : Average)

57. Find the H.C.F and L.C.M of the numbers 510 and 92 by the method of prime factorization and verify that $L.C.M \times H.C.F = \text{The product of the numbers}$ (SLP-2024 : Average)
58. Find the H.C.F and L.C.M of the integers 336 and 54 by the method of prime factorization and verify that $L.C.M \times H.C.F = \text{The product of the integers.}$ (SLP-2024 : Average)
59. Find the H.C.F and L.C.M of 26 and 91 by the method of prime factorization and verify that $L.C.M \times H.C.F = \text{The product of the numbers}$ (Average)
60. Find the H.C.F of 135 and 75 by prime factorization method and then find the L.C.M of H.C.F(135, 75) and 20. (SLP-2020:Difficult)
61. Find the L.C.M and H.C.F of 12, 15 and 21 by prime factorization method. (Average)
62. Find the L.C.M and H.C.F of 6, 72 and 120 by prime factorization method. (Average)
63. An army contingent of 616 members is to march behind an army band of 32 members in a parade. The two groups are to march in the same number of columns. What is the maximum number of columns in which they can march? Also find the number of rows of each team. (Difficult)

UNIT 2 : POLYNOMIALS

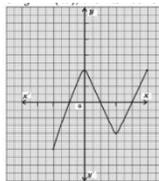
Learning Points:

- ❖ Degree of a polynomial
- ❖ Types of polynomials
- ❖ Zeroes of the polynomial
- ❖ Geometrical meaning of the zeroes of a polynomial
- ❖ Relationship between Zeroes and Coefficients of a Polynomial
- ❖ Finding a polynomial when its zeroes are given

Number of questions	Easy	Average	Difficult
56	33	10	13

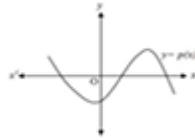
I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. The degree of a polynomial $p(x) = x^2 - 3x + 4x^3 - 6$ is, [MQP 2018, Easy]
 A) 2 B) 1 C) 3 D) 6
2. The degree of a linear polynomial is, [MQP 2019, Easy]
 A) 0 B) 1 C) 2 D) 3
3. The degree of a polynomial $p(x) = 2x^3 + 3x - 11 + 6$ is, [Easy]
 A) 2 B) 6 C) 3 D) 4
4. The degree of a quadratic polynomial is, [Easy]
 A) 4 B) 1 C) 3 D) 2
5. The degree of a cubic polynomial is, [MARCH 2020 Easy]
 A) 4 B) 1 C) 3 D) 2
6. The maximum number of zeroes of a quadratic polynomial is, [SLP 2024, Easy]
 A) 4 B) 1 C) 2 D) 3
7. In the quadratic polynomial $f(x) = x^2 - 9x + 20$ the value of $f(0)$ is, [Easy]
 A) 20 B) 11 C) -20 D) 29
8. In the polynomial $p(x) = x^2 - 1$, the value of $p(2)$ is, [Easy]
 A) 2 B) 3 C) 0 D) 1
9. In the figure, the number of zeroes of the polynomial $y = p(x)$ represented in the graph is, [JUNE 2019, Easy]



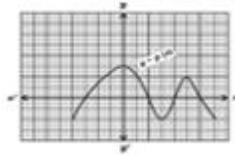
- A) 4 B) 3 C) 2 D) 7

10. In the figure, the polynomial $y = p(x)$ is represented in the graph. The number of zeroes of the polynomial is, [Easy]



- A) 4 B) 2 C) 3 D) 1

11. In the figure, the number of zeroes of the polynomial $y = p(x)$ is, [Easy]

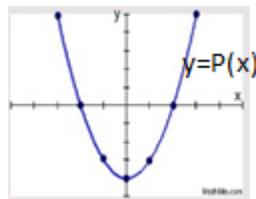


- A) 3 B) 5 C) 4 D) 2

12. The quadratic polynomial whose sum and product of the zeroes are -2 and 8 is, [SLP 2019, Difficult]

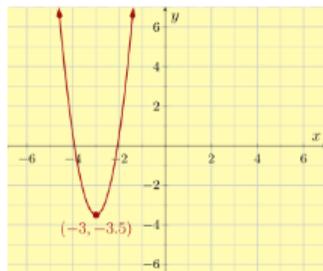
- A) $x^2 + 2x + 8$ B) $x^2 - 2x - 8$ C) $x^2 + 2x - 8$ D) $x^2 - 2x + 8$

13. In the figure, the number of zeroes of the polynomial $y = p(x)$ is, [Easy]



- A) 1 B) 3 C) 2 D) 4

14. In the figure, the zeroes of the polynomial $y = p(x)$ is, (EASY)



- A) 1 and -4 B) -3 and -4 C) -2 and -4 D) -1 and -4

15. If α and β are the zeroes of the polynomial $p(x) = ax^2 + bx + c$, then the value of $\alpha \times \beta$ is, [APRIL 2024, Easy]

- A) $\frac{b}{a}$ B) $\frac{-b}{a}$ C) $\frac{c}{a}$ D) $\frac{-c}{a}$

16. If α and β are the zeroes of the polynomial $p(x) = ax^2 + bx + c$, then the value of $\alpha + \beta$ is, [Easy]

- A) $\frac{b}{a}$ B) $\frac{-b}{a}$ C) $\frac{c}{a}$ D) $\frac{-c}{a}$

17. If one of the zeroes of the polynomial $p(x) = x^2 - x + k$ is 2, then the value of k is, [JUNE 2019, Difficult]

- A) 2 B) -2 C) -6 D) 6

18. If the sum of the zeroes of the polynomial $p(x) = kx^2 + 2x + 3k$ is equal to the product of its zeroes, then the value of k is, [Average]

- A) $\frac{2}{3}$ B) $\frac{-2}{3}$ C) $\frac{3}{4}$ D) $\frac{-3}{4}$

19. The quadratic polynomial whose sum and product of the zeroes are 4 and 5 respectively is, [MQP 2023, Easy]

- A) $p(x) = x^2 - 4x - 5$ B) $p(x) = x^2 + 4x - 5$ C) $p(x) = x^2 - 5x + 4$ D) $p(x) = x^2 - 4x + 5$

20. The sum of the zeroes of the polynomial $p(x) = x^2 - 2x - 8$ is, [MQP 2024, Average]

- A) -8 B) 2 C) -2 D) 8

21. If the graph of a polynomial $P(x)$ passes through the coordinate points $(-3,0)$, $(-1,-5)$, $(0, -6)$ and $(2,0)$ then the zeroes of the quadratic polynomial are, [MQP 2024: Difficult]

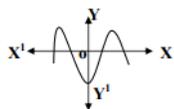
- A) -3 and -6 B) 0 and -3 C) -1 and -5 D) -3 and 2

II. Answer the following questions. (1 Mark)

22. What is the maximum number of zeroes of a cubic polynomial? [Easy]

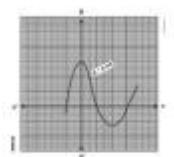
23. Find the number of zeroes of the polynomial $p(x)$ from the given graph.

[MQP 2020, Easy]



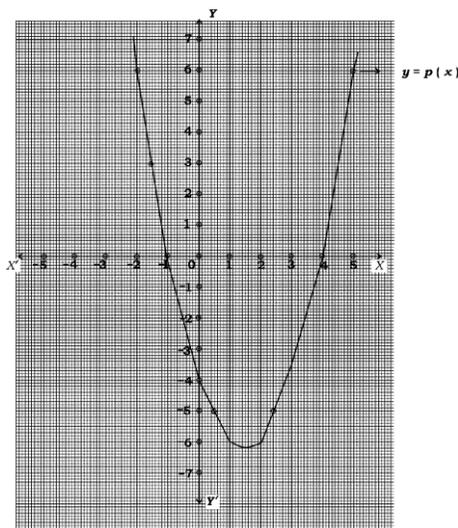
24. Find the number of zeroes of the polynomial $p(x)$ from the given graph.

[JUNE 2020, APRIL 2023, Easy]



25. Write the degree of the polynomial $p(x) = x^3 + 2x^2 - 5x^4 - 6$ [APRIL 2016, Easy]

26. Write the degree of the polynomial $f(x) = x^2 - 3x^3 + 2$ [APRIL 2018, Easy]
27. Write the degree of the polynomial $f(x) = 2x^2 - x^3 + 5$ [APRIL 2019, Easy]
28. Write the degree of the polynomial $p(x) = 3x^3 - 4x^2 + 5x^4 - 3x + 4$ [APRIL 2023, Easy]
29. Write the degree of the polynomial $p(x) = x(x^2 + 2x) + 3x - 5$ [Average]
30. Write the degree of the polynomial $g(p) = 7p^4 - 2p^3 + 3p^2 + p - 3$ [MQP 2024, Easy]
31. Find the sum of the zeroes of the polynomial $P(x) = x^2 - 5x + 6$ [JUNE 2023, Easy]
32. Find the product of the zeroes of the polynomial $P(x) = 2x^2 - 9x + 10$ [SLP 2020, Easy]
33. Find the sum of the zeroes of the polynomial $P(x) = x^2 + 7x + 10$ [March 2024, Easy]
34. If the product of the zeroes of the polynomial $f(x) = 2x^2 - 3x + k$ is 3, then find the value of 'k'. [Average]
35. Write the quadratic polynomial whose sum and product of the zeroes are -3 and 2 respectively. [SLP 2019, Easy]
36. Find the zeroes of the polynomial $p(x) = x^2 - 3$ [Easy]
37. Find the zeroes of the polynomial $p(x) = x^2 - 25$ [Easy]
38. If $P(x) = 2x^3 + 3x^2 - 11x + 6$, then find the value of $p(1)$ [Average]
39. Write the zeroes of the polynomial $y=p(x)$ given in the graph. [MARCH 2025, Easy]



III. Answer the following questions. (2 Marks)

40. Write the standard form of linear polynomial and quadratic polynomial. [MQP 2020, Easy]
41. Find the zeroes of the polynomial $P(x) = 6x^2 - 3 - 7x$ [MQP 2019, Average]
42. Find the zeroes of the polynomial $P(x) = 4x^2 - 4x - 3$ [APRIL 2019, Average]
43. If the sum of zeroes of the polynomial $p(x) = ax^2 + bx + c$ is -3 and product of the zeroes is 2, then prove that $b + c = 5a$ [Difficult]
44. If α and β are the two zeroes of the polynomial $P(x) = x^2 - 4x + 5$ then find the value of $\alpha^2 + \beta^2$. [Difficult]

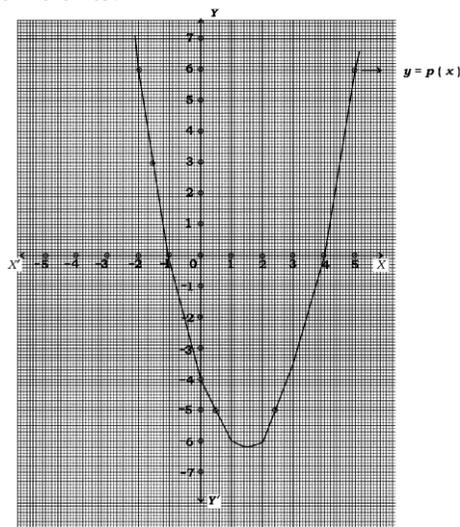
45. If α and β are the two zeroes of the polynomial $P(x) = x^2 + 3x + 1$ then find the value of $\frac{1}{\alpha} + \frac{1}{\beta}$ [Difficult]
46. If α and β are the two zeroes of the polynomial $P(x) = x^2 + 3x + 1$ then find the value of $\alpha^2\beta + \alpha\beta^2$ [Difficult]
47. One of the zeroes of the polynomial $P(x) = 2x^2 - 6x + k$ is twice the other. Find the value of 'k' [SEPT 2020, Average]
48. The sum and product of the zeroes of the polynomial $P(x) = ax^2 + bx - 4$ are $\frac{1}{4}$ and -1 respectively. Find the value of a and b [Average]
49. Find the zeroes of the polynomial $P(x) = x^2 - 5x + 6$ [Average]
50. Find the polynomial whose zeroes are $\sqrt{3}$ and $-\sqrt{3}$ (Difficult)

IV. Answer the following questions. (3 Marks)

51. Find the zeroes of the quadratic polynomial $p(x) = x^2 - 2x - 8$ and verify the relationship between the zeroes and the coefficients. [Difficult]
52. Find the zeroes of the quadratic polynomial $p(x) = x^2 + 7x + 10$ and verify the relationship between the zeroes and the coefficients. [JUNE 2023, APRIL 2025, Difficult]
53. Write the quadratic polynomial whose sum and product of the zeroes are -3 and 2 respectively and find the zeroes of this polynomial. [MARCH 2024, Difficult]
54. Write the quadratic polynomial whose sum and product of the zeroes are 7 and 12 respectively and find the zeroes of this polynomial. [JUNE 2024, Difficult]

V. Answer the following questions. (4 Marks)

55. Find the quadratic polynomial represented in the graph. Verify the relationship between the zeroes and the coefficients. (Difficult)



VI. Answer the following question. (5 Marks)

56. Write the quadratic polynomial whose sum and product of the zeroes are -6 and 8 respectively. Find the zeroes of this polynomial. Verify the relationship between the zeroes and the coefficients. (Difficult)

UNIT 3 : PAIR OF LINEAR EQUATIONS IN TWO VARIABLES

Learning Points:

1. Introduction to a pair of linear equations in two variables
2. The standard form of a pair of linear equations in two variables
3. Graphical Method of Solution of a Pair of Linear Equations
4. Interpretation of the relationship between the ratio of coefficients of linear equations
5. Algebraic Methods of Solving a Pair of Linear Equations
 - (i) Substitution Method
 - (ii) Elimination Method
6. Application Problems

Number of questions	Easy	Average	Difficult
51	12	29	10

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. If the lines drawn for the pair of linear equations $a_1x+b_1y+c_1=0$ and $a_2x+b_2y+c_2=0$ are coincident then the correct relation among the following is, (June-2025, Easy)

A) $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ B) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ C) $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ D) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2} = \frac{c_1}{c_2}$

2. If the lines drawn for the pair of linear equations $a_1x+b_1y+c_1=0$ and $a_2x+b_2y+c_2=0$ are intersecting then the correct relation among the following is, (July-2021, Easy)

A) $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ B) $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ C) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ D) $\frac{a_1}{b_2} = \frac{b_1}{a_2}$

3. In the pair of linear equations, $a_1x+b_1y+c_1=0$ and $a_2x+b_2y+c_2=0$ if $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ then,

(June-2022, Easy)

- A) Equations do not have any solution
- B) Equations have unique solution
- C) Equations have three solutions
- D) Equations have infinitely many solutions

4. If the pair of linear equations $a_1x+b_1y+c_1=0$ and $a_2x+b_2y+c_2=0$ have unique solution, then the correct relation among the following is,

(Easy)

A) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ B) $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ C) $\frac{a_1}{a_2} = \frac{b_1}{b_2}$ D) $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

5. The lines representing the equations $2x+3y-9=0$ and $4x+6y-18=0$ are
 A) Intersecting lines B) Perpendicular to each other (April-24, Average)
 C) Parallel lines D) Coincident lines
6. The lines representing the equations $x+2y-4=0$ and $2x+4y-12=0$ are
 (September-2020, Average)
 A) Intersecting lines B) Parallel lines
 C) Perpendicular to each other D) Coincident lines
7. The pair of linear equations $2x-5y+4=0$ and $2x+y-8=0$ has (Easy)
 A) exactly two solutions
 B) infinitely many solutions
 C) unique solution
 D) no solution
8. The lines represented by the pair of linear equations $x - 2y=0$ and $3x+4y - 20=0$ are
 (July-2021, Average)
 A) intersecting lines B) perpendicular to each other
 C) parallel lines D) coincident lines
9. If the pair of linear equations $x+2y - 4 =0$ and $2x+4y - 12=0$ are represented in a graph they are
 (April-2024, Average)
 A) intersecting lines B) perpendicular to each other
 C) parallel lines D) coincident lines
10. The lines represented by the pair of linear equations $x - y =8$ and $3x - 3y=16$ are
 (June-2022, Average)
 A) intersecting lines B) perpendicular to each other
 C) parallel lines D) coincident lines
11. If a pair of linear equations is inconsistent then the lines represented by them are
 (Easy)
 A) intersecting lines B) perpendicular to each other
 C) parallel lines D) coincident lines
12. If the lines represented by the pair of linear equations $x+2y=3$ and $2x+4y=k$ are coincident then the value of 'k' is,
 (August-2024, Difficult)
 A) 3 B) 6 C) -3 D) -6
13. If the lines represented by the pair of linear equations $3x+2ky=2$ and $2x+5y+1=0$ are parallel then the value of 'k' is,
 (Difficult)
 A) $-\frac{5}{4}$ B) $\frac{2}{5}$ C) $\frac{15}{4}$ D) $\frac{3}{2}$

14. The pair of linear equations representing coincident lines among the following is, (Average)

A) $x-2y=0$
 $3x+4y=20$

B) $2x+3y=9$
 $4x+6y=18$

C) $x+2y=4$
 $2x+4y=12$

D) $x+y=8$
 $x-y=4$

15. The incorrect statement with respect to the lines represented by the pair of linear equations among the following is, (Average)

A) If the lines are parallel, then the equations have no solution

B) If the lines are perpendicular to each other, then the equations have no solution

C) If the lines are coincident, then the equations have infinitely many solutions

D) If the lines are intersecting, then the equations have unique solution

16. The values of x and y which satisfy the equation $2x+3y=16$ are (Average)

A) $x=5, y=2$

B) $x=2, y=5$

C) $x=-5, y=-2$

D) $x=-5, y=2$

II. Answer the following questions (1 mark)

17. Write the standard form of a pair of linear equation with variables ' x ' and ' y '. (Easy)

18. How many solutions does the pair of linear equations in two variables have if they are inconsistent? (April-2022, Average)

19. How many solutions does the pair of linear equations $a_1x+b_1y+c_1=0$ and $a_2x+b_2y+c_2=0$ have if $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$? (September-2022, Easy)

20. How many solutions does the pair of linear equations in two variables have if the lines represented by them are coincident? (Easy)

21. The perimeter of a rectangle having length ' l ' units and breadth ' b ' units is 32m. Form a linear equation in two variables for this statement. (Average)

22. In a class, 'The number of boys (x) is 1 more than twice the number of girls (y)'. Form a linear equation in two variables for this statement. (Average)

23. If the lines represented by the equations $x+2y-4=0$ and $ax+by-12=0$ are coincident, then find the value of ' a ' and ' b '. (Average)

24. If the lines represented by the equations $4x+py+8=0$ and $4x+4y+2=0$ are parallel, then find the value of 'p'.
(Difficult)

25. How many solutions does the pair of linear equations $x+2y-4=0$ and $3x+2y-5=0$ have?
(June-2023, Easy)

26. How many solutions does the pair of linear equations $2x+3y-9=0$ and $4x+6y-18=0$ have?
(Easy)

27. How many solutions does the pair of linear equation in two variables have if the lines represented by them are intersecting?
(June-2024, Easy)

28. How many solutions does the pair of linear equations $2x-3y+4=0$ and $3x+5y+8=0$ have?
(April-2024, Average)

29. How many solutions does the pair of linear equations $2x + 3y - 9 = 0$ and $3x - 2y + 6 = 0$ have?
(March-2025, Average)

III. Answer the following questions (2 marks)

30. Solve the given pair of linear equations by elimination method.
 $2x + y = 10$
 $x - y = 2$
(March- 2025, Average)

31. Solve the given pair of linear equations by elimination method.
 $3x - y = 15$
 $2x - y = 5$
(Average)

32. Solve the given pair of linear equations by elimination method.
 $2x + y = 8$
 $x - y = 1$
(June-2024, Average)

33. Solve the given pair of linear equations by substitution method.
 $x + y = 14$
 $x - y = 4$
(Average)

34. Solve the given pair of linear equations by substitution method.
 $x + 2y = 8$
 $x - y + 1 = 0$
(Average)

35. Solve the given pair of linear equations by elimination method.
 $2x+y=8$
 $3x - y = 7$
(March-2024, Average)

36. The sum and difference of two positive integers are 10 and 2 respectively. Find the integers.
(Average)

37. The sum of two positive integers is 15. If one number is 1 more than the other, then find the integers.
(Average)

38. Solve the given pair of linear equations by elimination method. (Difficult)

$$3x+2y=5$$

$$x - y = 1$$

39. Solve the given pair of linear equations by elimination method. (Difficult)

$$2x + 5y = 7$$

$$5x + 2y = 7$$

IV. Answer the following questions (3 mark)

40. A fraction becomes $\frac{9}{11}$ when 2 is added to both numerator and denominator but when 3 is added to both numerator and denominator it becomes $\frac{5}{6}$. Find the fraction

(Difficult)

41. After 10 years x will be twice as old as 'y'. Ten years ago, the age of 'x' was six times of 'y'. Find their present ages. (Difficult)

42. Ritu takes 2 hours to row 20 km downstream and 2 hours to row 4 km upstream. Determine Ritu's speed in still water and the speed of the stream.

(Difficult)

43. The ratio of monthly income of two persons is 9 : 7 and the ratio of their monthly expenditures is 4 : 3. If each of them manages to save Rs. 2000 at the end of the month then find their monthly income.

(Difficult)

44. Five years hence, the age of 'A' will be three times that of his son. Five years ago, 'A's age was seven times that of his son. Find their present ages.

(Difficult)

V. Answer the following questions (4 mark)

45. Solve the given pair of linear equations by graphical method.

$$2x+y=6$$

$$2x-y=-2$$

(Average)

46. Solve the given pair of linear equations by graphical method.

$$x+2y=6$$

$$x+y=2$$

(Average)

47. Solve the given pair of linear equations by graphical method.

$$2x+y=8$$

$$x-y=1$$

(June-2019, Average)

48. Solve the given pair of linear equations by graphical method.

$$x+2y=6$$

$$x+y=5$$

(March-2025, Average)

49. Solve the given pair of linear equations by graphical method.

$$\begin{aligned}x+3y&=6 \\2x-3y&=12\end{aligned}$$

(March-2019, Average)

50. Solve the given pair of linear equations by graphical method.

$$\begin{aligned}2x+y&=6 \\2x-y&=2\end{aligned}$$

(May-2025, Average)

51. Solve the given pair of linear equations by graphical method.

$$\begin{aligned}2x-y&=7 \\x-y&=2\end{aligned}$$

(July-2022, Average)

UNIT 4 : QUADRATIC EQUATIONS

Learning Points:

- ❖ Definition of quadratic equation and the standard form
- ❖ Identifying quadratic equations among the given equations
- ❖ Solution to quadratic equations by factorization method
- ❖ Discriminant of a quadratic equation and nature of roots
- ❖ Application problems

Number of questions	Easy	Average	Difficult
73	16	44	13

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. The standard form of a quadratic equation is,

(MQP II -2020 : Easy)

- A) $ax^2-bx+c=0$ B) $ax^2+bx+c=0$ C) $ax^2-bx-c=0$ D) $ax^2-bx-c=0$

2. The quadratic equation among the following is,

(APRIL-2025 EXAM-1 : Average)

- A) x^3-6x B) $p(x)=x^2+7x$ C) $3x = 9$ D) $x^2+3x+4=0$

3. The quadratic equation among the following is,

(SLP-2022 : Easy)

- A) $x^{-2} - 3x + 2 = 0$ B) $2x + 3 = 0$ C) $x^2 - 5x + 6 = 0$ D) $2x^3 + 7x + 1 = 0$

4. The constant obtained when the quadratic equation $5x^2=2(2x+3)$ is written in the standard form is,

(MQP II -2020 : Average)

- A) 5 B) 6 C) 4 D) -6

5. $x(x+2)=6$ This is a (MQP-1: 2025 : Average)

- A) linear equation B) quadratic equation
C) cubic polynomial D) quadratic polynomial

6. The standard form of a quadratic equation $2x^2 = 3x - 5$ is, (Easy)

- A) $x^2 - x + 5 = 0$ B) $2x^2 + 3x - 5 = 0$
C) $2x^2 - 3x - 5 = 0$ D) $2x^2 - 3x + 5 = 0$

7. The product of two consecutive positive integers is 30. The equation for this statement is, (APRIL -2019 : Easy)

- A) $(x+2)=30$ B) $(x-2)=30$ C) $(x-3)=30$ D) $x(x+1)=30$

8. The discriminant of the quadratic equation $ax^2 + bx + c = 0$ is, (APRIL-2024 EXAM-3 : Easy)

- A) $b^2 - 4ac$ B) $c^2 - 4ab$ C) $b^2 + 4ac$ D) $a^2 + 4ab$

9. The value of discriminant of the quadratic equation $x^2 + 4x + 4 = 0$ is, (SLP-2024 : Average)

- A) 0 B) 12 C) 16 D) 48

10. If the value of discriminant of a quadratic equation is zero, then the nature of the roots is (MQP-2022 : Easy)

- A) Distinct, Real and Irrational B) Real and Equal
C) Distinct, Real and Rational D) No real roots

11. The nature of the roots of the quadratic equation $x^2 - 2x + 1 = 0$ is, it has (MQP-2021 - Average)

- A) it has two equal real roots
B) it has two distinct, real and rational roots
C) it has two distinct, real and irrational roots
D) it has no real roots

12. If the roots of the quadratic equation $x^2 + 6x + k = 0$ are real and equal, then the value of ' k ' is, (MQP 1-2020- Average)

- A) 9 B) -9 C) 8 D) 5

13. If the roots of the quadratic equation $ax^2 + bx + c = 0$ are real and distinct, then (SLP-2024 – Easy)

- A) $a^2 - 4ac > 0$ B) $b^2 - 4ac = 0$ C) $a^2 - 4ac = 0$ D) $b^2 - 4ac > 0$

14. The roots of the equation $(x-3)(x+2) = 0$ are (JULY-2021 : Easy)

- A) -3,2 B) 3,-2 C) -3,-2 D) 3,2

15. If one of the roots of the quadratic equation $(2x-3)(x+5)=0$ is -5 then the other root is, (MQP-2021 : Easy)

- A) 5 B) $\frac{-3}{2}$ C) $\frac{3}{2}$ D) $\frac{2}{3}$

16. If one of the roots of the quadratic equation $2x^2 + ax + 6 = 0$ is 2 then the value of 'a' is (JULY-2021 : ಸಾಧಾರಣ)

- A) 7 B) $\frac{7}{2}$ C) -7 D) $\frac{-7}{2}$

II. Answer the following questions (1 mark)

17. Express the equation $x(2+x)=3$ in the standard form of a quadratic equation (APRIL -2023 : Easy)

18. Express the equation $\frac{x+1}{2} = \frac{1}{x}$ in the standard form of a quadratic equation.

(JUNE -2020 : Average)

19. Write the discriminant of the quadratic equation $px^2 + qx - r = 0$

(MQP-2020 : Average)

20. Find the discriminant of the quadratic equation $2x^2 - 4x + 3 = 0$

(APRIL-2019 : Average)

21. If one of the roots of the quadratic equation $(x+4)(x+3)=0$ is -4 then find the other root.

(SEPT -2020: Easy)

22. Find the roots of the quadratic equation $(x-1)(x+3) = 0$

(SLP -2024 : Easy)

23. Find the discriminant of the quadratic equation $x^2 - 5x + 1 = 0$

(JUNE-2023 : Average)

24. Write the nature of the quadratic equation $x^2 - 9 = 0$

(MQP-4, 2024 : Average)

25. Write the equation $2m^2 = 2 - m$ in the standard form of the quadratic equation.

(Easy)

26. Find the roots of the quadratic equation $x^2 - x = 0$

(Easy)

27. Write the roots of the quadratic equation $x(x + 2) = 0$

(MARCH-2025 : Easy)

28. Write the roots of the quadratic equation $ax^2 + bx + c = 0$

(May 2025 Easy)

29. 'The product of two consecutive positive integers is 306'. Write this statement in the standard form of quadratic equation.

(Average)

III. Answer the following questions (2 marks)

30. Find the roots of the quadratic equation $x^2 + 7x + 12 = 0$ by factorization method.
(JUNE-2019 : Average)
31. Find the roots of the quadratic equation $x^2 + 4x - 60 = 0$
(MQP-4,2024 : Average)
32. Find the roots of the quadratic equation $x^2 + 3x + 2 = 0$ by factorisation method.
(MQP-2, 2024 : Average)
33. Find the roots of the quadratic equation $2x^2 + x - 6 = 0$
(SLP-4,2024 : Average)
34. Find the roots of the quadratic equation $x^2 + 8x + 12 = 0$
(APRIL-2025 : Average)
35. Find the discriminant of the quadratic equation, $2x^2 - 5x + 3 = 0$ and write the nature of the roots.
(SEPT-2020 : Average)
36. Find the discriminant of the quadratic equation, $4x^2 - 4x + 1 = 0$ and write the nature of the roots.
(JUNE-2019 : Average)
37. Find the discriminant of the quadratic equation, $2x^2 - 6x + 3 = 0$ and write the nature of the roots.
(MQP-1,-2021 : Average)
38. Find the discriminant of the quadratic equation, $x^2 + 4x + 4 = 0$ and write the nature of the roots.
(SLP-2024, Average)
39. Find the discriminant of the quadratic equation, $2x^2 - 5x - 1 = 0$ and write the nature of the roots.
(SEPT-2020, Average)
40. Prove that the roots of the quadratic equation $x^2 + ax - 4 = 0$ are real and distinct.
(MQP-1,2021 : Average)
41. For what value of 'k' the roots of the equation $kx^2 + 6x + 1 = 0$ are equal?
(SLP-2022 : Average)
42. If the quadratic equation $x^2 + bx + 9 = 0$ has two equal real roots then find the equation.
(MQP-1,2024:Average)
43. Find the value of 'k' for which the quadratic equation $2x^2 + kx + 3 = 0$ has equal real roots.
(MQP-2, 2024 :Average)
44. Find the discriminant of quadratic equation $x^2 + 4x + 5 = 0$ and hence write the nature of the roots.
(APRIL-2024 :Average)
45. Find the roots of the equation $3x^2 - 5x + 2 = 0$ by Factorisation method.
(MQP-2,2021 :Average)

IV. Answer the following questions (3 marks)

46. The sum of the areas of two squares is $640m^2$. If the difference between their perimeters is 64 m, then find the sides of the square. (MQP-1,2020 :Average)
47. The sum of the squares of two consecutive odd positive integers is 290. Find the integers. (MQP-2,2021 :Average)
48. Age of mother is twice the square of age of her son. After 8 years mother's age will be 4 years more than the thrice the age of her son. Find their present ages. (APRIL-2023:Average)
49. The difference between the altitude and base of a right angled triangle is 5cm. If the area of the triangle is $150cm^2$, then find the base and altitude of the triangle. (APRIL-2025 :Difficult)
50. The sum of the squares of two consecutive even positive integers is 164. Find the integers. (APRIL-2024:Average)
51. Find the two numbers whose sum is 27 and the product is 182. (MQP-1,2024 :Average)
52. The altitude of a right angled triangle is 7 cm less than its base. If the hypotenuse is 13 cm, then find the other two sides. (MQP-1,2024: Average)
53. A student bought some books for Rs.60. Had he bought 5 more books for the same amount each book would have cost Rs.1 less. Find the number of books bought by him. (MQP-2,2024 :Difficult)
54. Age of a father is 30 years more than his son. After 5 years, the product of their ages becomes 400. Find the present ages of both the son and father. (MQP-3,2024 :Average)
55. A number is 3 more than the other number. If the sum of their squares is 29 then find the numbers. (MQP-3, 2024: Average)
56. The base of a triangle is 4 cm more than twice its height. If the area of triangle is $48cm^2$, then find the length of the base and height of the triangle. (MQP-4,2024 :Average)
57. Some students planned a picnic. The budget for the food was Rs.900. As 10 of them failed to join the picnic, the cost of the food for each member was increased by Rs.15. Find how many students went for the picnic. (SLP-2024 :Difficult)
58. The area and perimeter of a rectangular field are $60 m^2$ and 32 m respectively. Find the length and breadth of the field. (MQP-2023:Average)
59. A train travels 480 km at a uniform speed. If the speed had been 10 km/h more, it would have taken 4 hours less for the same journey. Find the speed of the train. (MQP-2, 2021: Difficult).
60. The area and perimeter of a rectangular field are $400 m^2$ and 80 m respectively. Find the length and breadth of the field. (Average)
61. To save fuel, to avoid air pollution and for good health two persons 'A' and 'B' ride bicycle for a distance of 12 km to reach their office. As the cycling speed of 'B' is 2 km/h more than that of 'A', 'B' takes 30 minutes less than that of 'A' to reach the office. Find the time taken by A and B to reach the office. (April 2020 – Difficult)

62. A dealer sells an article for Rs. 24 and gains as much percent as the cost price. Find the cost price of the article. (Average)
63. A dealer sells an article for Rs. 24 and loses as much percent as the cost price. Find the cost price of the article. (Average)
64. If the equation $(1+m^2)x^2 + 2mcx + c^2 - a^2 = 0$ has equal roots, then prove that $c^2 = a^2(1+m^2)$ (Difficult)
65. If the roots of the equation $(b - c)x^2 + (c - a)x + (a - b) = 0$ are equal then prove that $2b = a + c$ (June 2019- Difficult)

V. Answer the following questions (4 mark)

66. A motor boat whose speed is 11km/h in still water takes 2 hours 45 minutes to go 12 km upstream then to return downstream to the same spot. Find the speed of the stream. (SLP-2024:Difficult)
67. The ages of two students 'A' and 'B' are 19 years and 15 years respectively. Find how many years it will take so that the product of their ages becomes equal to 480. (JUNE-2019 :Average)
68. A motor boat goes down the stream 30 km and again returns to the starting point in a total time of 4 hours and 30 minutes. If the speed of the stream is 5km/h, then find the speed of the motor boat in still water. (SLP-2020 :Difficult)
69. An express train takes 1 hour less than a passenger train to travel 132 km between two towns A and B. The Average speed of the express train is 11km/h more than that of a passenger train. Find the Average speed of these trains. (SLP-2022 :Difficult)
70. Age of person 'A' is 26 years more than age of person 'B' .The product of their ages 3 years from now will be 360. Find the present ages of person 'A' and person 'B' (SLP-2023 :Difficult)
71. A farmer wishes to grow a 100 m^2 rectangular vegetable garden. Since he has only 30m barbed wire, he fences the sides of the rectangular garden letting his house compound wall act as the fourth side fence. Find the dimensions of the garden. (Difficult)
72. The denominator of a fraction is one more than twice it numerator. The sum of this fraction and its reciprocal is $\frac{29}{10}$. Find the fraction. (May 2025 - Average)
73. In a school, it was decided to distribute Rs. 1500 equally to the students who secure A+ grade in the 10th standard annual examination. But after the results, 5 more students secured A+ grade than expected before the examination. Hence the amount received by each student was reduced by Rs. 25. Find the number of students who secured A+ grade after examination (SLP- 2025: Difficult)

UNIT 5 : ARITHMETIC PROGRESSIONS

Learning Points:

- ❖ Definition of an arithmetic progression
- ❖ General form of an arithmetic progression
- ❖ nth term of an arithmetic progression
- ❖ The sum of n terms of an arithmetic progression
- ❖ Application problems

Number of questions	Easy	Average	Difficult
84	20	56	8

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

- The arithmetic progression in the following is, (Easy)
A) 1, 2, 4, 8..... B) 3, 7, 10, 14..... C) 1, 4, 9, 16..... D) 5, 9, 13, 17.....
- The common difference of the arithmetic progression -7,-9,-11,-13..... is, (Easy)
A) -7 B)-2 C)2 D)3
- The common difference of the arithmetic progression 100 , 93 , 86..... is, (MARCH 2025) (Easy)
A) -7 B) 7 C) 3 D) 5
- The formula to find the n^{th} term of an arithmetic progression is (AUG 2024) (Easy)
A) $a_n = a + (n-1) d$ B) $a_n = a + (n + 1) d$ C) $a_n = a - (n - 1)d$ D) $a_n = n+1$
- If the n^{th} term of an arithmetic progression is $5n+3$, then the 3^{rd} term of the progression is, (June 2019) (Average)
A) 11 B) 18 C) 12 D) 13
- If the n^{th} term of an arithmetic progression $a_n= 3n - 2$, then the 9th term is (September 2020) (Easy)
A) -25 B) 5 C) -5 D) 25

7. If the n^{th} term of an arithmetic progression $a_n = 24 - 3n$, then the 2^{nd} term is, (APRIL 2019) (Easy)
- A) 18 B) 15 C) 0 D) 2
8. If the n^{th} term of the arithmetic progression $a_n = 2n - 1$ then the 4^{th} term is, (Easy)
- A) -7 B) 7 C) 5 D) 6
9. In an arithmetic progression if $a_n = 3n+4$ then a_{n+1} term is, (Average)
- A) 3 B) $3n+1$ C) $3n+7$ D) $3n+5$
10. In an arithmetic progression, if $a_n = 2n+1$ then the common difference of the progression is, (JUNE 2020) (Easy)
- A) 0 B) 1 C) 2 D) 3
11. If 6, x , 14 are in arithmetic progression, then the value of x is, (APRIL 2024: Easy)
- A) 10 B) 20 C) 18 D) 12
12. In an arithmetic progression, if $a = 12$, $d = 4$, $a_n = 76$ then, $n =$ (Average)
- A) 17 B) 18 C) 16 D) 19
13. In an arithmetic progression, if $a = -7$, $d = 5$ then, $a_{12} =$ (Average)
- A) 48 B) 45 C) 46 D) 42
14. If the first term of an arithmetic progression is 'm' and the common difference is 3 then the 10^{th} term of the progression is, (Average)
- A) $m + 25$ B) $m + 12$ C) $m + 30$ D) $m + 27$
15. If $(2p+1)$, 13, $(5p-3)$ are the three consecutive terms of an arithmetic progression, then the value of 'p' is, (Average)
- A) 4 B) -4 C) 2 D) 3
16. If 4, x_1 , a_n , x_2 , 22, 28 are in arithmetic progression, then the value of x_1 and x_2 respectively is, (Average)
- A) 10, 16 B) 16, 10 C) 16, 22 D) 22, 16

17. There are 20 terms in an arithmetic progression. If the first term is 2 and the last term is 78, then the arithmetic progression is, (JUNE 2024 EXAM 2 Average)
 A) 2, 5 8 B) 2, 7, 12, C) 2, 6, 10,.....
 D) 2, 4, 6,.....
18. The n th term of the arithmetic progression 3, 7, 11,..... is, (Average)
 A) $a_n = 4n-1$ B) $a_n = 3n-4$ C) $a_n = 4n-7$ D) $a_n = 4n + 1$
19. The formula to find the sum of all terms of the arithmetic progression with first term 'a' and the last term 'l' is (Easy)
 A) $s_n = \frac{n}{2} (a+1)$ B) $s_n = \frac{n}{2} (a-1)$ C) $s_n = \frac{n}{2} (a \times l)$ D) $s_n = \frac{n}{2} (a \div l)$
20. If a_n , S_n and S_{n-1} represent the n th term, sum of the first n terms and sum of first $(n-1)$ terms, then the correct relation among the following is, (JUNE 2025 - Easy)
 A) $S_{n-1} = a_n + S_n$ B) $a_n = S_n - S_{n-1}$ C) $S_n = S_{n-1} - a_n$ D) $S_n = a_n - S_{n-1}$

II. Answer the following questions (1 Mark)

21. If the first term of an arithmetic progression is 'a' and the last term is ' a_n ' then write the formula to find the sum of the first n terms of the arithmetic progression. (JUNE 2019) (EASY)
22. In an arithmetic progression if 'b' is the first term and 'd' is the common difference, then write its ' n 'th term. (Easy)
23. If a, a+d, a+2d l is an arithmetic progression then find the n th term of the progression from the last term (Easy)
24. If the sum of three consecutive terms of an arithmetic progression is 21, then find the second term. (Average)
25. If the m th term of an arithmetic progression is 'n' and the n th term is 'm', then find the p th term. (Difficult)
26. In an arithmetic progression the sum of first 4 terms is 20 and the sum of first 3 terms is 12 then find the 4th term of the arithmetic progression. (Average)
27. If the 4th term of an arithmetic progression is 11 and the 3rd term is 7, then what is the common difference? (Average)
28. If the 3rd term of an arithmetic progression is 13 and the 2nd term is 8, then find the first term of the progression. (Average)

29. Write the general term of an arithmetic progression. (Easy)
30. If 4, x, 28 are in arithmetic progression then find the value of x. (Average)
31. If the n^{th} term of an arithmetic progression $a_n = 7 - 4n$ then find the common difference. (Average)
32. If the n^{th} term of an arithmetic progression $a_n = 4n + 1$ then find its first three terms (Average)

III. Answer the following questions. (2 marks)

33. Find the 15th term of the arithmetic progression 2, 7, 12,..... using formula.(Average)
34. Find the number of terms of the arithmetic progression 100, 96, 92,12. (Average)
35. There are 10 terms in an arithmetic progression. If the last term is 34 and common difference is 3, then find the first term of the progression. (Average)
36. Find out, which term of the arithmetic progression -1, 3, 7, 11..... is 95 using formula (Average)
37. Find whether 77 is a term of the arithmetic progression 1,5,9,13..... using formula. (Average)
38. Find the 26th term of the arithmetic progression 5, 8, 11..... using formula. (Average)
39. Find the 30th term of the arithmetic progression 2, 5, 8..... using formula. (AUG 2024) (APRIL 2024) (JUNE 2024 EXAM – 2) (Average)
40. Find the sum of the first 10 terms of the arithmetic progression 3+7+11..... using formula. (APRIL 2018) (MARCH 2025) (JUNE 2025) (Average)
41. Water is heated up to 24⁰C at constant pressure. When the heating of water is continued, the temperature of water is increasing at the rate of 4⁰C per minute. Find how many minutes are required for water to reach 100⁰ C using formula. (APRIL 2018) (Average)

42. Find the sum of the first 10 terms of the arithmetic progression $5+8+11+\dots$ using formula. (JUNE 2020) (Average)
43. Find the sum of first 20 positive integers using formula. (Average)
44. Find, which term of the arithmetic progression 21, 42, 63..... is 210 using formula. (Average)
45. Find the sum of the first n terms of the arithmetic progression $1,3,5,7,\dots,n$ using formula. (Average)
46. Find the sum of the first n terms of the arithmetic progression $2,4,6,8,\dots,n$ using formula. (Average)
47. How many two digit numbers are divisible by 3? (Average)
48. Find the sum of the natural numbers between 1 and 201 that are divisible by 5 using formula. (Average)
49. If a, A, b are in arithmetic progression, then prove that $A=\frac{a+b}{2}$. (Average)
50. Find, which is the first negative term of the arithmetic progression $25,20,15,\dots$ using formula. (Average)
51. Find, which term of the arithmetic progression $2,7,12,\dots$ is 47 using formula. (Average)
52. Find, which term of the arithmetic progression $3,15,27,39,\dots$ is 132 more than its 54^{th} term using formula. (Average)
53. Find how many terms of the arithmetic progression 3, 6, 9, must be added to get the sum 165. (July-2022: Average)

IV. Answer the following questions. (3 Marks)

54. The sum of first 6 terms in an arithmetic progression is 114. If the sum of first 5 terms of the progression is 80, then find the progression. (Average)
55. The 7^{th} term of an arithmetic progression is four times its 2^{nd} term. If the 12^{th} term is 2 more than thrice the fourth term, then find the arithmetic progression. (APRIL 2019) (Average)
56. Find the arithmetic progression whose third term is 16 and its 7th term exceeds the 5th term by 12. (July 2022: Average)
57. The 5^{th} term of an arithmetic progression is 26 and the common difference is three times the first term. Find the sum of first 20 terms of the progression. (Average)
58. The digits of a three digit number are in arithmetic progression and the sum of the digits is 15. If the digits of units place and hundreds place are interchanged, then the number obtained is 594 less than the original number. Find the original number. (Average)

59. The number 56 is divided into 4 parts such that they are the terms of arithmetic progression. If the ratio of the product of their extremes to the product of their means is 5:6 then find the four terms.
(Difficult)
60. A straight wooden stick of length 25 cm is cut into 5 parts whose lengths are in arithmetic progression. The sum of the squares of each part is 135. Find the length of the each part.
(Difficult)
61. The 9th term of an arithmetic progression is one more than 5 times its 2nd term and its 12th term is 7 more than twice the 5th term. Find the arithmetic progression.
(Average)
62. Find the sum of the integers between 1 and 100, all of which leave a remainder 1 when divided by 5.
(Average)
63. The sum of three numbers in an arithmetic progression is 216. The biggest number is 7 times the smallest number. Find the numbers.
(Average)
64. The sum of the 4th term and 8th term of an arithmetic progression is 24 and the sum of 6th term and 10th term of the progression is 44. Find the first three terms of the progression.
(JUNE 2019) (Average)
65. The three angles of a triangle are in arithmetic progression. If the smallest angle is half the biggest angle then find the measures of all the angles of the triangle.
(Average)
66. If the mth term of an arithmetic progression is $\frac{1}{n}$ and nth term is $\frac{1}{m}$ then prove that the mnth term is 1.
(Difficult)
67. If the pth term of an arithmetic progression is 'a', qth term is 'b' and rth term is 'c' then prove that $a(q-r) + b(r-p) + c(p-q) = 0$
(Difficult)
68. The sum of first 9 terms of an Arithmetic progression is 144 and its 9th term is 28. Then find the first term and common difference of the Arithmetic progression.
(April- 2022: Average)

IV. Answer the following questions. (4 Marks)

69. In an arithmetic progression the first term is 22, nth term is -11 and the sum of the first 'n' terms is 66. Find the number of terms of the progression and common difference.
(Average)

70. Five integers are in arithmetic progression. The difference obtained on subtracting the square of the first term from the square of the fifth term is 192 and the sum of the 2nd and 4th term is 16. Find the five terms of the progression
(Easy)
71. In an arithmetic progression the sum of the first 'n' term is 210 and the sum of the first (n-1) terms is 171. If the first term of the progression is 3, then find the progression. Also find the 20th term of the progression.
(APRIL 2024) (Average)
72. The sum of the interior angles of a polygon of 'n' sides is $(n - 2) 180^\circ$. The interior angles of a pentagon are in arithmetic progression. If the smallest angle is 72° then find the angles of the pentagon.
(April 2024 -Average)
73. A person works in a shop from Monday to Saturday. His every day earnings are in arithmetic progression. His total earnings from Monday to Wednesday are Rs. 525 and Friday he gets Rs. 100 more than his Monday's earning. Find his every day's earning.
(August 2024) (Average)
74. The angles of a quadrilateral are in arithmetic progression. If the sum of a pair of opposite angles is 130° , then find the angles of the quadrilateral.
(Average)
75. An arithmetic progression consists of 16 terms. The sum of all its terms is 768. If the last term of the progression is 93, then find the arithmetic progression. Also show that the sum of all the terms of this progression is equal to 3 times the sum of first 16 odd natural numbers using formula.
(March 2025 -Average)
76. In an arithmetic progression 7th term is five times its 2nd term and 5th term is 1 less than twice the 3rd term. Write the Arithmetic progression. Find the 15th term of this progression using formula.
(May 2025: Average)
77. The ratio of 11th and 8th terms of an arithmetic progression is 3:2. Find the ratio of sum of the first 5 terms to the sum of first 21 terms.
(Difficult)
78. The 7th term of an arithmetic progression is four times its 2nd term and the 12th term is 2 more than thrice its 4th term. Find the progression.
(Difficult)
79. The 'p'th term of an arithmetic progression is 'q' and 'q'th term is 'p'. Prove that 'r'th term of the progression is p+q-r
(Average)
80. There are five terms in an Arithmetic Progression. The sum of these terms is 55, and the fourth term is five more than the sum of the first two terms. Find the terms of the Arithmetic progression.
(April 2020: Average)

81. In an Arithmetic Progression sixth term is one more than twice the third term. The sum of the fourth and fifth terms is five times the second term. Find the tenth term of the Arithmetic Progression.

(April 2020: Average)

V. Answer the following questions. (5 Marks)

82. The sum of first 'n' terms of an arithmetic progression is $5n - n^2$. Write the progression. Find the 21st term and also find the sum of first 21 terms of the progression.

(Average)

83. The common difference of two different arithmetic progressions is equal. The first term of the first progression is 3 more than the first term of the second progression. If the 7th term of the first progression is 28 and the 8th term of the second progression is 29, then find the progressions.

(Difficult)

84. An arithmetic progression contains 30 terms. 17th term of the progression is 4 more than the thrice of its 5th term. The 10th term of the progression is 31. Find the last three terms of the progression and also find the progression.

(June-2024: Average)

UNIT 6 : TRIANGLES

Learning Points points:

- ❖ Similar Figures
- ❖ Similarity of triangles
- ❖ Thales theorem (Basic Proportionality theorem)
- ❖ Converse of Thales theorem
- ❖ AAA, SAS, SSS criterion for similarity of triangles
- ❖ Problems based on theorems

Number of Questions	Easy	Average	Difficult
55	18	30	7

I. Four alternatives are given for each of the following questions/incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

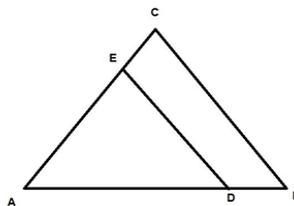
- 1) In the following, the shapes which are always similar are, (March 2025 (Easy)
 - A) Any two equilateral triangles
 - B) Square and rectangle
 - C) Square and rhombus
 - D) Any two trapeziums

- 2) Which of the following pair of triangles are always similar? [Model : 2022 , Average]
 - A) Two isosceles triangles
 - B) Two scalene triangles
 - C) Two equilateral triangles
 - D) Two right angled triangles

- 3) In $\triangle ABC$, $DE \parallel AB$. If $CD = 3$ cm, $EC = 4$ cm, $BE = 6$ cm, then DA is equal to (Average)

A) 7.5 cm B) 3 cm C) 4.5 cm D) 6 cm

- 4) D and E are the points on sides AB and AC of triangle ABC . If $DE \parallel BC$, $AD = 2$ cm, $BD = 3$ cm and $BC = 7.5$ cm and then length of DE is (Average)

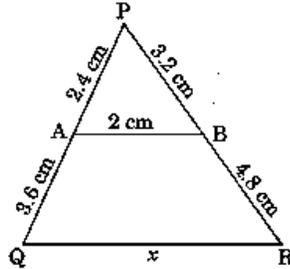


- A) 2.5 cm B) 3 cm C) 5 cm D) 6 cm

- 5) $\triangle ABC$ and $\triangle DEF$ are similar and if $\frac{AB}{DE} = \frac{BC}{FD}$ then the correct relation among the following is (Average)

A) $\angle B = \angle E$ B) $\angle A = \angle D$ C) $\angle B = \angle D$ D) $\angle A = \angle F$

- 6) In the figure, value of x is (Average)



A) 4 cm B) 5 cm C) 6 cm D) 8 cm

- 7) In $\triangle ABC$, $DE \parallel BC$, $AD = x$, $DB = x - 2$, $AE = x + 2$ and $EC = x - 1$ then value of x is (Average)

A) 3 B) 4 C) 5 D) 3.5

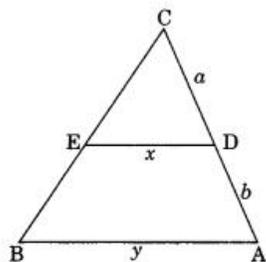
- 8) $\triangle ABC$ is similar to $\triangle DEF$ such that $2 AB = DE$ and $BC = 8$ cm, then length of EF is (Average)

A) 12 cm B) 4 cm C) 16 cm D) 8 cm

- 9) In $\triangle ABC$, $AE = \frac{1}{4} AC$, $AB = 6$ cm and $DE \parallel BC$ then length of AD is (Average)

A) 2 cm B) 1.2 cm C) 1.5 cm D) 4 cm

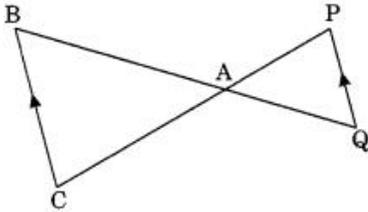
- 10) In the figure, If $DE \parallel AC$ then the correct relation among the following is (Average)



A) $x = \frac{a+b}{ay}$ B) $y = \frac{ax}{a+b}$ C) $x = \frac{ay}{a+b}$ D) $\frac{x}{y} = \frac{a}{b}$

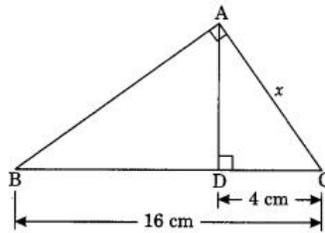
- 11) $\triangle ABC \sim \triangle DEF$. If $AB = 4$ cm, $BC = 3.5$ cm, $CA = 2.5$ cm and $DF = 7.5$ cm then, Perimeter of $\triangle DEF$ is
 A) 10 cm B) 14 cm C) 30 cm D) 25 cm (Average)

- 12) In the figure, $\triangle ACB \sim \triangle APQ$. $AB = 6$ cm, $BC = 8$ cm and $PQ = 4$ cm then length of AQ is
 (Easy)



- A) 2 cm B) 2.5 cm C) 3 cm D) 3.5 cm

- 13) In the figure, the value of x is
 (Average)

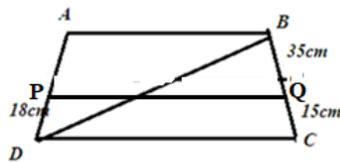


- A) 4 cm B) 5 cm C) 8 cm D) 3 cm

- 14) In $\triangle LMN$, $\angle L = 50^\circ$ and $\angle N = 60^\circ$ If $\triangle LMN \sim \triangle PQR$ then measure of $\angle Q$ is
 (Easy)
 A) 50° B) 70° C) 60° D) 40°

- 15) D and E are midpoints of sides AB and AC of $\triangle ABC$. If $BC = 6$ cm and $DE \parallel BC$ then, length of DE is
 (Easy)
 A) 12 cm B) 3 cm C) 5 cm D) 6 cm

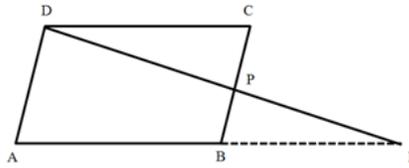
- 16) In trapezium $ABCD$, $AB \parallel DC$ and P, Q are points on sides AD and BC respectively. If $PQ \parallel DC$, $PD = 18$ cm, $BQ = 35$ cm and $QC = 15$ cm then length of AD is
 (Difficult)



- A) 5 cm B) 57 cm C) 60 cm D) 62 cm

- 17) ABCD is a parallelogram. If P is a point on BC and AB is produced to meet DP at L, then the correct relation among these is

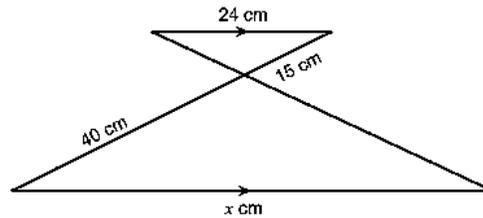
(Difficult)



- (A) $\frac{DP}{BL} = \frac{DC}{PL}$ (B) $\frac{DP}{PL} = \frac{DC}{BL}$ (C) $\frac{DP}{PL} = \frac{BL}{DC}$ (D) $\frac{DP}{PL} = \frac{AB}{DC}$

- 18) In the figure, value of x is

(Average)



- (A) 64 cm (B) 60cm (C) 25cm (D) 53cm

- 19) If a flag pole of height 5m casts a shadow of length 4m then the height of the tree that casts a shadow of 20m at the same time is,

(Difficult)

- (A) 25m (B) 30m (C) 60m (D) 20m

- 20) If in $\triangle ABC$ and $\triangle DEF$, $\angle B = \angle E$, $\angle C = \angle F$ and $AB = 3DE$, then the triangles are, (Easy)

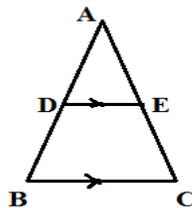
A) congruent but not similar B) similar but not congruent

C) neither congruent nor similar D) congruent and similar

- 21) If in $\triangle ADE$ and $\triangle ABC$, $\angle D = \angle B$ and $\angle E = \angle C$ then which of the following is incorrect? (Easy)

- A) $\frac{AD}{DB} = \frac{AE}{CE}$ B) $\frac{AD}{AB} = \frac{AE}{AC}$ C) $\frac{DE}{BC} = \frac{AD}{AB}$ D) $\frac{AE}{AC} = \frac{DE}{BC}$

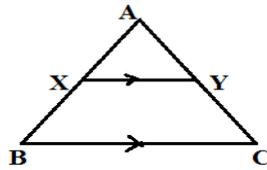
- 22) In the figure, D and E are midpoints of AB and AC respectively. If $DE = 4\text{cm}$ then BC is equal to (Easy)



- A) 4cm B) 6cm C) 8cm D) 12cm

23) In the figure, if $XY \parallel BC$ then $\frac{AX}{AB}$ is equal to

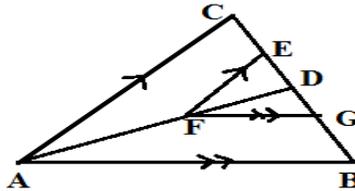
(July:2021) (Easy)



- A) $\frac{AX}{AY}$ B) $\frac{AX}{XB}$ C) $\frac{AY}{AC}$ D) $\frac{AC}{AY}$

24) In the figure, if $EF \parallel CA$ and $FG \parallel AB$ then $\frac{DE}{EC}$ is equal to

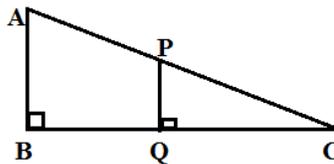
(Difficult)



- A) $\frac{DG}{GB}$ B) $\frac{GB}{DG}$ C) $\frac{AF}{DF}$ D) $\frac{AB}{AD}$

25) In the figure $AB \parallel PQ$. If $PQ = 1.5\text{cm}$, $QC = 2\text{cm}$ and $BQ = 8\text{cm}$ then length of AB is,

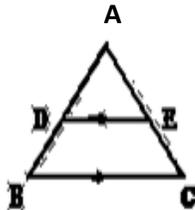
(Average)



- A) 10cm B) 7.5cm C) 9.5cm D) 3.5cm

26) In the figure $DE \parallel BC$ and if $AD = x$, $BD = y$, $AE = m$ and $CE = n$, then the correct relation among the following is

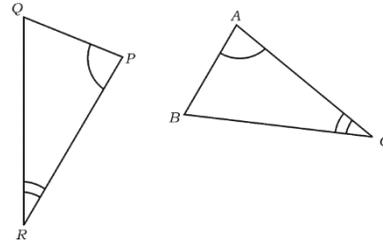
(Easy)



- A) $\frac{x}{y} = \frac{m}{m+n}$ B) $\frac{x}{y} = \frac{n}{m}$ C) $\frac{x+y}{y} = \frac{m}{m+n}$ D) $\frac{x}{x+y} = \frac{m}{m+n}$

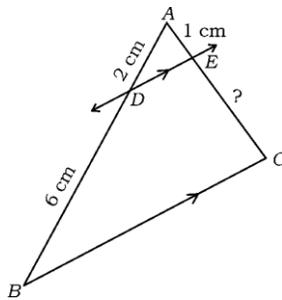
27) In the figure, If $\Delta PQR \sim \Delta ABC$ then the pair of corresponding sides among these is

(Average) (MQP-1 2024-25)



- A) PQ and AB B) PR and AB
 C) QR and AC D) PR and BC

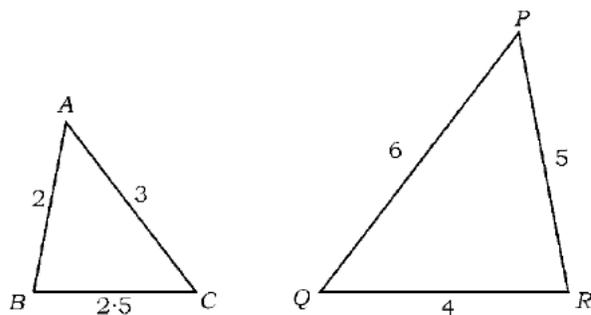
28) In the figure, $DE \parallel BC$. If $AD = 2$ cm, $AE = 1$ cm and $BD = 6$ cm then the length of EC is
 (May 2025 Easy)



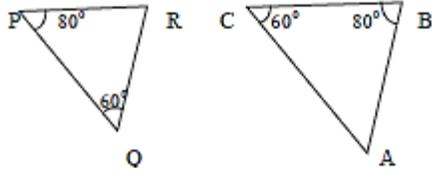
- A) 2 cm B) 3 cm C) 4 cm D) 5 cm

II. Answer the following questions (1 mark)

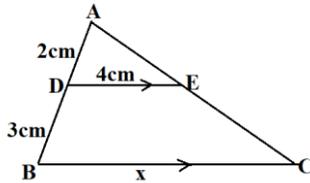
- 29) What are similar figures? (Easy)
 30) Write two conditions for similarity of polygons. (Easy)
 31) State Basic proportionality theorem (Thales theorem) (June/may:2022 - Easy)
 32) State AAA criterion for similarity of triangles. (Easy)
 33) In the given figure, write the similarity criterion used to show that $\Delta ABC \sim \Delta QRP$.
 (March 2025) (Easy)



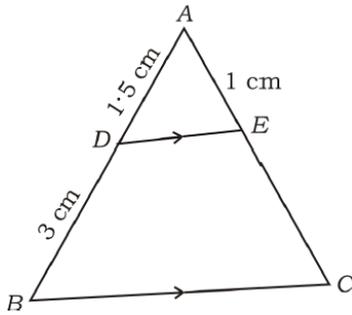
- 34) In the given figure, write the side of ΔPQR corresponding to the side AB of ΔABC .
June-2023 (Average)



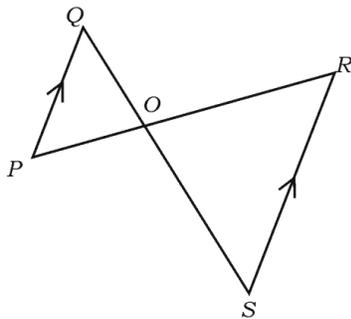
- 35) In the given figure, find the value of x . (Average)



- 36) In triangle ABC, if $DE \parallel BC$, $AD = 1.5$ cm, $BD = 3$ cm and $AE = 1$ cm then, find the length of EC. (Average)

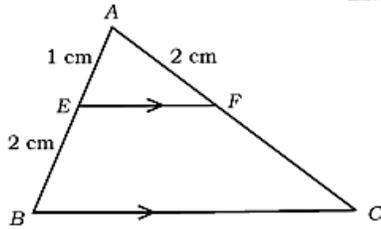


- 37) In the figure $\Delta POQ \sim \Delta ROS$ and $PQ \parallel SR$. If $PQ:SR = 1:2$ then, find $OS:OQ$
(MQP-1 2024-25) (Average)



38) In the given figure, find the length of FC

(Easy)



III. Answer the following questions (2 marks)

39) In the parallelogram ABCD, E is midpoint of AD and BE cuts CD at F.

Prove that $\Delta ABE \sim \Delta CFB$

(Average)

40) In ΔABC , $DE \parallel BC$. If $AD=2.4\text{cm}$, $AB=3\text{ cm}$, $AC=5\text{cm}$ then find AE

(Average)

41) A vertical pole of length 6 m casts a shadow 4 m long on the ground and at the same time a tower casts a shadow 28 m long. Find the height of the tower.

(Average)

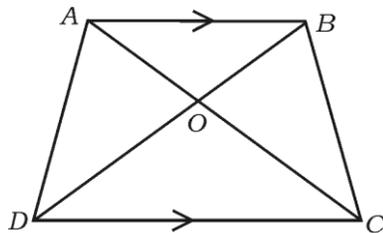
42) Two line segments AB and CD intersect each other at a point 'O'. Join AC and BD such that $AC \parallel BD$ and prove that $\Delta AOC \sim \Delta BOD$.

(March 2025 Average)

43) In the trapezium ABCD, $AB \parallel DC$. Diagonals AC and BD intersect each other at O.

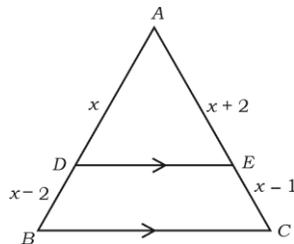
show that $\frac{AO}{BO} = \frac{CO}{DO}$

(Difficult)



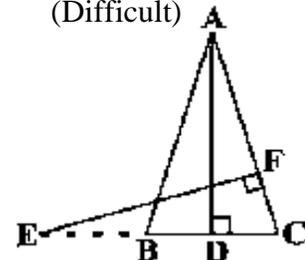
44) In triangle ABC, $DE \parallel BC$. If $AD = x$, $BD = x - 2$, $AE = x + 2$ and $EC = x - 1$ then find x and hence find $AD : DB$.

(Difficult)



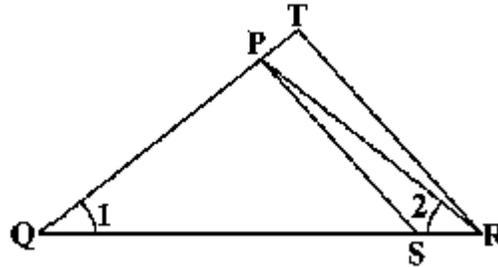
45) In the figure, E is a point on side CB produced of an isosceles triangle ABC with $AB = AC$. If $AD \perp BC$ and $EF \perp AC$, prove that $\Delta ABD \sim \Delta ECF$.

(Difficult)



46) In the figure, $\frac{QR}{QS} = \frac{QT}{PR}$ and $\angle 1 = \angle 2$. Show that $\Delta PQS \sim \Delta TQR$.

(Average)



IV. Answer the following questions (3 mark)

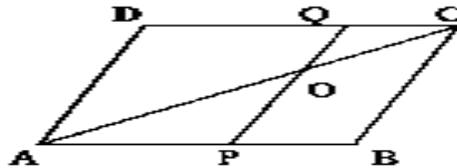
47) D is a point on the side BC of a triangle ABC such that $\angle ADC = \angle BAC$.

Show that $AC^2 = BC \cdot CD$

(Average)

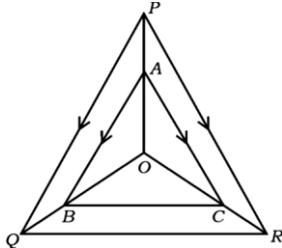
48) In the figure, ABCD is a parallelogram. If P divides AB in the ratio 2:3 and Q divides DC in the ratio 4:1 then prove that $OA = 2 \times OC$

(Average)



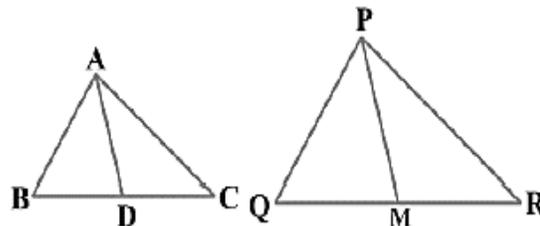
49) In the figure, A, B and C are points on OP, OQ and OR respectively such that $AB \parallel PQ$ and $AC \parallel PR$. Show that $BC \parallel QR$.

(MQP 2–2024 -25) [Easy]



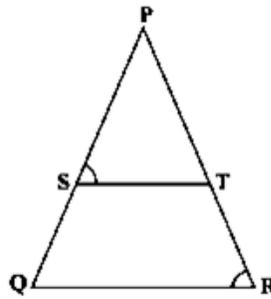
50) Sides AB and BC and median AD of a triangle ABC are respectively proportional to sides PQ and QR and median PM of ΔPQR . Show that $\Delta ABC \sim \Delta PQR$

(Average)



51) In the figure, $\frac{PS}{SQ} = \frac{PT}{TR}$ and $\angle PST = \angle PRQ$. Prove that PQR is an isosceles triangle.

(Easy)



V. Answer the following Questions (4 marks)

52) State and prove Basic Proportionality theorem.

(March 2018 / 2017April 2023/2025) (Average)

53) Prove that “If in two triangles, corresponding angles are equal, then their corresponding sides are in the same ratio (or proportion) and hence the two triangles are similar.”

(March 2022 /March 2019/April 2023/March 2025) (Average)

54) Prove that “If in two triangles, sides of one triangle are proportional to (i.e., in the same ratio of) the sides of the other triangle, then their corresponding angles are equal and hence the two triangles are similar.”

(MQP 2025 – 03 Average)

55) Prove that “If one angle of a triangle is equal to one angle of the other triangle and the sides including these angles are proportional, then the two triangles are similar.”

(MQP 2025 – 02 Average)

UNIT 7: COORDINATE GEOMETRY

Learning Points Points:

- ❖ Cartesian system
- ❖ The distance between two points: Distance formula
- ❖ Section Formula
- ❖ Mid-point Formula

Number of questions	Easy	Average	Difficult
58	27	21	10

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. The coordinates of the point lying on x – axis are, [Easy]

- A) (x , 0) B) (y , 0) C) (0 , x) D) (0 , y)

2. The coordinates of the point lying on y – axis are, [Easy]

- A) (x , 0) B) (y , 0) C) (0 , x) D) (0 , y)

3. The perpendicular distance of the point A(2, 5) from y – axis is, [Easy]

- A) 2 units B) 5 units
C) 7 units D) 3 units

4. The distance of the point (3, -4) from the x – axis is, [Easy]

- A) 3 units B) 5 units
C) 4 units D) -4 units

5. The coordinates of origin are, [MQP 2018/2019:Easy]

- A) (1, 1) B) (2, 2)
C) (0, 0) D) (3, 3)

6. The distance of the point P(a, b) from the origin (0,0) is, [April 2018, July 2022:Easy]

- A) $a^2 + b^2$ B) $\sqrt{a^2 - b^2}$ C) $\sqrt{a + b}$ D) $\sqrt{a^2 + b^2}$

7. The distance of the point P(x, y) from the origin is,
[June 2019, March 2025, May 2025: Easy]

- A) $x^2 + y^2$ B) $\sqrt{x^2 - y^2}$ C) $\sqrt{x + y}$ D) $\sqrt{x^2 + y^2}$

8. The distance between the points A (5, k) and (1, 0) is 5 units. The value of 'k' is,

- A) ± 3 B) - 3 C) - 2 D) ± 4 [Average]

9. The coordinates of the midpoint of the line segment joining the points (2, 3) and (4, 7) are,
[JUNE-2018 : Easy]

- A) (-3, 5) B) (1, 2) C) (3, 5) D) (6, 10)

10. The coordinates of the midpoint of the line segment joining the points (-4, 2) and (-2, 6) are,
[MQP-3, 2025: Easy]

- A) (3, 2) B) (-3, 4) C) (-2, 3) D) (-4, 1)

11. If the coordinates of the midpoint of the line segment joining that points A(-5, 9) and (8, 9) are $P(\frac{x}{2}, 4)$ then the value of 'x' is,
[Average]

- A) 13 B) 3 C) - 2 D) - 3

12. The distance between the points A (x_1, y_1) and B (x_2, y_2) is,
[MODEL PAPER-4:2025: Easy]

- A) $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ B) $\sqrt{(x_2 + x_1)^2 - (y_2 + y_1)^2}$
C) $\sqrt{(x_1 + x_2) + (y_2 + y_1)}$ D) $\sqrt{x^2 + y^2}$

13. The distance of the point (-3, 4) from the origin is, [Easy]

- A) 7 B) 1 C) 5 D) -5

14. In the following, a point on the x – axis is, [Easy]

- A) (-2, 0) B) (0, 2) C) (3, 3) D) (0, -2)

II. Answer the following questions. (1 Mark)

15. Find the distance between the points (0,0) and (-3, 5).
[Easy]

16. Find the distance of the point (6, 8) from the origin.
[Model paper-1:2025: Easy]

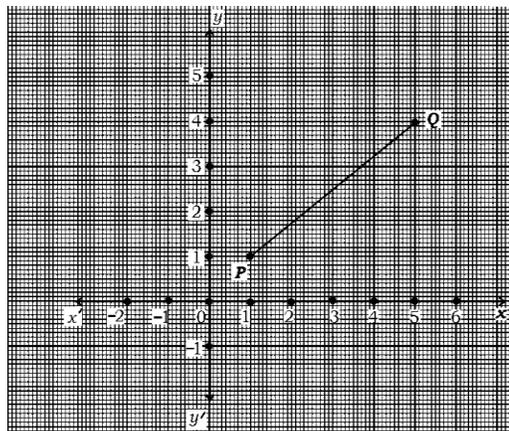
17. Write the coordinates of the midpoint of the line segment joining the points A (x_1, y_1) and B (x_2, y_2) .
[April-2020, MQP -2 : 2024/25 : Easy]

18. Find the coordinates of the midpoint of the line segment joining the points A(5, 4) and B(1, 4)
[MODEL PAPER-4: 2025: Easy]

19. Find the coordinates of the midpoint of the line segment joining the points (2, 3) and (4, 3)
(Oct-2024:Easy)
20. Find the coordinates of the midpoint of the line segment joining the points P(3, 4) and Q(5, 6) using midpoint formula.
[April 2022:Easy]
21. If the midpoint of the line segment joining the points (6, 3) and (4, y) are (5, 5), then find the value of 'y'.
[Average]
22. Write the coordinates of the point P which divides the line segment joining the points A(x_1, y_1) and B(x_2, y_2) internally in the ratio $m_1:m_2$
[Easy]
23. Write the coordinates of the point P which divides the line segment joining the points A(x_1, y_1) and B(x_2, y_2) internally in the ratio 1:1.
[Easy]

III. Answer the following questions. (2 Marks)

24. Find the distance between the points P (2, 3) and Q (4, 1) using distance formula.
[June 2019, July2022, Easy]
25. Find the distance between the points P (2, 4) and Q (8, 12) using distance formula.
[June-2018 : Easy]
26. Find the distance between the points P (5, 6) and Q (1, 3) using distance formula. [MQP-2025:Easy]
27. Find the distance between the points (-5, 7) and (-1, 3) using distance formula.
[APRIL -2020, OCT-2024 : Easy]
28. Find the distance between the points A (2, 6) and B(5, 10) using distance formula.
[April-2022:Easy]
29. Find the distance between the points A(5, -7) and B(1, -3).
[Easy]
30. If the distance between the points P(2, -3) and Q(10, y) is 10 units, then find the value of 'y'.
[Average]
31. If the distance between the points (3, 1) and (0, x) is 5 units, then find the value of 'x'.
[MQP-2025:Average]
32. Find the coordinates of the point P and Q from the given graph and find the length of PQ using distance formula.
[APRIL-2024 : Easy]



33. Find the ratio in which the point $(-4, 6)$ divides the line segment joining the points $(-6, 10)$ and $(3, -8)$ internally.

[JULY-2022 : Average]

34. Find the coordinates of the point which divides the line segment joining the points $(4, -3)$ and $(8, 5)$ internally in the ratio $3 : 1$.

[MARCH-2019, APRIL- 1 : 2024, JUNE- 2 : 2024 Average]

35. Find the coordinates of the point which divides the line segment joining the points $(-1, 7)$ and $(4, -3)$ internally in the ratio $2 : 3$.

[MARCH – 2023, MARCH -1 : 2025 : AUGUST-3 : 2024, Average]

36. Find the coordinates of the point which divides the line segment joining the points $(1, 6)$ and $(4, 3)$ in the ratio $1 : 2$ internally.

[APRIL -2020, MODEL PAPER-3:2025, Average]

37. Find the coordinates of the point which divides the line segment joining the points $(1, -3)$ and $(8, 5)$ internally in the ratio $3 : 1$.

[MODEL PAPER:2025, Average]

38. Find the coordinates of a point A, where AB is the diameter of a circle whose centre is $(2, -3)$ and B is $(1, 4)$.

[Average]

39. A $(2, 4)$ and B $(2, 8)$ are the end points of the diameter AB of a circle. Find the coordinates of the centre of the circle.

[May 2025: Average]

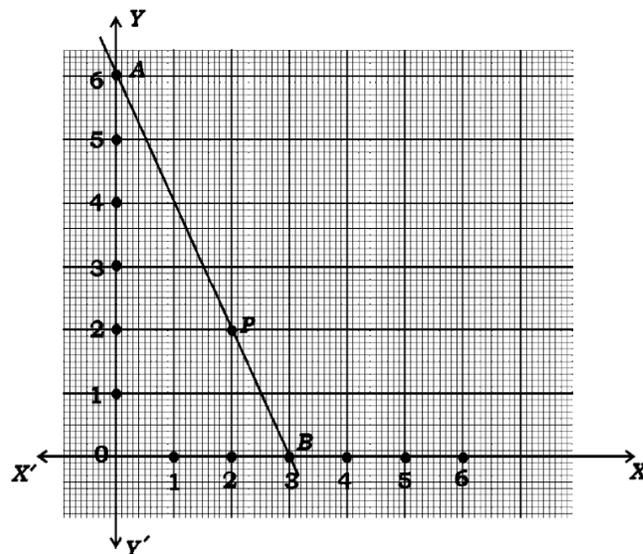
40. A circle with centre $(-5, 4)$ is passing through a point $(-7, 1)$. Find the radius of the circle.

[Model paper-2025: Average]

IV. Answer the following questions. (3 Marks)

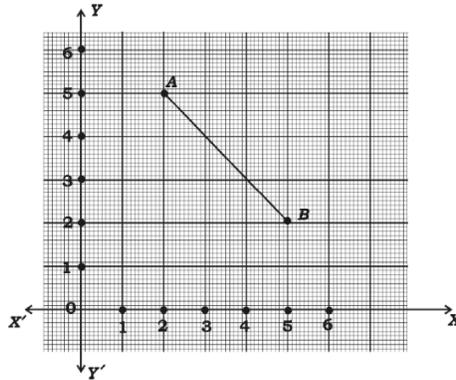
41. Find the ratio in which the point 'P' divides the line segment 'AB' in the given graph using formula.

[Model Paper-2025:Average]



42. In the figure, find the coordinates of the point which divides the line segment 'AB' internally in the ratio 1:2 using section formula.

[Model Paper-2025:Average]



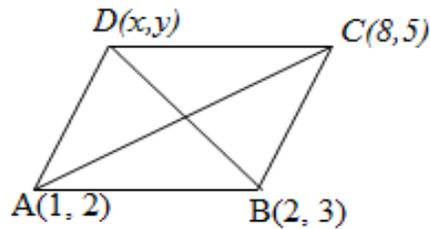
43. Prove that the points A (1, 5) , B(2, 4) and C(9, -3) are collinear using distance formula.
[Average]
44. Verify whether the points A (7, -2), B(5, 1) and C(3, 4) are collinear using distance formula.
[Average]
45. Verify whether the points (5, -2) (6, 4) and (7, -2) are the vertices of an isosceles triangle.
[Average]
46. The vertices of a triangle are A(8, -4), B(9, 5) and C(0, 4). Show that it is an isosceles triangle.
[September-2020:Average]
47. The midpoint of a line segment joining the points A(x, 0) and B(0, y) is (4, 3). Find the length of AB.
(March-2023:Difficult)
48. Find the coordinates of the point of trisection of the line segment joining the points (4, -1) and (-2, -3).
(Difficult)
49. Find the coordinates of the point of trisection of the line segment joining the points (2, -2) and (-7, 4).
(Model Paper-2025:Difficult)
50. Find the ratio in which the line segment joining A(1, - 5) and B(- 4, 5) is divided by the x-axis. Also find the coordinates of the point of division.
[Average]
51. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (- 3, 4).
[Difficult]

52. The point $P(x, y)$ is equidistant from the points $A(7, 1)$ and $B(3, 5)$. Find the relationship between x and y . If the points A, P and B are collinear, then find the coordinates of the point ' P '.

[Model Paper-2025:Difficult]

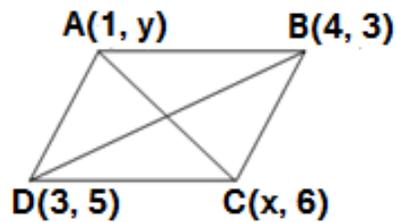
53. The coordinates of the three vertices of a parallelogram are $A(1, 2)$, $B(2, 3)$ and $C(8, 5)$. Find the coordinates of the 4th vertex.

[Difficult]



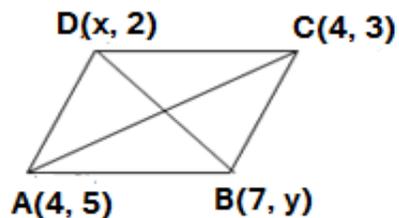
54. If $A(1, y)$, $B(4, 3)$, $C(x, 6)$ and $D(3, 5)$ are the consecutive vertices of a parallelogram, then find the value of ' x ' and ' y '.

[March 2025:Difficult]



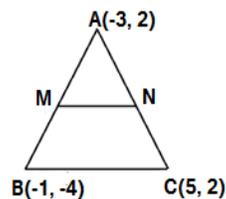
55. If $A(4, 5)$, $B(7, y)$, $C(4, 3)$ and $D(x, 2)$ are the vertices of a parallelogram, then find the values of x and y .

[Model Paper-2025:Difficult]



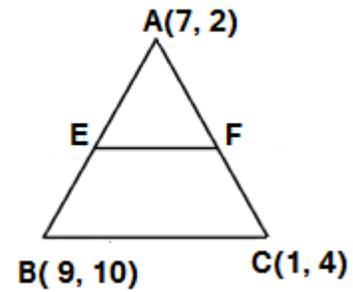
56. The vertices of a triangle ABC are $A(-3, 2)$, $B(-1, -4)$ and $C(5, 2)$ and M and N are the midpoints of AB and AC respectively. Prove that $2MN = BC$

[April-2019:Difficult]



57. The vertices of a triangle ABC are A(7, 2), B(9, 10) and C(1, 4) and E and F are the midpoints of AB and AC respectively. Prove that $EF = \frac{1}{2} BC$

[Difficult]



58. Prove that the points (1, 7), (4, 2), (-1, -1) and (-4, 4) are the vertices of a square.

[Average]

UNIT 8 : INTRODUCTION TO TRIGONOMETRY

Learning Points:

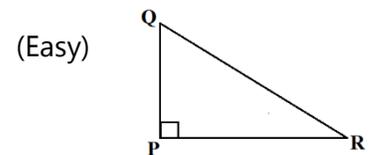
- ❖ Trigonometric ratios
- ❖ Trigonometric ratios for standard angles
- ❖ Trigonometric identities and problems

Number of questions	Easy	Average	Difficult
100	13	56	31

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

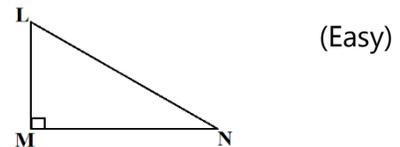
1. In the figure, $\cos R$ is equal to

- A) $\frac{PQ}{PR}$ B) $\frac{PR}{QR}$ C) $\frac{PR}{PQ}$ D) $\frac{PQ}{QR}$



2. In the figure, $\frac{LN}{MN} =$

- A) $\cos L$ B) $\cot L$ C) $\operatorname{cosec} L$ D) $\sec L$



3. In the figure, the value of $\sin C$ is,

- A) $\frac{2}{\sqrt{3}}$ B) $\frac{\sqrt{3}}{2}$ C) $\frac{1}{2}$ D) 1



4. If $\sin \theta = \frac{5}{13}$, then the value of $\operatorname{cosec} \theta$ is,

- A) $\frac{13}{5}$ B) $\frac{5}{12}$ C) $\frac{13}{12}$ D) $\frac{12}{13}$

[Easy]

5. If $\angle A = 30^\circ$, then the value of $\sin^2 A$ is,

- A) 0 B) $\frac{1}{4}$ C) $\frac{1}{2}$ D) $\frac{1}{\sqrt{2}}$

[Average]

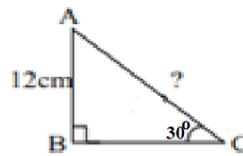
6. The value of $\sin 30^\circ + \cos 60^\circ$ is, [MQP- 2020: Easy]
 A) $\frac{1}{2}$ B) $\frac{3}{2}$ C) $\frac{1}{4}$ D) 1
7. If $\sin A = \frac{1}{\sqrt{2}}$, then the value of $\angle A$, [MQP- 2020: Average]
 A) 90° B) 60° C) 30° D) 45°
8. If $\operatorname{cosec} \theta = \frac{5}{3}$, then the value of $\sin \theta$ is, [Easy]
 A) $\frac{5}{3}$ B) $\frac{3}{5}$ C) $\frac{3}{4}$ D) $\frac{5}{4}$
9. If $13 \cos \theta = 12$, then the value of $\sec \theta$ is, [Average]
 A) $\frac{12}{5}$ B) $\frac{13}{5}$ C) $\frac{12}{13}$ D) $\frac{13}{12}$
10. The value of $\sec^2 26^\circ - \tan^2 26^\circ$ is, [Average]
 A) $\frac{1}{2}$ B) 0 C) 2 D) 1
11. The value of $\sin 45^\circ \times \cos 45^\circ$ is, [Average]
 A) $\frac{1}{\sqrt{2}}$ B) $\frac{\sqrt{3}}{2}$ C) $\frac{1}{4}$ D) $\frac{1}{2}$
12. The value of $\tan 45^\circ \times \cot 45^\circ$ is, [Average]
 A) $\sqrt{3}$ B) 2 C) 1 D) $\frac{1}{\sqrt{3}}$
13. If $2 \sin 2\theta = \sqrt{3}$, then the value of ' θ ' is, [MQP 1 -2021: Average]
 A) 90° B) 60° C) 30° D) 45°
14. If $\sin \theta = \frac{x}{y}$, then the value of $\cos \theta$ is, [MQP 1- 2021: Difficult]
 A) $\frac{y}{\sqrt{y^2-x^2}}$ B) $\frac{y}{x}$ C) $\frac{x}{\sqrt{y^2-x^2}}$ D) $\frac{\sqrt{y^2-x^2}}{y}$
15. If $\sin A + \sin^2 A = 1$, then the value of $\cos^2 A + \cos^4 A$ is, [MQP 1- 2021: Difficult]
 A) $\frac{1}{2}$ B) 2 C) 3 D) 1
16. If $\sin \theta = \frac{3}{5}$, then the value of $(1 - \cos^2 \theta)$ is, [MQP-2 2021: Average]
 A) $\frac{9}{25}$ B) $\frac{6}{10}$ C) $\frac{9}{5}$ D) $\frac{25}{9}$

17. The correct relation among the following is, [July 2021: Average]
 A) $\tan^2\theta = \sec^2\theta + 1$ B) $\sin\theta = \frac{1}{\sec\theta}$
 C) $\cot\theta = \frac{\sin\theta}{\cos\theta}$ D) $\sin^2\theta + \cos^2\theta = 1$
18. The value of $(\sin 30^\circ + \cos 60^\circ - \tan 45^\circ)$ is, [July 2021: Average]
 A) 0 B) -1 C) 2 D) 1
19. $(3 + \sec^2 A)$ is equal to, [July- 2021: Average]
 A) $4 + \tan^2 A$ B) $4 + \cot^2 A$ C) $2 + \cot^2 A$ D) $3 + \cot^2 A$
20. The value of $(\sin A \times \operatorname{cosec} A)$ is, [July- 2021: Average]
 A) 2 B) 1 C) $-\frac{1}{2}$ D) $\frac{\sqrt{3}}{2}$
21. $(1 + \tan^2\theta)$ is equal to, [June- 2022: Average]
 A) $\operatorname{cosec}^2\theta$ B) $\cos^2\theta$ C) $\sec^2\theta$ D) $\cot^2\theta$
22. $(\sec^2\theta - 1)(1 - \operatorname{cosec}^2\theta)$ is equal to, [Difficult]
 A) -1 B) $\cot\theta$ C) 0 D) $\operatorname{cosec}\theta$
23. $\cot^2\theta - \frac{1}{\sin^2\theta}$ is equal to, [Average]
 A) -1 B) 1 C) $\sin^2\theta$ D) $\cos^2\theta$
24. If $(\sec A - \tan A) = k$, then $(\sec A + \tan A)$ is equal to, [Average]
 A) $1 - \frac{1}{k}$ B) $1 - k$ C) $1 + k$ D) $\frac{1}{k}$
25. If $8 \tan P = 15$, then $\sin P - \cos P$ is equal to, [Average]
 A) $\frac{8}{17}$ B) $\frac{17}{8}$ C) $\frac{1}{17}$ D) $\frac{7}{17}$
26. If $\tan^2\theta = \frac{8}{7}$ where θ is an acute angle, then the value of $\frac{(1+\sin\theta)(1-\sin\theta)}{(1+\cos\theta)(1-\cos\theta)}$ is, [Difficult]
 A) $\frac{8}{7}$ B) $\frac{7}{8}$ C) $\frac{7}{4}$ D) $\frac{64}{49}$

II. Answer the following questions. (1 Mark)

27. In ΔABC , if $\angle ABC = 90^\circ$ and $\angle ACB = 30^\circ$, then find $AB:AC$. [June 2019: Difficult]
28. If $\sin\theta = \frac{3}{5}$ and $\cos\theta = \frac{4}{5}$, then find the value of $\sin^2\theta + \cos^2\theta$ [MQP 1 2020: Average]
29. Find the value of $\operatorname{cosec} 60^\circ + \sec 30^\circ$. [Easy]
30. Find the value of $\sin 90^\circ + \tan 45^\circ$ [MQP 2 2020: Average]

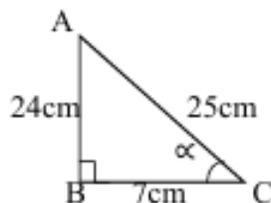
31. In $\triangle ABC$, if $AB \perp BC$, $\angle ACB = 30^\circ$ and $AB = 15\text{m}$, then find the measure of BC .
[SLP 2020:Difficult]
32. Find the value of $\tan 45^\circ + \cot 45^\circ$.
[June 2020: Easy]
33. If $\cos \theta = \frac{24}{25}$, then find the value of $\sec \theta$.
[September 2020:Easy]
34. If $\sin^2 A = 0$, then find the value of $\cos A$.
[September 2020:Easy]
35. If $15 \cot A = 8$, then find the value of $\tan A$.
[Average]
36. In the figure, ABC is a right angled triangle. If $\angle C = 30^\circ$ and $AB = 12\text{cm}$ then find the measure of AC .
[June 2022:Average]



37. If $x \tan 45^\circ \cdot \sin 30^\circ = \cos 30^\circ \cdot \tan 30^\circ$, then find the value of x . [Average]
38. Find the value of $5 \tan^2 A - 5 \sec^2 A + 1$. [Difficult]
39. What is the value of $\sin A \cdot \operatorname{cosec} A$? [Average]
40. What is the value of $\tan A \cdot \cot A - \cos A \cdot \sec A$? [Difficult]
41. Find the value of $\tan^2 45^\circ - \sin^2 30^\circ$. [Average]
42. If $\sin A = \cos A$, then what is the value of A ? [Average]

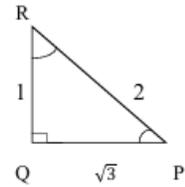
III. Answer the following questions. (2 Marks)

43. If $\sin \theta = \frac{12}{13}$ and $\cos \theta = \frac{5}{13}$, then find the value of $\sec \theta$ and $\tan \theta$ [Easy]
44. If $\operatorname{cosec} \theta = \frac{13}{12}$ and $\tan \theta = \frac{5}{12}$, then find the value of $\cos \theta$ [Average]
45. In the adjoining figure, find the value of $\sin \alpha$ and $\cos \alpha$. [Average]



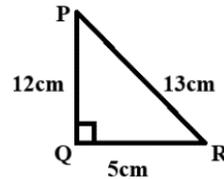
46. In the figure, find the value of $\sin P$ and $\tan R$.

[SLP 2023:Easy]



47. In the figure, find the value of $\tan P - \cot R$.

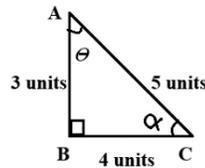
[Average]



48. In the figure, $\angle ABC = 90^\circ$. Write the values of the following.

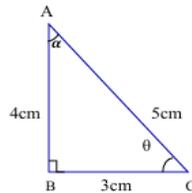
[March 2025:Easy]

- i) $\sin \alpha$
- ii) $\tan \theta$



49. In the figure, find the value of $\sin \alpha + \cos \theta$

[Average]



50. Evaluate : $2\tan^2 45^\circ + \cos^2 30^\circ - \sin^2 60^\circ$.

[MQP 2019: Average]

51. If $\sqrt{3} \tan \theta = 1$ and θ is an acute angle, find the value of $\sin 3\theta + \cos 2\theta$.

[April 2023:Average]

52. Show that $(\tan A \times \sin A) + \cos A = \sec A$.

[June 2019:Average]

53. If $\cos \theta = 0.6$, then show that $5 \sin \theta - 3 \tan \theta = 0$.

[MQP 2020: Difficult]

54. Prove that $(\sec^4 \theta - \sec^2 \theta) = \tan^2 \theta + \tan^4 \theta$.

[MQP 2020:Difficult]

55. Prove that $\operatorname{cosec} A (1 - \cos A) (\operatorname{cosec} A + \cot A) = 1$.

[September 2020: Difficult]

56. Prove that $\tan^2 \theta - \sin^2 \theta = \tan^2 \theta \cdot \sin^2 \theta$

[Difficult]

57. Prove that $\cot^2 \theta - \cos^2 \theta = \cot^2 \theta \cdot \cos^2 \theta$

[Difficult]

58. Prove that $\sin 30^\circ + \cos 60^\circ + \tan 45^\circ = \sec 60^\circ$. [Average]
59. Prove that $\frac{\sin 30^\circ + \cos 60^\circ}{\operatorname{cosec} 30^\circ - \cos 45^\circ} = \sin 90^\circ$. [April 2024:Average]
60. Find the value of $\frac{\cos 45^\circ \cdot \sin 45^\circ}{\sec 30^\circ - \cot 60^\circ}$ [Average]
61. Prove that $\frac{1+\cos A}{1-\cos A} = (\operatorname{cosec} A + \cot A)^2$ [April 2019:Average]
62. Prove that $\frac{1+\sin A}{1-\sin A} = (\sec A + \tan A)^2$ [Difficult]
63. Prove that $\frac{\cos A}{1+\sin A} + \frac{1+\sin A}{\cos A} = 2\sec A$ [April 2025:Average]
64. Prove that $\frac{\sin A}{1+\cos A} + \frac{1+\cos A}{\sin A} = 2\operatorname{cosec} A$ [Average]
65. Prove that $\frac{\cos A - \sin A \cdot \cos A}{\cos A + \sin A \cdot \cos A} = \frac{\operatorname{cosec} A - 1}{\operatorname{cosec} A + 1}$ [April 2024:Average]
66. Prove that $\sin 30^\circ \cdot \cos 60^\circ + \cos 30^\circ \cdot \sin 60^\circ = \sin 90^\circ$ [July 2024:Average]
67. If $\frac{\sqrt{3}\sec A}{\operatorname{Cosec} A} = 1$, then find the value of A. [July 2024:Average]
68. Prove that $\sec A (1 - \sin A) (\sec A + \tan A) = 1$ [Difficult]
69. If $2\sin\theta = 1$, then find the value of $\cos^2 60^\circ + \sec^2 30^\circ$ [Average]
70. Prove that $\tan^2\theta + \cot^2\theta = \sec^2\theta + \operatorname{cosec}^2\theta - 2$ [Difficult]
71. Evaluate: $4\sin 30^\circ + \cos 60^\circ \cdot \sec 60^\circ - 3\tan 45^\circ$. [Average]
72. Evaluate : $6\cos 60^\circ - \sin 30^\circ + \sin^2 45^\circ + \cos^2 45^\circ$. [Average]
73. Evaluate : $\frac{5\cos^2 60 + 4\sec^2 30 - \tan^2 45}{\sin 30^\circ + \cos 30^\circ}$ [March 2025:Average]
74. Prove that $\frac{\sec 60^\circ}{\cot 45^\circ} - \frac{2\sin 90^\circ}{\cos 0^\circ} + \frac{\tan 45^\circ}{\operatorname{cosec} 30^\circ} = \frac{1}{2}$ [Average]
75. If $\sin\theta = \frac{1}{3}$, then find the value of $(2\cot^2\theta + 2)$ [Average]
76. Find the value of $2\cos^2\theta + \frac{2}{1+\cot^2\theta}$ [Difficult]
77. Find the value of $\frac{5}{\cot^2\theta} - \frac{5}{\cos^2\theta}$ [Difficult]
78. If $\sec^2 A(1+\sin A)(1-\sin A) = k$, then find the value of 'k' [Average]

IV. Answer the following questions. (3 Marks)

79. Prove that $\frac{\sin A}{1-\cot A} + \frac{\cos A}{1-\tan A} = \sin A + \cos A$. [MQP 1 2021:Difficult]
80. Prove that $\frac{1+\cos A}{\sin A} - \frac{\sin A}{1+\cos A} = 2\cot A$. [SLP 2020: Average]
81. Prove that $\frac{1+\sin A}{\cos A} - \frac{\cos A}{1+\sin A} = 2\tan A$. [Average]

82. Prove that $\frac{\cos\theta - 2\cos^3\theta}{2\sin^3\theta - \sin\theta} = \cot\theta$. [MQP 1 2021:Difficult]
83. Prove that $\frac{\sin\theta - 2\sin^3\theta}{2\cos^3\theta - \cos\theta} = \tan\theta$. [Difficult]
84. Prove that $\frac{\sin A - \cos A}{\sin A + \cos A} + \frac{\sin A + \cos A}{\sin A - \cos A} = \frac{2}{2\sin^2 A - 1}$. [MQP 2 2021:Difficult]
85. If $x = p \tan\theta + q \sec\theta$ and $y = p \sec\theta + q \tan\theta$, then prove that $x^2 - y^2 = q^2 - p^2$. [June 2020:Difficult]
86. Prove that $(\sec\theta - \cos\theta)\{(\operatorname{cosec}\theta - \sin\theta)(\tan\theta + \cot\theta)\} = 1$. [MQP-2 2021:Difficult]
87. Prove that $\frac{\sec A + \tan A - 1}{\tan A - \sec A + 1} = \frac{1 + \sin A}{\cos A}$. [June 2024:Difficult]
88. Prove that $\frac{\sin\theta}{1 - \cos\theta} + \frac{\tan\theta}{1 + \cos\theta} = \cot\theta + \sec\theta \cdot \operatorname{cosec}\theta$. [Difficult]
89. Prove that $\frac{\tan A - \sin A}{\tan A + \sin A} = \frac{\sec A - 1}{\sec A + 1}$. [Difficult]
90. Prove that $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$. [MQP1 2024: Average]
91. Prove that $\sec\theta(1 - \sin\theta)(\sec\theta + \tan\theta) = 1$. [March 2022: Average]
92. Prove that $\operatorname{cosec} A(1 - \cos A)(\operatorname{cosec} A + \cot A) = 1$. [Average]
93. Prove that $(\operatorname{cosec} A - \sin A)(\sec A - \cos A) = \frac{1}{\tan A + \cot A}$ [Difficult]
94. Prove that $\sqrt{\frac{1 + \cos A}{1 - \cos A}} = \operatorname{cosec} A + \cot A$. [April 2023: Average]
95. Prove that $\sqrt{\frac{1 + \sin A}{1 - \sin A}} = \sec A + \tan A$. [Average]
96. Prove that $(\sec A - \cos A)(\cot A + \tan A) = \tan A \cdot \sec A$. [June 2023: Average]
97. Prove that $(\operatorname{cosec} A - \sin A)(\tan A + \cot A) = \cot A \cdot \operatorname{cosec} A$. [Average]
98. If $\tan\theta = \sqrt{3}$, then find the value of $\frac{4\sin\theta - \cos\theta - 1}{4\sin\theta + \cos\theta + 1}$. [Difficult]
99. Evaluate : $\frac{2\cos(90^\circ - 30^\circ) + \tan 45^\circ - \sqrt{3}\operatorname{cosec} 60^\circ}{\sqrt{3}\sec 30^\circ + 2\cos 60^\circ + \cot 45^\circ}$ [June 2022: Difficult]
100. Prove that $\frac{\cos^3\theta + \sin^3\theta}{\cos\theta + \sin\theta} + \frac{\cos^3\theta - \sin^3\theta}{\cos\theta - \sin\theta} = 2$. [Difficult]

UNIT 9: SOME APPLICATIONS OF TRIGONOMETRY

Learning Points:

- ❖ Angle of elevation
- ❖ Angle of depression
- ❖ Line of sight
- ❖ Application problems

Number of questions	Easy	Average	Difficult
36	11	19	6

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet (1mark)

1. The length of shadow of a tower on level ground is $\sqrt{3}$ times the height of the tower. The angle of elevation of sun is, (Easy)

- A) 45° B) 30° C) 60° D) 90°

2. If a tower of height 6m casts a shadow of length $2\sqrt{3}$ m on the ground, then the angle of elevation of the sun is, (Easy)

- A) 60° B) 45° C) 90° D) 30°

3. The ratio of the height of a tower and the length of its shadow on the ground is $\sqrt{3} : 1$. The angle of elevation of Sun is, (Easy)

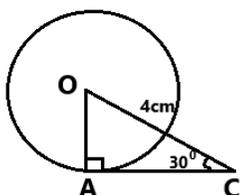
- A) 30° B) 45° C) 60° D) 75°

4. At some time of the day, if the length of the shadow of a tower is equal to its height then the angle of elevation of the sun is, (Easy)

- A) 30° B) 60° C) 90° D) 45°

5. In a circle with centre 'O' AC is a tangent at 'A'. If $OC=4\text{cm}$ and $\angle ACO=30^\circ$ then the radius of the circle is,

- A) $\sqrt{3}\text{ cm}$ B) $4\sqrt{3}\text{ cm}$ C) 2 cm D) 3 cm



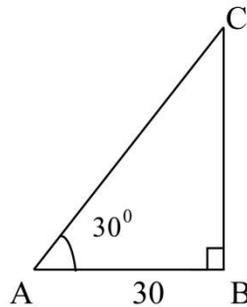
[MQP 2021 Difficult]

II. Answer the following questions (1 mark)

6. A person standing at a distance of 10m away from the foot of building observes its top at an angle of 45° . Find the height of the building. (Easy)
7. Name the angle formed by the line of sight with the horizontal when the line of sight is above the horizontal level. (Easy)
8. Name the angle formed by the line of sight with the horizontal when the line of sight is below the horizontal level. (Easy)
9. A ladder makes an angle of 60° with the ground, when placed against a wall. If foot of the ladder is 6m away from the wall, find the length of ladder. (Easy)
10. At certain time in a day, if the height and length of the shadow of a tree are equal, then find the angle of elevation of sun. (Easy)

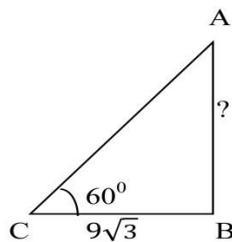
III. Answer the following questions (2 mark)

11. The angle of elevation of the top of a tower from a point on the ground which is 30m away from the foot of the tower is 30° . Find the height of the tower. (MQP 2019, Easy)

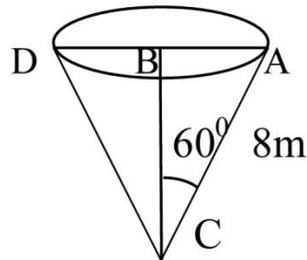


12. The angle of elevation of the top of a vertical tower on a level ground from a point at a distance of $9\sqrt{3}$ m from its foot on the same ground is 60° . Find the height of the tower.

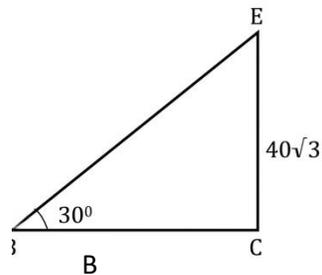
(MQP 2019 , Easy)



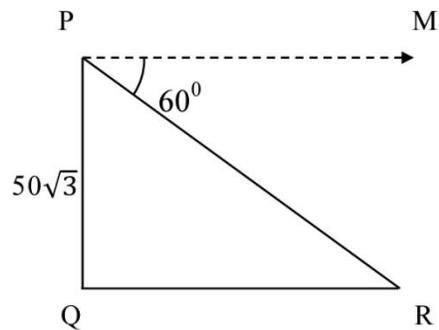
13. Find the diameter of the circular base of right circular cone whose slant height is 8cm and semi vertex angle is 60° . (MQP 2020 , Average)



14. A person standing on a ground observes the top of a windmill of height $40\sqrt{3}$ m at an angle of elevation 30° . Find the distance between the person and the foot of windmill. (Average)



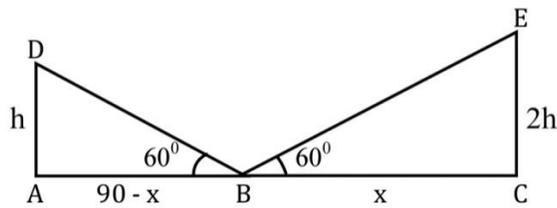
15. From the top of a building of height $50\sqrt{3}$ m a person observes an object on the ground at angle of depression 60° . Find the distance of the object from the building. (MQP 2020 , Average)



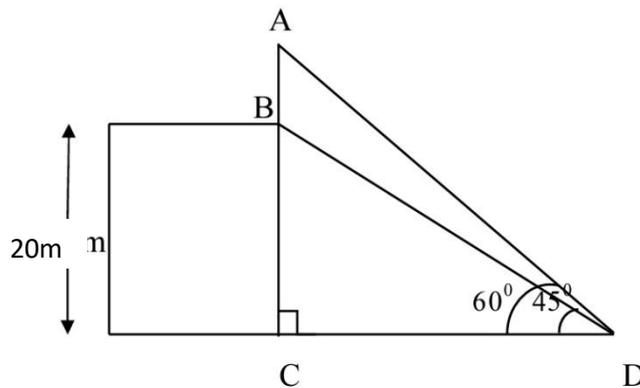
IV. Answer the following questions (3 mark)

16. Two windmills of height 50m and $40\sqrt{3}$ m are on either side of the field. A person observes the top of the windmills from a point in between them. The angle of elevation was found to be 45° and 30° . Find the distance between the windmills. (June 2019 , Average)

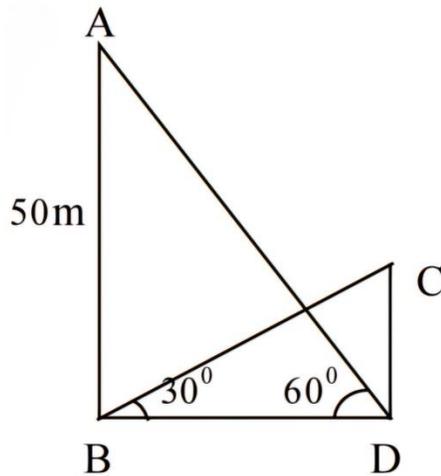
17. Two vertical poles are on either side of the road. The width of the road is 90 feet and heights of the pole are in the ratio 1:2. From a point between them on the road the angle of elevation to the top of the poles is 60° . Find the heights of the poles. (SLP 2020 , Average)



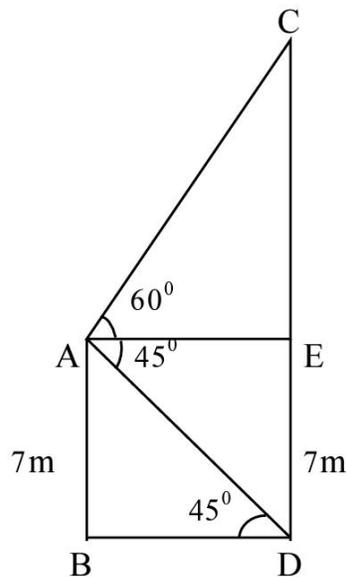
18 .From a point on the ground, the angles of elevation of the top and bottom of a transmission tower fixed at the top of a 20m high building are 60° and 45° respectively. Find the height of the transmission tower. (MQP-1 2021 , Average)



19. A tower and a building are standing vertically on the same level ground. The angle of elevation of the top of the building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60° . If the tower is 50m high, find the height of the building. (MQP 2022 , Average)

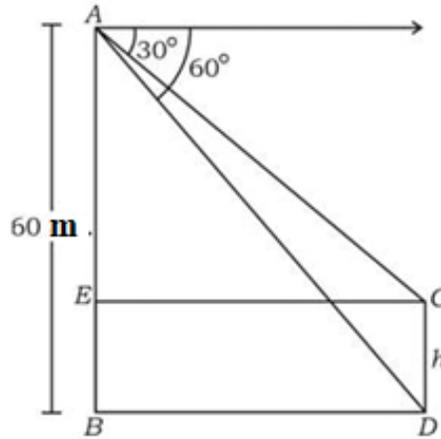


20. A cable tower and a building are standing vertically on the same level ground. From the top of the building which is 7m high, the angle of elevation of the cable tower is 60° and the angle of depression of its foot is 45° . Find the height of the tower. (June 2022 , Average)



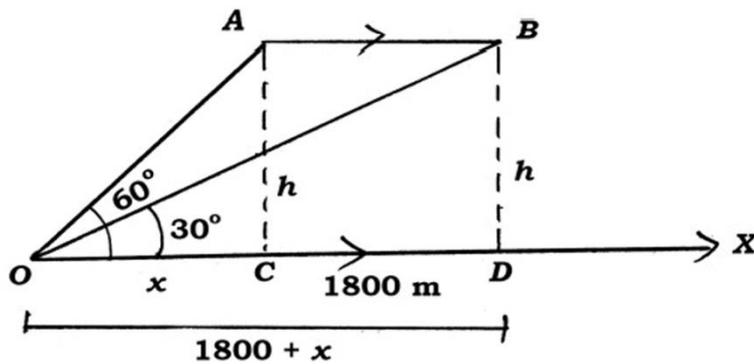
V. Answer the following questions (4 marks)

21. A tower and a pole stand vertically on the same level ground. It is observed that the angles of depression of the top and foot of the pole from the top of tower of height 60 m is 30° and 60° respectively. Find the height of the pole. (June 2020 , Average)



22. An aircraft flying parallel to the ground in the sky from the point A through the point B is observed, the angle of aircraft at A from a point on the level ground is 60° , after 10 seconds it is observed that the angle of elevation of aircraft at B is found to be 30° from the same point. Find at what height the aircraft is flying, if the velocity of aircraft is 648 km/hr.

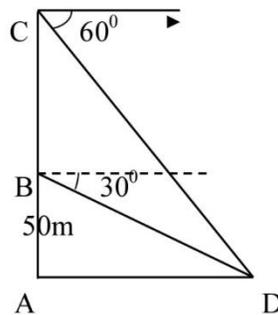
(Take $\sqrt{3} = 1.73$)



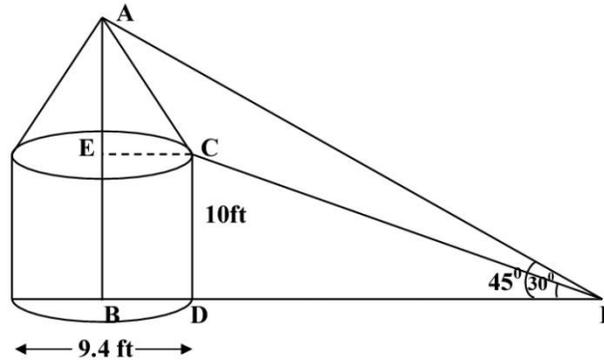
(September 2020 , Average)

23. The angle of depression from the top of a vertical tower to a point on the ground is found to be 60° and from a point 50m above the foot of the tower the angle of depression to the same point is found to be 30° as shown in the figure. Find the height of the tower.

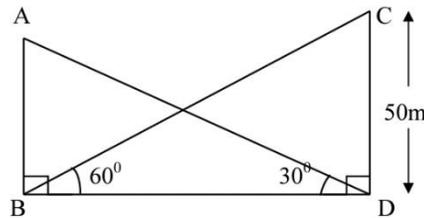
(MQP 2022 , Average)



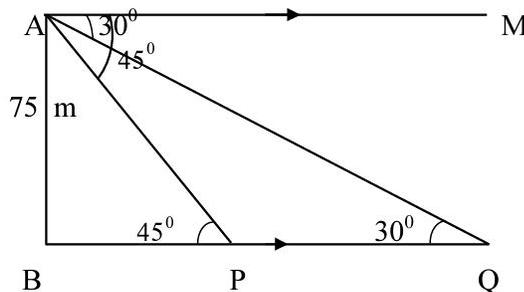
24. A building on the ground is in the form of a conical tomb surmounted by a cylinder of height 10 feet as shown in the figure. From a point P on the same ground the angle of elevation of the top edge of the cylinder is found to be 30° and the angle of elevation to the vertex of the cone is found to be 45° . If the diameter of the outer edge of circular base of the cylinder is 9.4 feet, find the height of the conical shaped tomb. (SLP 2022 , Average)



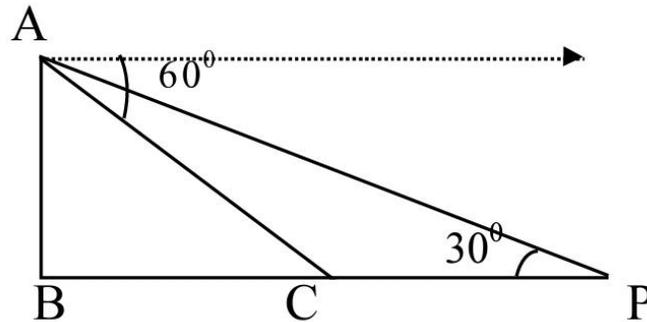
25. The angle of elevation of the top of a building from the foot of a tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60° . Both the tower and building are on the same level. If the height of the tower is 50m, then find the height of the building. (April 2022 , Average)



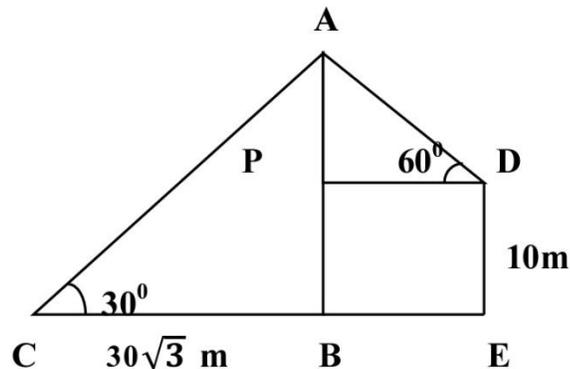
26. As observed from the top of a 75 m high light house from the sea level, the angles of depression of two ships are 30° and 45° . If one ship is exactly behind the other on the same side of the light house, then find the distance between the two ships. (MQP 2023 , April 2020- Average)



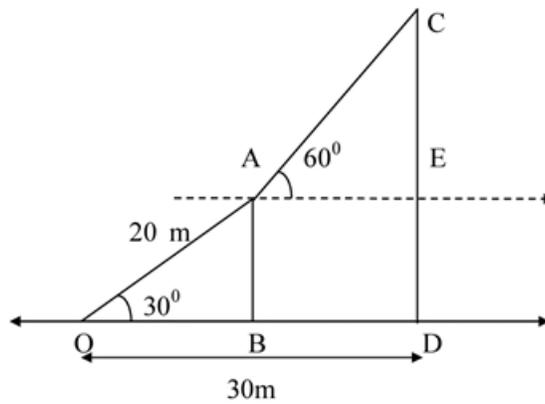
27. As observed from the top of a building standing vertically on the ground, the angle of depression of a point 'C' on the ground is 60° . From the foot (B) of the building when moved through point 'C' in a straight line and observe the top of the building, from point 'P', if the angle of elevation has to be 30° (as shown in the figure) then show that the distance moved from 'C' to 'P' is twice the distance BC. (MQP 2023 , Average)



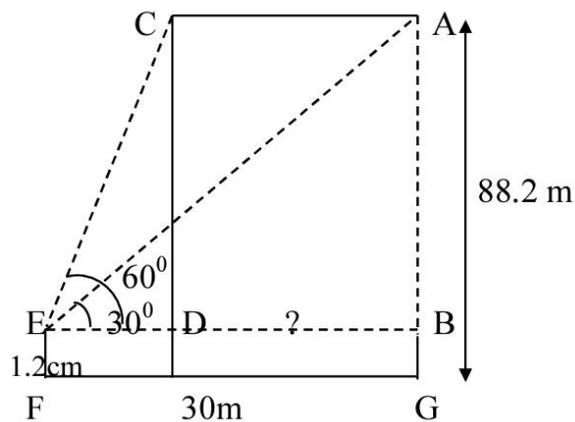
28. A tower and a building are standing vertically on a level ground. The angles of elevation of the top of the tower from a point on the same ground and from the building are found to be 30° and 60° respectively. If the distance of the point from the foot of the tower is $30\sqrt{3}$ m and height of the building is 10m, then find the distance between the foot of the tower and building and also the distance between their tops. (SLP 2023 , Average)



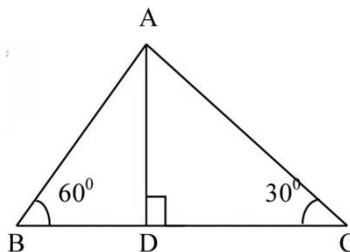
29. In the given figure, a rope is tightly stretched and tied from the top of a vertical pole to a peg on the same level ground such that the length of the rope is 20 m and the angle made by it with the ground is 30° . A circus artist climbs the rope, reaches the top of the pole and from there he observes that the angle of elevation of the top of another pole on the same ground is found to be 60° . If the distance of the foot of the longer pole from the peg is 30 m, then find the height of this pole. (Take $\sqrt{3} = 1.73$) (April 2023 , Difficult)



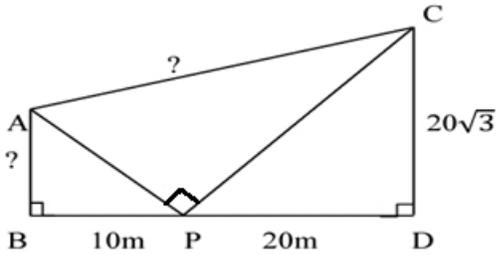
30. A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60° . After some time the angle of elevation reduces to 30° (see the figure). Find the distance travelled by the balloon during the interval. (June 2023 , Average)



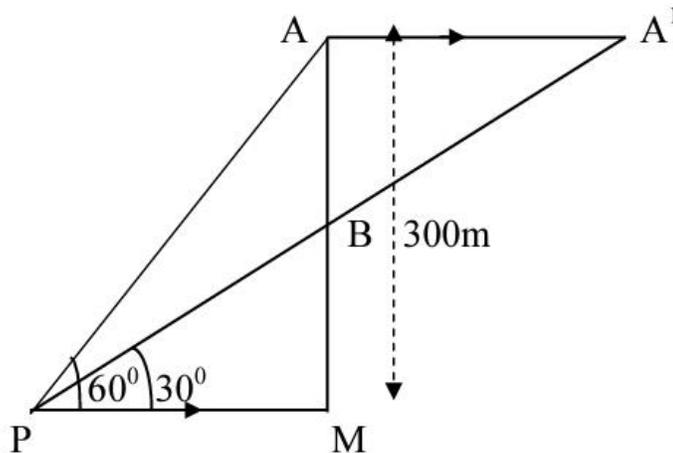
31. In $\triangle ABC$, $AD \perp BC$. If $\angle ABC = 60^\circ$, $\angle ACB = 30^\circ$ and $BC = 36$ cm, then find measures of AB , AC and AD . (MQP 2024 , Average)



32. In the figure, the poles AB and CD of different heights are standing vertically on a level ground. Calculate the angle of elevation from a point P on the line joining the foot of the poles on the level ground, to the tops of the poles. The height of CD and the distance PD are $20\sqrt{3}$ m and 20 m respectively. If $\angle APC = 90^\circ$ and BP is 10 m, then find the length of the pole AB and the distance AC between the tops of the poles. (Difficult)

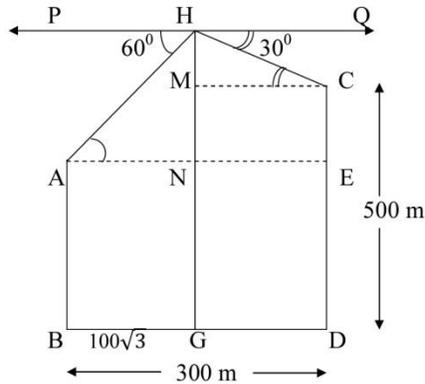


33. Two kites 'A' and 'B' are flying one below the other above the horizontal ground as shown in the figure. Kite 'A' is flying 300 m above the ground. The angles of elevation of kites 'A' and 'B' as observed from a point 'P' on the ground are 60° and 30° respectively. Find the distance between the two kites (AB). After some time when the thread of kite 'A' is released, it moves horizontal to the ground and reaches the point 'A¹' in the sky. If P, B, A¹ are in the same line, then find the distance between the kites (A¹B). (June 2024 , Difficult)



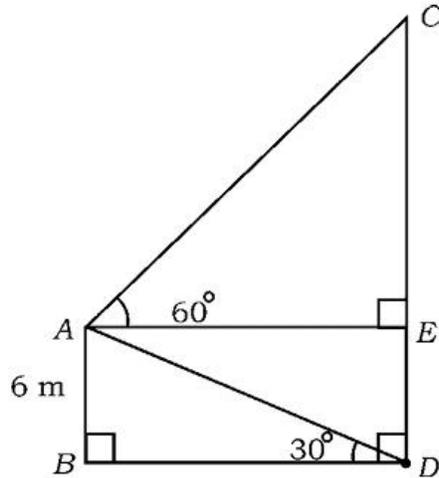
34. There are two vertical towers on a level ground which are 300m apart. A soldier in a helicopter above the ground observes the top of the towers and he found the angles of depression to be 60° and 30° as shown in the figure. If the height of the taller tower is 500 m and the distance between the foot of the shorter tower and the foot of the altitude from the helicopter to the ground is $100\sqrt{3}$ m, then find the height of the shorter tower.

(Exam-3 2024, Difficult)

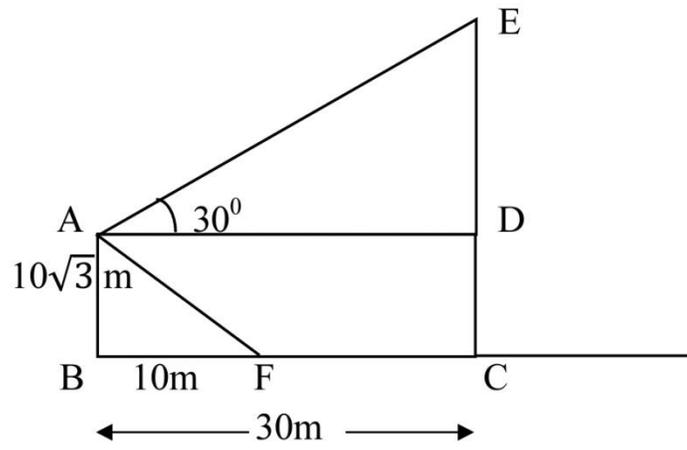


VI. Answer the following questions (5 marks)

35. A pole and a tower are standing vertically on a level ground. The height of the pole is 6m and the angle of elevation to the top of the pole from the bottom of the tower is 30° . The angle of elevation to the top of the tower from the top of the pole is 60° as shown in the figure. Find the height of the tower (CD). Also find the distance (AC) between the top of the pole and the top of the tower (April 2025, Difficult)



36. The lighthouse [AB] of height $10\sqrt{3}$ m stands vertically on a sea shore. A tower [CE] and a ship [F] are standing 30m and 10m away from the foot of the lighthouse respectively. The angle of elevation of the top of the tower from the top of the lighthouse is 30° . Find the height of the tower and distance between the top of the lighthouse to the top of the tower [AE]. Also find the angle of depression formed from the top of the lighthouse to the ship. (Difficult)



UNIT 10: CIRCLES

Learning Points

- ❖ Secant , tangent and point of contact
- ❖ Theorem: “The tangent at any point of a circle is perpendicular to the radius through the point of contact”.”
- ❖ Theorem: “The lengths of tangents drawn from an external point to a circle are equal”
- ❖ Application problems based on theorems

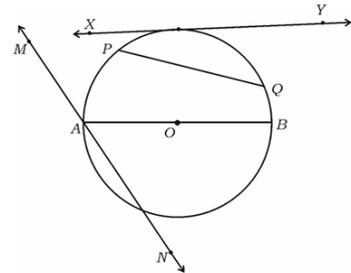
I. Four alternatives are given for each of the following questions/incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

No. of Questions	Easy	Average	Difficult
35	20	12	3

1) In the figure, secant to the circle is,

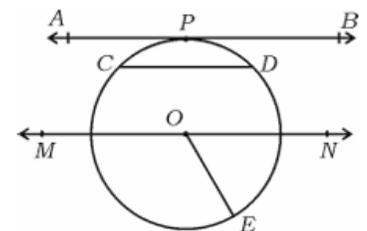
[JUNE 2022, Easy]

- A) AB B) PQ C) XY D) MN



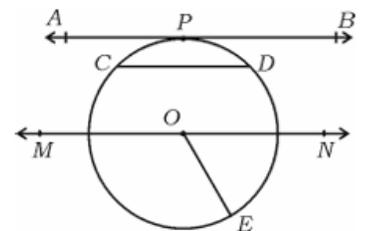
2) In the figure, the tangent to the circle is,
[Easy]

- A) MN B) OE C) CD D) AB



3) In the figure, point of contact is, (Easy)

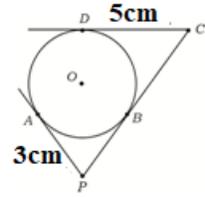
- A) P B) C C) D D) E



- 4) In the figure, PA, PC and PD are tangents drawn to the circle with centre O. If AP = 3cm, CD = 5cm then the length of PC is,

[JUNE 2019, Easy]

- A) 3 cm B) 5 cm C) 8 cm D) 2 cm



- 5) The angle between the tangent and radius drawn at the point of contact is, [MARCH 2022, Easy]

- A) 30° B) 60° C) 90° D) 180°

- 6) The distance between the parallel tangents in the circle of radius 3.5cm is,

[Average]

- A) 7cm B) 14cm C) 3.5cm D) 1.75cm

- 7) A line intersecting a circle in 2 points is a, [JUNE 2020, Easy]

- A) chord B) secant
C) tangent D) radius

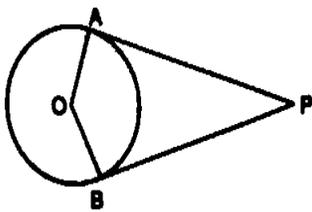
- 8) The line that intersects circle at only one point is a,

[APRIL 2020, Easy]

- (A) tangent (B) secant (C) radius (D) Chord

- 9) In the figure, PA and PB are tangents to the circle with centre O. If $\angle APB = 80^\circ$ then $\angle AOB$ is equal to

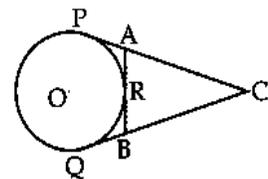
(Average)



- A) 80° B) 100° C) 180° D) 360°

- 10) In the figure CP and CQ are tangents to the circle with centre O. ARB is another tangent at R. If CP = 11cm, BC = 7cm then length of BR is, [Average]

- A) 7 cm B) 5 cm C) 12 cm D) 4 cm

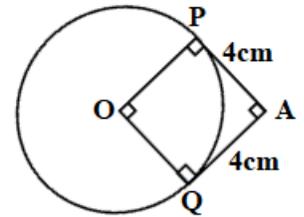


11) If the angle between the two radii drawn in a circle is 130° , then the angle between the tangents drawn at the ends of the radii is, [Average]

- A) 90° B) 50° C) 70° D) 40°

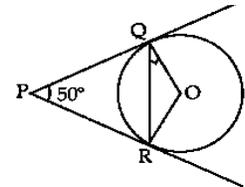
12) In the figure, O is the centre of a circle. AP and AQ are tangents drawn to the circle from the point A such that $\angle PAQ = 90^\circ$. If AP = 4cm then the radius of the circle is, (Average)

- A) 2 cm B) 3cm C) 4 cm D) 1cm



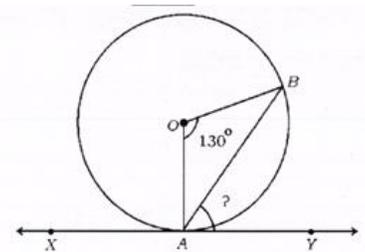
13) In the figure, PQ and PR are tangents drawn to the circle with centre O from the point P such that $\angle QPR = 50^\circ$ then $\angle OQR$ is equal to, [Easy]

- A) 25° B) 35° C) 40° D) 20°



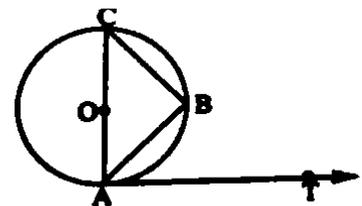
14) In the figure, XY is tangent to the circle with centre O. If $\angle AOB = 130^\circ$ then the measure of $\angle BAY$ is, [MARCH 2025 ,Average]

- A) 90° B) 25° C) 50° D) 65°



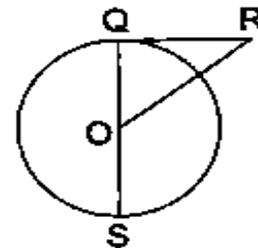
15) In the figure, if $\angle ACB = 50^\circ$ then $\angle BAT$ is equal to, [Average]

- A) 70° B) 60° C) 50° D) 40°



16) In the figure, RQ is tangent to the circle with centre O. If SQ = 6cm, QR = 4cm then the length of OR is [Easy]

- A) 4cm B) 5cm C) 6cm D) 3cm



17) A tangent PQ at a point P of a circle of radius 5cm meets a line through the centre O at a point Q so that OQ = 12cm. Length of PQ is, [Average]

- A) 12cm B) 13cm C) 8.5cm D) $\sqrt{119}$ cm

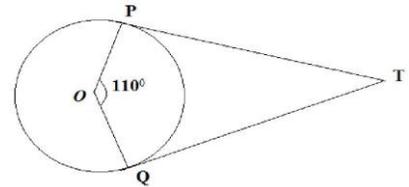
18) If the length of the tangent drawn from Q to the circle is 24cm and the distance from Q to the centre of the circle is 25cm then the radius of the circle is

[Easy]

- A) 7cm B) 12cm C) 15cm D) 24.5cm

19) In the figure, TP and TQ are tangents to the circle with centre O. If $\angle POQ = 110^\circ$ then the measure of $\angle PTQ$ is (Easy)

- A) 60° B) 70° C) 80° D) 90°

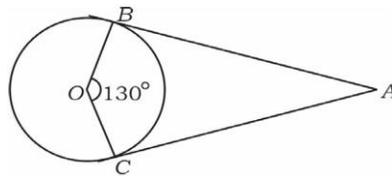


II. Answer the following questions (1 mark)

- 20) What is a tangent? (Easy)
 21) What is a secant? (Easy)
 22) What is the measure of the angle between the tangent and radius drawn at the point of contact in a circle? (Easy)
 23) What is the maximum number of tangents that can be drawn to a circle from an external point? (Easy)
 24) How many tangents can be drawn at a point on the circle? (Easy)

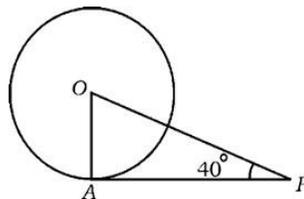
25) In the figure, AB and AC are tangents drawn to a circle with centre O from the external point A. If $\angle BOC = 130^\circ$ then find the measure of $\angle BAC$.

[APRIL 2020, Easy]



26) In the figure, O is the centre of a circle. OA is the radius and AP is the tangent. If $\angle OPA = 40^\circ$ then find the measure of $\angle AOP$.

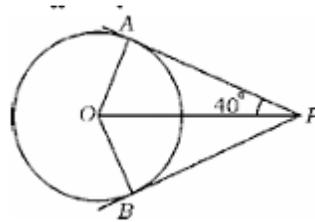
[JUNE 2024 Easy]



III. Answer the following Questions (2 mark)

- 27) In the given figure, PA and PB are tangents to the circle with centre 'O'. If PA= 4 cm and $\angle APO = 40^\circ$, then find the measure of $\angle AOB$ and find the length of PB

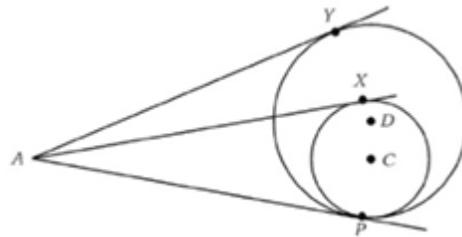
[MARCH 2025, Average]



- 28) In the given figure, AP, AX and AY are the tangents drawn to the circles.

Prove that $AY = AX$

[JUNE 2019, Easy]



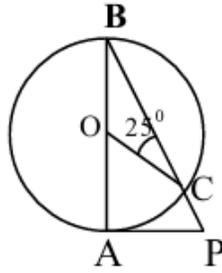
- 29) Two concentric circles of radii 5 cm and 3 cm are drawn. Find the length of the chord of the larger circle which touches the smaller circle at point P.

[JUNE 2019, Easy]



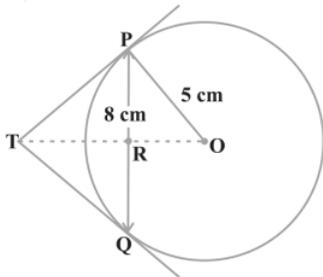
- 30) In a circle with centre O, AB is the diameter and AP is the tangent. If $\angle OCB = 25^\circ$ then find the measure of $\angle APB$

[MODEL 2019, Average]

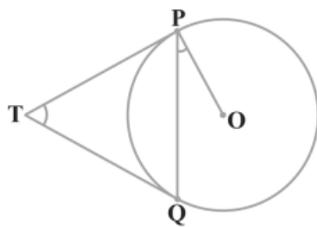


IV. Answer the following questions (3 mark)

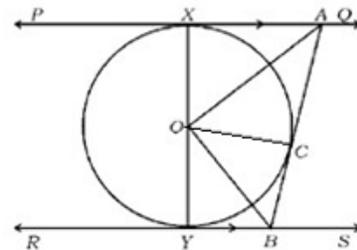
- 31) Prove that “The tangent at any point of a circle is perpendicular to the radius through the point of contact”.
[MARCH 2025, Average]
- 32) Prove that “the lengths of tangents drawn from an external point to a circle are equal”.
[MARCH, JULY 2019, SEPTMBER 2020, MARCH 2022, MARCH, JUNE, AUGUST 2024, Average]
- 33) PQ is a chord of length 8 cm of a circle of radius 5 cm. The tangents at P and Q intersect at a point T. Find the length of TP.
(Difficult)



- 34) Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ = 2 \angle OPQ$.
(Difficult)



- 35) In the given figure, PQ and RS are two parallel tangents to a circle with centre O and another tangent AB with point of contact C intersecting PQ at A and RS at B. Prove that $\angle AOB = 90^\circ$.
[APRIL 2019, Difficult]



UNIT 11: AREAS RELATED TO CIRCLES

Learning Points:

- ❖ Area and perimeter of a circle
- ❖ Sector and area of sector
- ❖ Segment and area of segment
- ❖ Length of arc of a sector
- ❖ Application problems

Number of questions	Easy	Average	Difficult
38	9	19	10

I. Four alternatives are given for each of the following questions/incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. If area of the circle is 49π sq. units then its perimeter is, [April 2019 Easy]
 A) 7π units B) 9π units C) 14π units D) 49π units

2. The total area of two congruent circles of radius r units is, [MQP 2019 Easy]
 A) $2\pi r^2$ B) 2 C) $\frac{1}{2}\pi r^2$ D) πr^2

3. In a circle of radius r the length of an arc of a sector of angle θ is, [June 2020 Easy]
 A) $\frac{\theta}{360} \times \pi r^2$ B) $\frac{\theta}{360} \times 2\pi r^2$ C) $\frac{\theta}{180} \times \pi r$ D) $\frac{\theta}{180} \times 2\pi r$

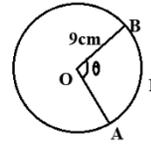
4. The area of sector of $\frac{1}{4}$ th part of the circle with radius r cm is, [SLP 2020 Easy]
 A) $\frac{\pi r^2}{360}$ cm² B) $\frac{\pi r^2}{90}$ cm² C) $\frac{\pi r^2}{4}$ cm² D) $\frac{\pi r^2}{2}$ cm²

5. The area of sector of $\frac{3}{4}$ th part of the circle with radius r cm is, [Average]
 A) $\frac{\pi r^2}{360}$ cm² B) $\frac{\pi r^2}{90}$ cm² C) $\frac{3\pi r^2}{4}$ cm² D) $\frac{\pi r^2}{2}$ cm²

6. If diameter of the circle is 14cm, then its circumference is [June 2024 Average]
 A) 28 cm B) 44 cm C) 56 cm D) 88 cm

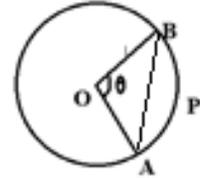
7. In the figure, O is centre of the circle and length of the arc APB is 4π cm. If $OB = 9$ cm then the measure of θ is, [March 2025 Average]

A) 60° B) 80° C) 85° D) 70°



8. In the figure, area of segment APB is, (Average)

A) Area of circle – area of Δ AOB
 B) Area of circle – Area of minor sector
 C) Area of sector OAPB – area of Δ AOB
 D) Area of circle – Area of major sector



9. If the diameter of a circle is 21cm, then its circumference is,

A) 44 cm B) 88 cm C) 66 cm

[Average]

D) 55 cm

10. If the area of a circle is 154cm^2 , then its circumference is,

A) 11 cm B) 22 cm C) 44 cm

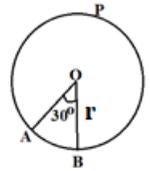
[Average]

D) 55 cm

11. In the figure, radius of the circle with centre O is r cm. Area of sector OAPB is,

A) $\frac{(360-30)\pi r^2}{360} \text{cm}^2$ B) $\frac{(360+30)\pi r^2}{360} \text{cm}^2$ C) $\frac{30\pi r^2}{360} \text{cm}^2$ D) $\frac{60\pi r^2}{360} \text{cm}^2$

[Average]



12. The length of arc of a quadrant of radius r cm is,

A) $\frac{\pi r}{4}$ cm B) $4\pi r$ cm C) $\frac{\pi r}{2}$ cm D) $2\pi r$ cm

[Average]

II. Answer the following questions (1 mark)

13. Write the formula to find area of a sector of a circle, if angle at the centre is ' θ ' degrees.

[June 2019 Easy]

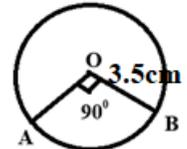
14. Write the formula to find length of the arc of sector of a circle, if angle at the centre is ' θ ' degrees. (Easy)

15. A circle is divided into 8 equal parts. Find the measure of the angle formed at the centre in each sector. (Easy)

16. In the figure, O is the centre of a circle of radius 3.5cm and $\angle AOB = 90^\circ$.

Find the length of the minor arc

[Average]



17. If the diameter of the circle is 7cm then find the length of the semicircular arc. [Average]

18. The area of a quadrant is $\frac{77}{2} \text{cm}^2$. Find the radius of the circle.

(Easy)

19. The length of the arc of the quadrant of a circle is 22cm. Find the radius of the circle.

(Easy)

20. If the area of a circle and its circumference are numerically equal then find the radius of the circle.

(Average)

III. Answer the following questions (2 marks)

21. In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find the length of the arc

[Average]

22. In a circle of radius 4 cm, an arc subtends an angle of 45° at the centre. Find the area of the sector.

(Use $\pi = 3.14$)

[Average]

23. Areas of two circles C_1 and C_2 are 92cm^2 and 62cm^2 respectively. Find the radius of the circle C_3 whose area is equal to sum of areas of C_1 and C_2 .

[June 2019 Average]

24. The length of the minute hand in a clock is 14 cm. Find the area swept by the minute hand in 10 minutes.

[MQP -2 2025 Average]

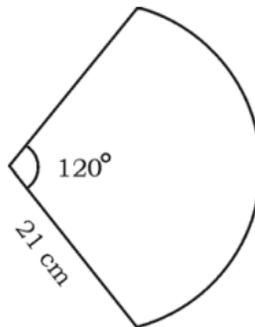
25. Find the area of the quadrant of a circle whose radius is 20 cm and also find the perimeter of the quadrant.

[MQP -2 2025 Average]

IV. Answer the following (3 marks)

26. A hand fan is made up of cloth fixed in between the metallic wires. It is in the shape of a sector of a circle of radius 21 cm and of angle 120° as shown in the figure. Calculate the area of the cloth used and also find the total length of the metallic wire required to make such a fan.

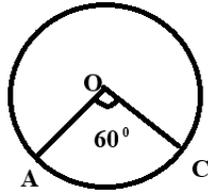
[June 2020 Difficult]



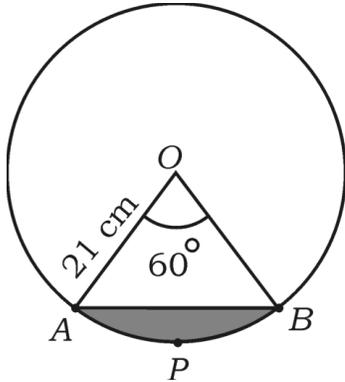
27. In a circle of radius 21 cm, an arc AC subtends an angle of 60° at the centre.

Find: (i) the length of the arc AC (ii) area of the sector OAC formed by the arc

[SLP 2022 Average]



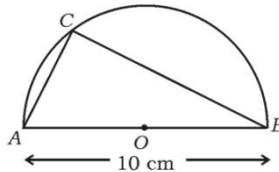
28. In the given figure, O is the centre of the circle of radius 21cm. If $\angle AOB = 60^\circ$ then find the area of the segment. (Take $\sqrt{3} = 1.73$)



[March 2025 Average]

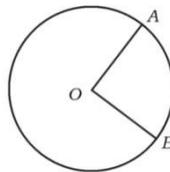
29. In the given figure, ACB is a semicircle. If $AB = 10$ cm and $AC = 6$ cm, then find the area of the segments in the semicircle.

[Difficult]

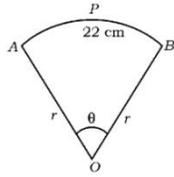


30. In the figure 'O' is the centre of the circle. Area of a sector AOB : Area of the circle = 1 : 5 and if the radius of the circle is 7 cm then find the length of the arc AB .

[MQP 3 2025 Difficult]

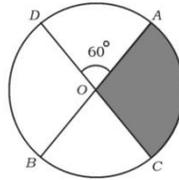


31. In the figure, the area of the sector AOBP is 231 cm^2 and length of the arc APB is 22 cm . Find the radius and the measure of angle θ [April 2024 Difficult]



32. In the figure, diameters AB and CD intersect at O. If the length of the arc BC = 22 cm and $\angle AOD = 60^\circ$ then find the area of the sector AOC.

[Aug 2024 Difficult]

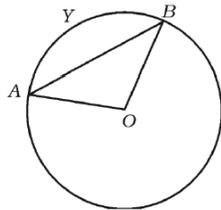


33. The area of the sector of a circle is numerically equal to the length of the arc of the same sector. If the length of the arc is $\frac{44}{21} \text{ cm}$, then find the radius of the circle and also the angle subtended by the arc at the centre.

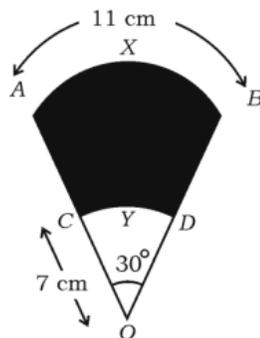
[MQP Difficult]

34. The area of the sector OAYB shown in the figure is 462 cm^2 . Find the length of the arc AYB if $\angle AOB = 120^\circ$.

[Average]

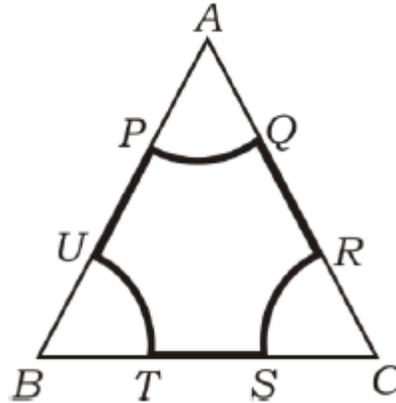


35. In the figure AXB and CYD are the arcs of two concentric circles with centre O. The length of the arc AXB is 11 cm . If $OC = 7 \text{ cm}$ and $\angle AOB = 30^\circ$, then find the area of the shaded region. [Take $\pi = \frac{22}{7}$]

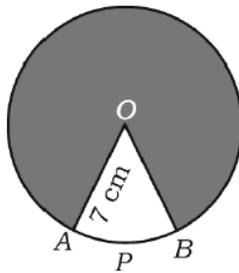


(Difficult)

36. ABC is an equilateral triangle. Arcs are drawn in ΔABC with A, B and C as the centres of the circles of radius 3.5 cm as shown in the figure. If the area of the ΔABC is $49\sqrt{3}$ cm², then find the perimeter of the shape $PQRSTUP$.

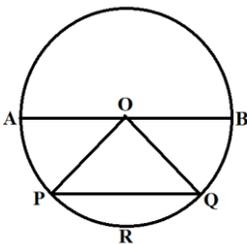


37. In the given figure O is centre of the circle of radius 7 cm. If the length of the arc APB is $\frac{22}{3}$ cm then find the area of the shaded region. (Take $\pi = \frac{22}{7}$)



(May 2025 - Difficult)

38. In the given figure, the length of the semicircular arc of the circle with centre O is 44 cm. If $\angle OPQ = 45^\circ$ then find the area of the segment PRQ .
(SLP 2025 – Difficult)



UNIT 12: SURFACE AREAS AND VOLUMES

Learning Points:

- ❖ Curved surface area, Total surface area and volumes of Cube, cuboid, cylinder, cone, sphere and hemisphere.
- ❖ Surface area of combined solids
- ❖ Volume of combined solids
- ❖ Application problems

Number of questions	Easy	Average	Difficult
65	26	23	16

I. Four alternatives are given for each of the following questions/incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet.

(1 Mark)

1. The formula to find the total surface area of cube of edge 'a' units is, [Easy]
 A) $4a^2$ B) $6a^2$ C) $4a^3$ D) $6a^3$
2. The formula to find the lateral surface area of cube of edge 'a' units is, [Easy]
 A) $6a^2$ B) $4a^3$ C) $6a^3$ D) $4a^2$
3. The formula to calculate the volume of a cube of edge 'a' units is, [Easy]
 A) a^2 B) a^4 C) a^3 D) a^6
4. The formula to find the total surface area of a cuboid of length 'l', breadth 'b' and height 'h' is, [Easy]
 A) $2(lb+bh+hl)^2$ B) $l \times b \times h$ C) $2l(b \times h)$ D) $l+b+h$
5. The formula to find the lateral surface area of a cuboid of length 'l', breadth 'b' and height 'h' is, [Easy]
 A) $2l(b+h)$ B) $2h(l+b)$ C) $l \times b \times h$ D) $2l \times 2b \times 2h$
6. The formula to find the volume of a cuboid of length 'l', breadth 'b' and height 'h' is, [Easy]
 A) $l+b+h$ B) $l \times b \times h$ C) $lb \div h$ D) $(l \times h) \div b$
7. The formula to find the curved surface area of a right circular cylinder of base radius 'r' and height 'h' is, [Easy]
 A) $\pi r^2 h$ B) $\pi r(r+h)$ C) $\pi h(r+r)$ D) $2\pi r h$
8. The formula used to find the total surface area of a right circular cylinder of base radius 'r' and height 'h' is, [Easy]
 A) $2\pi(r+h)$ B) $2\pi r h$ C) $\pi h(r+r)$ D) $\pi r^2 h$

9. The formula used to find the volume of a right circular cylinder of base radius 'r' and height 'h' is, [Easy]

- A) πr^2 B) $2\pi r^2 h$ C) $\pi r^2 h$ D) $2\pi r h$

10. The formula used to find the curved surface area of a right circular cone of base radius 'r' and slant height 'l' is, [Easy]

- A) $\pi r l$ B) $\pi r^2 l$ C) $\pi r^2 h$ D) $\frac{1}{3}\pi r^2 h$

11. The formula used to find the total surface area of a right circular cone of base radius 'r' and slant height 'l' is, [Easy]

- A) $2\pi r h$ B) $\pi r(r+l)$ C) $\pi r^2 h$ D) $\frac{1}{3}\pi r^2 h$

12. The formula used to find the volume of a right circular cone of base radius 'r' and slant height 'l' and vertical height 'h' is, [Easy]

- A) $\pi r^2 h$ B) $\pi r(r+l)$ C) $\frac{1}{3}\pi r^2 h$ D) $\pi r l$

13. The formula used to find the surface area of a sphere of radius 'r' is

- A) πr^2 B) $2\pi r^2$ C) $3\pi r^2$ D) $4\pi r^2$ [Easy]

14. The formula used to calculate volume of a sphere of radius 'r' units is

(July 2022) [Easy]

- A) $\frac{2}{3}\pi r^2$ cubic units B) $\frac{1}{3}\pi r^3$ cu.units C) $\frac{4}{3}\pi r^3$ cu.units D) $\frac{4}{3}\pi r^2$ cu.units

15. The ratio between volumes of cylinder and cone whose base radius and vertical heights are equal [Average]

- A) 1 : 3 B) 6 : 1 C) 3 : 1
D) 1 : 6

16. The base radius and the height of a cylinder and cone are equal. If the volume of cylinder is 60 cm^3 then the volume of cone is, [Average]

- A) 180 cm^3 B) 18 cm^3 C) 30 cm^3 D) 20 cm^3

17. The base radius of a cone is 8cm and its slant height is 10cm. Its vertical height is,

[Average]

- A) 3cm B) 6cm C) 5cm D) 10cm

18. The volume of a cube of edge 6cm is,

[Average]

- A) 36 cm^3 B) 12 cm^3 C) 216 cm^3 D) 18 cm^3

19. The volume of a cuboid whose length, breadth and height are 2cm, 3cm and 5cm respectively is, [Easy]

- A) 10 cm^2 B) 16 cm^3 C) 60 cm^3 D) 30 cm^3

20. The curved surface area of a cylinder is 100 cm^2 and its height is 10cm. The circumference of its base is, [Easy]

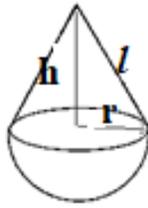
- A) 100cm B) 10cm C) 20cm D) 50cm

21. The amount of water required to fill the tank of length 5m, breadth 6m and height 2m completely is, [Difficult]
 A) 6L B) 60L C) 20L D) 60,000L
22. If the area of base of a cylinder is 22cm^2 and height is 10 cm then its volume is [Easy]
 A) 22000cm^3 B) 2200cm^3 C) 220cm^3 D) 220cm^2
23. The base radius and the height of a cylinder and cone are equal. If the volume of cylinder is 360cm^3 then the volume of cone is (Sept 2020) [Average]
 A) 120cm^3 B) 180cm^3 C) 90cm^3 D) 360cm^3
24. The surface area of sphere with radius 7cm is (Sept 2020 Average)
 A) 154cm^2 B) 616cm^3 C) 616cm^2 D) 308cm^2
25. The volume of a cube with edge is 5 cm is (Easy)
 A) 125cm^2 B) 30cm^3 C) 100cm^3 D) 125cm^3

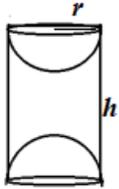
II. Answer the following: (1 mark)

26. Write the formula to find the total surface area of a hemisphere with radius is 'r' units. [Easy]
27. Write the formula to find the curved surface area of a hemisphere whose radius is 'r' units. [Easy]
28. Write the formula to find the volume of a hemisphere whose radius is 'r' units. [Easy]
29. Write the formula to find the volume of a sphere whose radius is 'r' units. [Easy]
30. Find the ratio of the volumes of sphere and hemisphere having equal radius. [Average]
31. Find the ratio of the total surface areas of sphere and hemisphere having equal radius. [Average]
32. The base radius and the height of a cylinder and cone are equal. If volume of the cone is 30cm^3 then find the volume of cylinder. [Average]
33. The circumference of the base of a cylinder is 10cm and its height is 25cm. Find its curved surface area. [Average]

34. Write the formula to calculate the total surface area of the toy shown in the figure. [Difficult]



35. The hemispheres are hollowed out from the base of a cylinder as shown in the figure. Write the formula to find the volume of the solid. [Difficult]



36. Find the radius of the cylinder whose volume is 500cm^3 and height is 10cm. [Average]

37. The ratio of diameters of two cylinders is 9:1 and the ratio of their heights is 1:9. Find the ratio of their volumes. [Difficult]

38. Find the surface area of a sphere of radius 7cm. [April 2018 Easy]

III. Answer the following questions : (2 marks)

39. Find the curved surface area of a cylinder whose height is 20cm and radius is 6cm. [Easy].

40. A cuboid is formed by joining two identical cubes of volume 27cm^3 . Find the total surface area of the cuboid. [Easy]

41. A toy is made by joining a cone of radius 7cm and height 4cm on a hemisphere of radius 7cm. Find the volume of the toy. [Average]

42. Two hemispheres of radius 7cm are joined at the ends of a cylinder of radius 7cm and height 10cm. Find the total surface area of the solid. [Average]

43. The volume of a cube is 125cm^3 . Find its lateral surface area. [Average]

44. The volume of a sphere is 38808 cm^3 . Find its surface area. [Difficult]

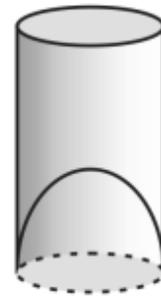
IV. Answer the following questions (3 marks)

45. A toy is in the form of a cone of radius 6 cm mounted on a hemisphere of same radius. The total height of the toy is 14 cm. Find the total surface area of the toy. [Average]

46. A solid is made as shown in the figure. The height of the cylinder is 10cm and its radius is 3.5cm. Find the total surface area of the solid. [Average]



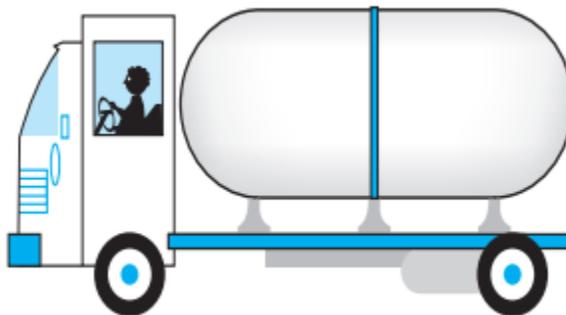
47. A juice seller was serving his customers using glasses as shown in Figure. The inner diameter of the cylindrical glass was 6 cm and the height of a glass is 12 cm. Find the actual capacity of the glass. [Difficult]



48. A circus tent is built in the shape of a cylinder surmounted by a conical top using canvas. If the height and diameter of the cylinder are 5 m and 126 m respectively, and the total height of the tent is 21 m, then find the area of the canvas used for making the tent. [Difficult]

V. Answer the following questions (4 marks)

49. A lorry has a fully filled petrol tank with hemispheres attached at both ends of the cylinder as shown in the figure. Petrol was drained from the tank at a rate of 742.5L per minute in 1 hour. If the diameter of the tank is 3m, find the length of the tank. [Difficult]



50. A cone is mounted on a hemisphere whose radius is same as that of the hemisphere. If the volume of hemisphere is $\frac{539}{6} \text{ cm}^3$ and the slant height is 12.5cm then find the surface area of the solid.

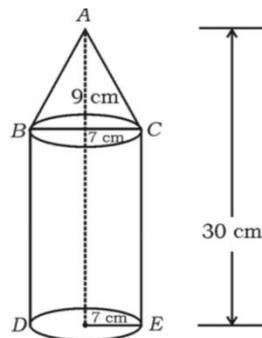
[Average]

51. A spherical glass vessel has a cylindrical neck 8 cm long, 2 cm in diameter; the diameter of the spherical part is 8.5 cm. By measuring the amount of water it holds, a child finds its volume to be 345 cm^3 . Check whether she is correct, taking the above as the inside measurements, and $\pi = 3.14$.

[Difficult]

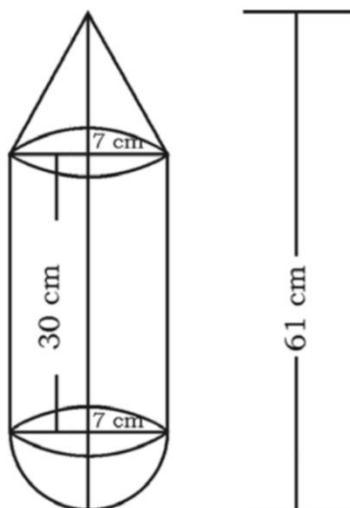
52. A solid is in the form of a cone mounted on a right circular cylinder, both having same radii as shown in the figure. The radius of the base and height of the cone are 7 cm and 9 cm respectively. If the total height of the solid is 30 cm, find the volume of the solid.

[April 2018 Average]

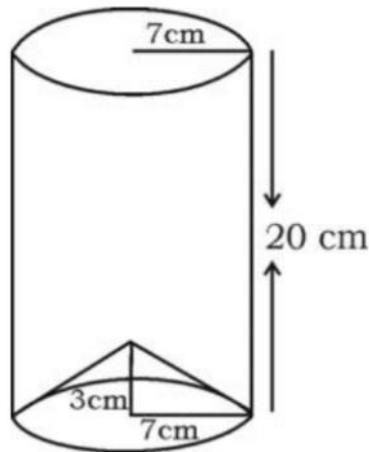


53. A solid is in the shape of a cylinder with a cone attached at one end and a hemisphere attached to the other end as shown in the figure. All of them are of the same radius 7 cm. If the total length of the solid is 61 cm and height of the cylinder is 30 cm, calculate the cost of painting the outer surface of the solid at the rate of Rs. 10 per 100 cm^2 .

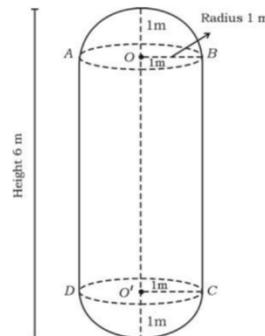
[June 2018 Difficult]



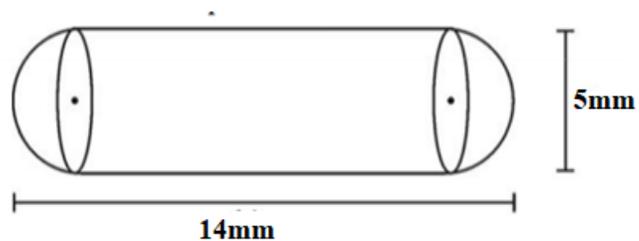
54. The bottom of a right cylindrical shaped vessel made from metallic sheet is closed by a cone shaped vessel as shown in the figure. The radius of the circular base of the cylinder and radius of the circular base of the cone each is equal to 7 cm. If the height of the cylinder is 20 cm and height of cone is 3 cm, calculate the cost of milk to fill completely this vessel at the rate of Rs. 20 per litre. [March 2019 Difficult]



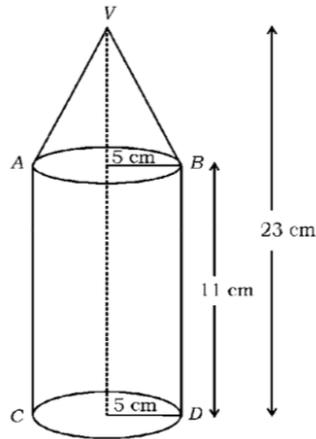
55. A milk tank is in the shape of a cylinder with hemispheres of same radii attached to both ends of it as shown in figure. If the total height of the tank is 6 m and the radius is 1 m, calculate the maximum quantity of milk filled in the tank in litres. [June 2019 Average]



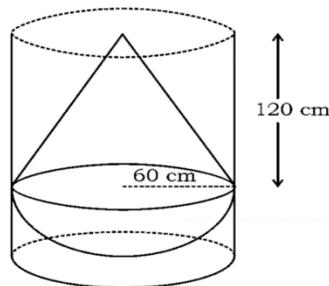
56. A medicine capsule is in the shape of a cylinder with hemispheres stuck to each of its ends. The length of the entire capsule is 14 mm and the diameter of the capsule is 5 mm. Find its surface area. [Sept 2020 Difficult]



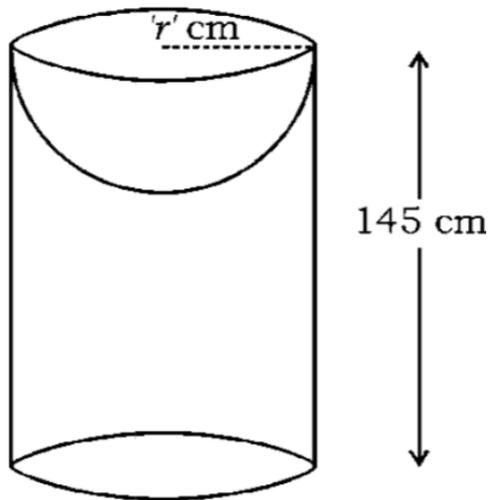
57. A solid is in the shape of a cone placed on the cylinder as shown in the figure. The radii of both the cylinder and the cone are equal to 5 cm. If the height of the cylinder is 11 cm and the total height of the solid is 23 cm, then find the curved surface area and volume of the solid. [June 2024 Average]



58. A solid consisting of a right circular cone of height 120 cm and radius 60 cm standing on a hemisphere of radius 60 cm is placed upright in a right circular cylinder full of water such that it touches the bottom as shown in the figure. If the radius of the cylinder is 60 cm and height is 180 cm, then find the volume of water left in the cylinder in terms of π . [April 2025 Difficult]

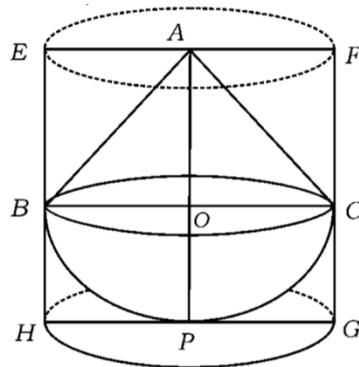


59. A solid is made of a cylinder with a hemispherical depression having the same radius ('r' cm) as that of cylinder at the top end as shown in the figure. The volume of the hemispherical depression is $18000 \pi \text{ cm}^3$. If the height of the cylinder is 145 cm, then find the total surface area of the solid. [April 2025 Difficult]



60. A solid toy is in the form of a hemisphere surmounted by a right circular cone. The height of the cone is 2 cm and the diameter of the base is 4 cm. Determine the volume of the toy. If a right circular cylinder circumscribes the toy as shown in the figure, find the difference of the volumes of the cylinder and the toy.

[May 2025 Difficult]



61. From a solid cylinder whose height is 2.4 m and diameter is 1.4 m, a conical cavity of the same height and same diameter as that of the cylinder is hollowed out. Find the total surface area of the remaining solid..

[May 2025 Average]

VI. Answer the following questions (5 marks)

62. A toy is made by attaching a hemisphere to one side and a cone on the other side of a cylinder. The diameter of these three solids are same. The diameter of cylinder is 10 cm and its height is 20 cm. If the slant height of the cone is 13 cm then find the surface area and volume of the toy.

[Easy]

63. From a solid cylinder whose height is 2.8 cm and diameter is 4.2 cm, a conical cavity of the same height and same diameter is hollowed out. Find the total surface area of the remaining solid.

[Difficult]

64. From a wooden cylinder of radius 6cm and height 27cm, a hemisphere and a cone of radius same as that of the cylinder are carved out from either bases of the cylinder. If the height of the cone is 8 cm then find the surface area and volume of the solid.

[Average]

65. The volume of a cylinder is 5 times the volume of a cone. The radius of the base and the slant height of the cone are 7 cm and 25 cm respectively. The radius of the base of the cylinder is 14 cm. Find the volume and lateral surface area of the cylinder.

[Aug 2024 Difficult]

UNIT : 13 STATISTICS

Learning Points:

- ❖ Mean, Median and Mode for grouped data
- ❖ The relationship between Mean, Median and Mode

Number of questions	Easy	Average	Difficult
64	14	47	3

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. The most repeated score in the given dataset is, (April 2021 Easy)
A) Mean B) Mode C) Median D) Range

2. The formula to find the midpoint of a class interval is, (Easy)
- A) $\frac{\text{Upper class limit} - \text{Lower class limit}}{2}$ B) $\frac{\text{Upper class limit} \times \text{Lower class limit}}{2}$
C) $\frac{\text{Upper class limit} + \text{Lower class limit}}{2}$ D) $\frac{\text{Upper class limit} + \text{Lower class limit}}{3}$

3. The lower limit of the modal class in the given frequency distribution is (Easy)

Class Interval	10-20	20-30	30-40	40-50
Frequency	6	4	12	3

- A)10 B)20 C)30 D)50

4. If The mean of a data is 7.5 , $\sum \text{fixi} = 120+3k$ and $\sum \text{fi} = 30$ then the value of 'k' is, (Easy)
A) 35 B) 3.5 C) 0.35 D) 3.05
5. Cumulative frequency is calculated **to find** (Easy)

- A) Mean B) Median C) Mode D) Deviation

6. The empirical relationship between the three measures of central tendency is, (April 2024) (Easy)

- A) 3 Median = 2 Mean + Mode B) 3 Mean = 2 Median + Mode
C) Mean = 3 Median + Mode D) Mode = 3 Mean +2 Median

7. In the formula to find the median, $\text{Median} = L + \left(\frac{\frac{n}{2} - Cf}{f}\right) \times h$ 'h' refers to (Average)
- A) Lower limit of the median class
 B) frequency of median class
 C) size of the class interval
 D) cumulative frequency
8. The Mean and Mode of the given set of a data are 7.5 and 6. The median of the data is, (Average)
- A) 3 B) 5 C) 7 D) 9
9. The median of the heights of girls in a school is, 149.03cm. The interpretation of this statement is, (Average)
- A) The height of 25% of girls is more than 149.03cm and the height of 75% of the girls is less than 149.03cm
 B) The height of 50% of girls is more than 149.03cm and the height of 50% of the girls is less than 149.03cm
 C) The height of 75% of girls is more than 149.03cm and the height of 25% of the girls is less than 149.03cm
 D) The height of 60% of girls is more than 149.03cm and the height of 40% of the girls is less than 149.03cm
10. The formula to find the mean by step deviation method is, (MQP -4 2025 EASY)
- A) $\bar{x} = a + \frac{\sum f_i u_i}{\sum f_i} \times h$ B) $\bar{x} = a + \frac{\sum f_i}{\sum f_i u_i} \times h$
 C) $\bar{x} = a \times \frac{\sum f_i u_i}{\sum f_i} \times h$ D) $\bar{x} = a \div \frac{\sum f_i u_i}{\sum f_i} \times h$

II. Answer the following questions. (1 Mark)

11. Write the midpoint of the class interval 10 – 24. (Easy)
12. In the given frequency distribution table write the median class interval.

(SLP -2024 – Easy)

Marks	Number of Students	Cumulative Frequency
0– 10	3	3
10 – 20	4	7
20 – 30	7	14
30 – 40	6	20
	n = 20	

13. In the given frequency distribution tables write the modal class. (March 2025 – Easy)

Class interval	Frequency
1-3	4
3-5	8
5-7	2
7-9	2

14. Write the formula to find the mean by direct method. (June 2021 Easy)

15. Find the upper limit of the modal class in the given frequency distribution table.

(March 2025 Easy)

Class Interval	0 -10	10 -20	20 -30	30 -40	40 -50
Frequency	5	8	7	12	6

16. If the Median of a data is 3 more than Mean, then by how much does the Mode exceed the Mean?

(Average)

17. Write the formula to find the median for grouped data. (Easy)

18. Write the formula to find the mode for grouped data. (Easy)

19. Find the Median of the data whose Mode is 12.4 and Mean is 10.5 (Average)

20. Find the Mode of the data whose Mean is 27 and Median is 33 (Average)

21. If the Mode and Mean of a given data is 7 and 8 respectively, then find the Median.

(Average)

III. Answer the following questions. (2 Marks)

22. The Mode and Median of a given data are 50.5 and 45.5 respectively. Find the Mean using formula. (Average)

23. Find the Mean for the given data by direct method. (Average)

Class Interval	Frequency
1-5	2
6-10	3
11-15	4
16-20	1

24. Complete the following table by considering the Assumed Mean of the data to be 62.5 (Average)

Class interval C I	Frequency f_i	Midpoint x_i	Deviation d_i
10 – 25	2		
25 – 40	3		
40 – 55	7		
55 – 70	6		
70 – 85	6		
85 - 100	6		

IV. Answer the following questions. (3 Marks)

25. Find the Mean for the given data by direct method

(Average)

Class Interval	Frequency
45-55	3
55-65	10
65-75	11
75-85	8
85-95	3

26. Find the Mean for the given data by direct method

(Average)

Class Interval	Frequency
1 – 3	2
3 – 5	5
5 – 7	8
7 – 9	3
9 - 11	2

27. Find the Mean for the following frequency distribution table

(Average)

Class Interval	Frequency
10 – 14	2
15 -19	3
20 -24	5
25 -29	3
30 – 34	2

28. Find the Mean for the following frequency distribution table

(Average)

Class Interval	Frequency
0 – 10	4
10 – 20	9
20 – 30	15
30 – 40	14
40 – 50	8

29. The Mean for the given data is 18. Find the value of 'x'

(Difficult)

Class Interval	Frequency
11 – 13	7
13 -15	6
15 – 17	9
17 -19	13
19 -21	x
21 – 23	5
23 – 25	4

30. Find the Mean for the following grouped data.

(Average)

Class Interval	15 – 25	25 -35	35 -45	45 -55	55 – 65
Frequency	5	8	12	15	9

31. Find the Mean for the following grouped data using assumed mean method.

(Difficult)

Class Interval	0 -10	10 – 20	20 – 30	30 – 40	40 – 50
Frequency	7	8	12	13	10

32. Find the Mean for the following data using step deviation method.

(Difficult)

Class Interval	20 -40	40 – 60	60 -80	80 -100	100 – 120
Frequency	7	15	20	8	5

33. Find the Mean for the following grouped data. (April 2022) (Average)

Class Interval	10 -20	20 -30	30 -40	40 -50	50 - 60
Frequency	2	3	5	7	3

34. Find the Mean for the following grouped data. (March 2025) (Average)

Class Interval	10 -20	20 -30	30 -40	40 -50	50 - 60
Frequency	2	3	6	5	4

35. Find the Mean for the following grouped data. (August 2024) (Average)

Class Interval	10 -20	20 -30	30 -40	40 -50	50 - 60
Frequency	2	5	6	5	2

36. Find the Mean for the following grouped data by direct method (June 2024)
(Average)

Class Interval	10 -20	20 -30	30 -40	40 -50	50 - 60
Frequency	4	6	5	4	1

37. Find the Mean for the given frequency distribution table by direct method (July 2022)
(Average)

Class Interval	5 -15	15 -25	25 -35	35-45	45 - 55
Frequency	1	3	5	4	2

38. Find the Mean for the given frequency distribution table (June 2023) (Average)

Class Interval	5 -15	15 -25	25 -35	35-45	45 - 55
Frequency	4	6	5	6	4

39. Find the Mean for the given data by direct method. (July 2024) (April 2024) (Average)

Class Interval	2 - 6	6 - 10	10 - 14	14 - 18	18 - 22
Frequency	4	8	2	1	5

40. Find the Mean for the given data. (February 2022) (Average)

Class Interval	0 - 10	10 - 20	20 - 30	30 - 40	40 - 50
Frequency	5	8	20	15	7

41. Find the Mean for the given data. (April 2023) (Average)

Class Interval	Frequency
1 - 5	4
6 - 10	3
11 - 15	2
16 - 20	1
21 - 25	5

42. Find the Median for the following frequency distribution table. (Average)

Class Interval	100-150	150-200	200-250	250-300	300-350
Frequency	6	3	5	20	10

43. Find the Median for the following frequency distribution table. (Average)

Class Interval	50 - 60	60 - 70	70 - 80	80 - 90	90 - 100
Frequency	6	9	20	10	5

44. Find the Median for the following frequency distribution table. (June 2024) (Average)

Class Interval	50 - 60	60 - 70	70 - 80	80 - 90	90 - 100
Frequency	5	8	10	4	3

45. Find the Median for the following frequency distribution table.

Class Interval	1 - 10	11 - 20	21 - 30	31 - 40	41 - 50
Frequency	5	8	20	15	7

46. Find the Median for the following frequency distribution table.

Class Interval	0 - 20	20 - 40	40 - 60	60 - 80	80 - 100
Frequency	6	5	9	4	2

47. Find the Median for the following frequency distribution table.

Class Interval	20-40	40 -60	60 -80	80 -100	100-120
Frequency	7	15	20	2	4

48. Find the Median for the following frequency distribution table. (June 2020) (Average)

Class Interval	20-40	40 -60	60 -80	80 -100
Frequency	7	15	20	8

49. Find the Median for the following frequency distribution table. (July 2022) (Average)

Class Interval	0 -20	20 -40	40 -60	60 -80	80 -100
Frequency	6	9	10	8	7

50. Find the Median for the following frequency distribution table. (Average)

Class Interval	5 -15	15 -25	25 -35	35-45	45 – 55
Frequency	1	3	5	7	2

51. Find the Median for the following frequency distribution table. (Average)

Class Interval	5 -15	15 -25	25 -35	35-45	45 – 55
Frequency	3	4	8	7	3

52. Find the Median for the following frequency distribution table. (March 2025 Average)

Class Interval	15 -20	20 -25	25 -30	30-35	35-40
Frequency	4	5	10	5	6

53. Find the Median for the following frequency distribution table. (Average)

Class Interval	50-52	53-55	56-58	59-61	62 – 64
Frequency	15	110	135	115	25

54. Find the Median for the following frequency distribution table. (Average)

(April 2019)

Class Interval	1 - 4	4 - 7	7 - 10	10 -13	13 - 16	16- 19
Frequency	6	30	40	16	4	4

55. Find the Mode for the following frequency distribution table. (Average)

Class Interval	10 -20	20 -30	30 -40	40 -50	50 - 60
Frequency	6	4	12	3	5

56. Find the Mode for the following frequency distribution table. (Average)

Class Interval	5-10	10-15	15-20	20-25	25-30
Frequency	3	5	8	4	5

57. Find the Mode for the following frequency distribution table. (Average)

Class Interval	1-3	3-5	5-7	7-9	9-11
Frequency	7	8	2	2	1

58. Find the Mode for the following frequency distribution table. (Average)

Class Interval	0 -20	20 -40	40 -60	60 -80	80 -100
Frequency	10	35	52	61	38

59. Find the Mode for the following frequency distribution table. (Average)

Class Interval	0 -10	10 -20	20 -30	30 -40	40 -50
Frequency	6	9	15	9	1

60. Find the Mode for the following frequency distribution table. (Average)

Class Interval	0 -10	10 - 20	20 - 30	30 - 40	40 - 50
Frequency	7	9	15	11	8

61. Find the Mode for the following frequency distribution table. (Average)

Class Interval	0 -10	10 -20	20 -30	30 -40	40 -50
Frequency	7	8	2	2	1

62. Find the Mode for the following frequency distribution table. (Average)

Class Interval	1-3	4-6	7-9	10-12	13-15
Frequency	7	8	2	2	1

63. Find the Mode for the following frequency distribution table. (Average)

Class Interval	5 -15	15 -25	25 -35	35-45	45 - 55
Frequency	3	4	8	7	3

64. Find the Mode for the following frequency distribution table. (Average)

Class Interval	10 -20	20 -30	30 -40	40 -50	50 - 60
Frequency	3	9	6	7	5

UNIT 14: PROBABILITY

Learning Points:

- ❖ Random Experiment
- ❖ Equally likely outcomes of an experiment
- ❖ Definition of Probability – Probability formula
- ❖ Sure Event and Impossible Event
- ❖ The elementary events of an experiment
- ❖ The relationship between the probability of an event $P(E)$ and the probability of complementary event $P(\overline{E})$
- ❖ Probability in daily life situations.

Number of questions	Easy	Average	Difficult
64	14	39	11

I. Four alternatives are given for each of the following questions / incomplete statements. Choose the correct alternative and write the complete answer along with its letter of alphabet. (1 Mark)

1. The probability of a sure event is, (June 2017, April 2024, Easy)
A) 1 B) 0 C) -1 D) 1.5
2. The probability of an impossible event is, (April 2020, Easy)
A) 1 B) 0 C) -1 D) 1.5
3. In an experiment of tossing a coin, the number of all possible outcomes is, (Easy)
A) 1 B) 2 C) 3 D) 4
4. In an experiment of tossing two coins, the number of all possible outcomes is, (Easy)
A) 2 B) 3 C) 4 D) 5
5. A die is thrown once. The number of all possible outcomes is, (Average)
A) 12 B) 24 C) 36 D) 6
6. Which of the following cannot be the probability of an event? (Easy)
A) $\frac{2}{3}$ B) -1.5 C) 15% D) 0.7
7. Which of the following can be the probability of an event? (May-2025 Easy)
A) $\frac{1}{5}$ B) 1.5 C) $\frac{5}{2}$ D) -5

8. A die numbered from 1 to 6 is thrown once. The probability of getting an odd number on the top is, [April-2016, Average]

- A) $\frac{3}{6}$ B) $\frac{1}{6}$ C) $\frac{2}{6}$ D) $\frac{4}{6}$

9. The probability of an event 'E' is 0.05, then the probability of 'not E' is, [March – 2019 Average]

- A) 0.59 B) 0.95 C) 1 D) 1.05

10. The letters of English alphabet are written on cards without any repetition and are put inside a box. A card is randomly drawn from the box. The probability of getting a vowel is, [Average]

- A) $\frac{3}{26}$ B) $\frac{5}{26}$ C) $\frac{1}{26}$ D) $\frac{21}{26}$

11. If the probability of an event 'E' $P(E) = 0.75$ then the value of $P(\bar{E})$ is, [March-2023 Average]

- A) 2.5 B) 0.25 C) 0.025 D) 0.75

12. A die is thrown twice. The number of all possible outcomes is, [Average]

- A) 12 B) 24 C) 36 D) 6

13. The probability of winning a game is $\frac{3}{4}$, then the probability of losing the same game is, [Sept-2023, Average]

- A) $\frac{1}{2}$ B) $\frac{3}{4}$ C) $\frac{1}{4}$ D) $\frac{1}{3}$

14. The probability of getting a square number of the top when the die is thrown once is, [Average]

- A) $\frac{2}{6}$ B) $\frac{6}{8}$ C) $\frac{5}{8}$ D) $\frac{8}{5}$

15. There are 28 bulbs in a box. 7 bulbs are defective among them. The probability of getting a non-defective bulb when a bulb is drawn randomly from the box is, [Difficult]

- A) $\frac{7}{28}$ B) $\frac{21}{28}$ C) $\frac{27}{28}$ D) $\frac{28}{7}$

16. There are 3 red, 4 white and 5 blue balls. A ball is drawn at random from the bag. The probability of getting a white ball is, [Average]

- A) $\frac{3}{9}$ B) $\frac{4}{8}$ C) $\frac{4}{12}$ D) $\frac{8}{12}$

17. A and B are two friends. The probability that their birthday falls on the same day is, [Difficult]

- A) $\frac{364}{365}$ B) $\frac{1}{365}$ C) 1 D) 0

18. If $P(E)$ is the probability of an event then the correct statement is, [Easy]

- A) $0 < P(E) < 1$ B) $0 \leq P(E) \leq 1$
C) $0 \leq P(E) < 1$ D) $0 < P(E) \leq 1$

19. Two dice are thrown simultaneously. The probability that the sum of the numbers appearing on the top of the faces is greater than 12 is, [Difficult]
 A) $\frac{6}{36}$ B) $\frac{1}{36}$ C) 1 D) 0
20. A die is rolled once. The probability of getting an even number on the top is, [Average]
 A) $\frac{1}{6}$ B) $\frac{1}{3}$ C) 0.5 D) $\frac{6}{5}$
21. A die is rolled once. The probability of getting a prime number on the top is, [Average]
 A) $\frac{1}{2}$ B) $\frac{1}{3}$ C) $\frac{1}{4}$ D) $\frac{2}{3}$
22. The probability of winning a game is 0.3, then the probability of losing the same game is, [Model QP-2017, Average]
 A) 0.1 B) 0.3 C) 0.7 D) 1.3
23. The sum of all the elementary events of a random experiment is, [Model QP 2024, Preparatory QP 2025, Model QP-2025, May-2025, Easy]
 A) 0 B) $\frac{1}{2}$ C) 1 D) -1
24. If the probability of a student scoring 100% in Mathematics examination is $\frac{4}{5}$, then the probability of the student not scoring 100% in the same subject is, [Average]
 A) $\frac{1}{5}$ B) $\frac{2}{5}$ C) $\frac{1}{4}$ D) $\frac{2}{3}$
25. The possible outcome of a random experiment is either win or loss. If the probability of winning is twice the probability of losing, then the probability of winning in the experiment is, [Difficult]
 A) $\frac{1}{3}$ B) $\frac{2}{3}$ C) 1 D) 2
26. The probability of getting 53 Fridays or 53 Saturdays in a leap year is, [Difficult]
 A) $\frac{1}{3}$ B) $\frac{2}{3}$ C) $\frac{3}{7}$ D) 1

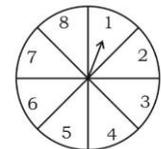
II. Answer the following questions. (1 Mark)

27. Find the probability of selecting a vowel from the word 'TRIANGLE' [Average]
28. Write the value of $P(E) + P(\overline{E})$ with reference to probability. [Model QP-2025, Easy]
29. If $P(E) = 0.05$, then find $P(\overline{E})$. [March-2019, Easy]
30. If the probability of raining at a specific time on a day is 0.75, then what is the probability of not raining on the same time? [Model QP-2023, Average]
31. If $P(A) = \frac{2}{3}$, then find the value of $P(\overline{A})$ [Sept-2020, Average]
32. If the probability of an event 'B' is $P(B) = 0.65$ then find the value of $P(\overline{B})$ [Average]

33. Find the probability of getting the number 6 on the top, when a die is thrown once. [Easy]
34. A fair coin is tossed once. Find the probability of getting a head. [April-2017, Easy]
35. If the probability of winning a game is 0.8, then find the probability of losing the same game. [March-2019, Easy]
36. If $P(A) = 80\%$ then prove that the probability of not 'A' is $\frac{1}{5}$. [Model QP-2024, Difficult]
37. A fair coin is tossed twice. What is the number of all possible outcomes? [Easy]

III. Answer the following questions. (2 Marks)

38. A coin is tossed once. Find the probability of getting i) one head only ii) at least one head on the top. [Difficult]
39. Find the probability of getting a number between 2 and 6, when a die is rolled once. [Average]
40. Two dice are rolled simultaneously. Find the probability that the sum of the two numbers on the top is 5. (Average)
41. A die numbered from 1 to 6 is rolled twice. Find the probability that the sum of the two numbers on the top is 10. [April-2019, Average]
42. Two numbered from 1 to 6 are rolled once. Find the probability that the sum of the two numbers on the top is more than 7. [Average]
43. The probability of an event 'A' is $P(A)$ and $P(A) : P(\overline{A}) = 1:2$. Find the value of $P(\overline{A})$ [Difficult]
44. A game of chance consists of spinning an arrow which comes to rest pointing at one of the numbers 1, 2, 3, 4, 5, 6, 7, 8 and these are equally likely outcomes. Find the probability that it will point at an even number. [Sept-2020, Average]
45. A box contains cards numbered from 2 to 25 and is well-shuffled. A card is drawn at random. Find the probability that the card drawn is i) an even number ii) a perfect square. [Average]
46. A bag contains 6 red, 5 blue and 4 green balls. A ball is drawn at random from the bag. Find the probability that the ball drawn is i) not green ii) red [Average]
47. There are 36 mangoes in a basket. $\frac{1}{4}$ th of the mangoes are rotten and others are good. Find the probability of getting a good mango when one mango is drawn randomly from the basket. [April 2024 , Average]



48. 'A' is a random experiment. If $P(A) : P(\overline{A}) = 5 : 11$, then find $P(A)$ and $P(\overline{A})$
[Average]
49. There are 500 watches in a box. 50 watches among them are defective. A watch is drawn at random from the box. Find the probability that the watch drawn is defective.
[April-2018, Easy]
50. A die whose faces are numbered from 1 to 6 is rolled once. Find the probability of getting a prime number or the multiple of 5 on the top. [Average]
51. Two dice whose faces are numbered from 1 to 6 are rolled once. Find the probability that the sum of the numbers on their top is 6. [June 2018:Average]
52. A fair coin is tossed twice. Find the probability of getting i) two heads ii) tail in particular
[March-2019:Average]
53. A die whose faces are numbered from 1 to 6 is rolled once. Find the probability of getting a) an even number b) a perfect square number [April 2020:Average]
54. The faces of a die are marked with letters A, B, C, D, E, I from English alphabet. Find the probability of getting a vowel on the top when the die is rolled once. [September 2020:Average]
55. There are 6 blue and some red marbles in a box. The probability of drawing a blue marble is $\frac{3}{8}$. Find the number of red marbles in the box and also find the probability of taking out a red marble. [May 2025:Difficult]
56. The six faces of a die show the given numbers: 1, 2, 3, 4, 1, 5. This die is rolled once. Find the probability of getting a perfect square number. [May 2025:Average]
57. There are 20 discs in a box which are numbered from 1 to 20. Find the probability of getting a perfect cube number when a disc is drawn at random from the box. [Average]

IV. Answer the following questions. (3 Marks)

58. When a die is rolled once, find the probability of getting a number on the top that is i) greater than 2 ii) less than or equal to 2 iii) not greater than 2 [Average]
59. Two coins are tossed simultaneously. Find the probability of getting a) at least one head b) both heads c) no head
[Average]
60. A bag contains cards numbered from 5 to 30. A card is drawn at random from the bag. Find the probability that the card drawn is a) a multiple of 2 and 3 b) a square number c) a multiple of 3
[Average]
61. There are 3 red balls, 5 white balls and 8 blue balls. A ball is drawn at random from the bag. Find the probability that the ball drawn is a) a red ball b) not a white ball [April-2020, Average]
62. A box contains 20 cards numbered from 1 to 20. One card is drawn randomly from the box. Find the probability of getting a card bearing i) a perfect square number ii) a number which is divisible by both 2 and 3. [March-2025:Difficult]
63. A bag contains white, black and red balls only. A ball is taken out at random from the bag. The probability of taking out white ball is $\frac{3}{10}$ and the probability of taking out black ball is

$\frac{2}{5}$. Find the probability of taking out the red ball. If the bag contains 20 black balls, find the total number of balls in the bag. [Difficult]

64. The following table shows the marks obtained by 50 students for 100 marks.

Marks	0-34	35-50	51-70	71-90	91-100
Number of students	8	9	14	11	8

Find the probability of a student scoring i) less than 34 ii) between 71-90 iii) more than 90 [Average]

MODEL ANSWERS

UNIT:1 REAL NUMBERS

I. Multiple Choice Questions

1. B) irrational number
2. A) irrational number
3. A) 5
4. C) $\sqrt{9}$
5. B) $\sqrt{4}$
6. A) irrational number
7. B) composite number
8. B) 13,7
9. C) 4
10. C) Prime numbers
11. D) $2^3 \times 3^1 \times 5^1$
12. A) 2,3,5
13. D) 6
14. A) 1
15. B) 1
16. C) 1 A) 60
17. B) $a \times b$
18. B) 2
19. (C) $(a \times b)$
20. (A) 60
21. (A) 2×5
22. B) $x y^2$
23. (C) 4
24. (B) 1
25. B) 2
26. C) 300
27. C) $6p$
28. B) 1000.

II. ONE MARKS QUESTIONS

- 29). $2 \mid 140$
 $2 \mid 70$
 $5 \mid 35$
 $7 \mid 7$

$$140 = 2 \times 2 \times 5 \times 7 = 2^2 \times 5 \times 7$$

30. Every composite number can be expressed as a product of primes and this factorization is unique except for the order in which the prime factors occur.

$$31. H \times L = A \times B$$

$$L = \frac{(A \times B)}{H}$$
$$= \frac{24 \times 36}{12}$$

$$LCM = 72$$

$$32. 2 | 96$$

$$2 | 48$$

$$2 | 24$$

$$2 | 12$$

$$2 | 6$$

$$3 | 3$$

$$96 = 2^5 \times 3$$

$$33. 156 = 2^2 \times 3 \times 13$$

$$34. 2 | 200$$

$$2 | 100$$

$$2 | 50$$

$$5 | 25$$

$$5 | 5$$

$$200 = 2^m \times 5^n$$

$$200 = 2^3 \times 5^2$$

$$m = 3, n = 2$$

$$35. 2 | 24$$

$$2 | 12$$

$$2 | 6$$

$$3 | 3$$

$$| 1$$

$$24 = 2^3 \times 3,$$

$$2 | 36$$

$$2 | 18$$

$$3 | 9$$

$$3 | 3$$

$$| 1$$

$$24 = 2^3 \times 3, \quad 36 = 2^2 \times 3$$

$$\therefore \text{HCF}(24, 36) = 12$$

$$36. 21$$

$$37. x = 2 \text{ \& } y = 5, \text{ Therefore } x + y = 7$$

III. TWO MARKS QUESTIONS:

38 $H \times L = A \times B$

$$L = \frac{(A \times B)}{H}$$
$$= \frac{306 \times 657}{9}$$

$$\text{LCM} = 22338$$

39 $7 \times 11 \times 13 + 13$

$$= 13(7 \times 11 + 1)$$

$$= 13 \times 78$$

$\therefore 7 \times 11 \times 13 + 13$ is composite number

40. $H \times L = A \times B$

$$H = (A \times B) / L$$

$$= (91 \times 26) / 182$$

$$= 2366 / 182$$

$$\text{HCF} = 13$$

41. A Number which can be expressed as two or more its factors is know as composite number .
composite number $24 = 2 \times 2 \times 2 \times 3$

42.

$$2 \mid 438$$

$$3 \mid 219$$

$$73 \mid 73$$

$$438 = 2 \times 3 \times 73$$

$$2 \mid 606$$

$$3 \mid 303$$

$$101 \mid 101$$

$$606 = 2 \times 3 \times 101$$

$$\text{HCF} = 2 \times 3 = 6$$

43. Let as assume, $\sqrt{3} + 5$ is a rational numbers

$$\sqrt{3} + 5 = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$\sqrt{3} = \frac{a}{b} - 5$$

$$\sqrt{3} = \frac{a-5b}{b}$$

$\sqrt{3}$ is a rational number ,

$$\frac{a-5b}{b} \text{ is a rational}$$

but $\sqrt{3}$ is not a rational number

this gives as contraduction

our assumption that $5 + \sqrt{3}$ is a rational number is wrong

$\sqrt{3} + 5$ is an irrational number

44. Let us assume $\sqrt{5} - 7$ is a rational number

$$\sqrt{5} - 7 = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$\sqrt{5} = \frac{a}{b} + 7$$

$$\sqrt{5} = \frac{a+7b}{b}$$

$\sqrt{5}$ is a rational number $= \frac{a+7b}{b}$ is rational. but $\sqrt{5}$ is not a rational number

our assumption that $\sqrt{5} - 7$ is a rational number is wrong

$\sqrt{5} - 7$ is an irrational number

45. Let us assume $2 + \sqrt{5}$ is a rational number

$$2 + \sqrt{5} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$\sqrt{5} = \frac{a}{b} - 2$$

$$\sqrt{5} = \frac{a-2b}{b}$$

$\sqrt{5}$ is a rational number $= \frac{a-2b}{b}$ is rational but $\sqrt{5}$ is not a rational number

our assumption that $2 + \sqrt{5}$ is a rational number is wrong

$2 + \sqrt{5}$ is an irrational number

46. Let us assume $6 + \sqrt{2}$ is a rational number

$$6 + \sqrt{2} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$\sqrt{2} = \frac{a}{b} - 6$$

$$\sqrt{2} = \frac{a-6b}{b}$$

$\sqrt{2}$ is a rational number $= \frac{a-6b}{b}$ is rational but $\sqrt{2}$ is not a rational number

our assumption that $6 + \sqrt{2}$ is a rational number is wrong

$6 + \sqrt{2}$ is an irrational number

47. Let us assume $5 - \sqrt{3}$ is a rational number

$$5 - \sqrt{3} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$\sqrt{3} = 5 - \frac{a}{b}$$

$$\sqrt{3} = \frac{5b-a}{b}$$

$\sqrt{3}$ is a rational number $= \frac{5b-a}{b}$ is rational but $\sqrt{3}$ is not a rational number

our assumption that $5 - \sqrt{3}$ is a rational number is wrong

$5 - \sqrt{3}$ is an irrational number

48. Let us assume $3 + 2\sqrt{5}$ is a rational number

$$3 + 2\sqrt{5} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$2\sqrt{5} = \frac{a}{b} - 3$$

$$\sqrt{5} = \frac{a-3b}{2b}$$

$\sqrt{5}$ is a rational number $= \frac{a-3b}{2b}$ is rational but $\sqrt{5}$ is not a rational number

our assumption that $3 + 2\sqrt{5}$ is a rational number is wrong

$3 + 2\sqrt{5}$ is an irrational number

49. Let us assume $2\sqrt{3} - 4$ is a rational number

$$2\sqrt{3} - 4 = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$2\sqrt{3} = \frac{a}{b} + 4$$

$$\sqrt{3} = \frac{a+4b}{2b}$$

$\sqrt{3}$ is a rational number $\frac{a+4b}{2b}$ is rational but $\sqrt{3}$ is not a rational number

our assumption that $2\sqrt{3} - 4$ is a rational number is wrong

$2\sqrt{3} - 4$ is an irrational number

50. . They meet again at the time by their value of the LCM

$$18 = 2 \times 3 \times 3 = 2 \times 3^2$$

$$12 = 2 \times 2 \times 3 = 2^2 \times 3$$

$$\text{LCM } L = 2^2 \times 3^2 = 36$$

$$\text{LCM } L = 4 \times 9 = 36$$

Therefore, They meet again after 36 minutes at the initial point

51. $2|40$

$$2|20$$

$$2|10$$

$$5|5$$

$$|1$$

$$\therefore x = 2, y = 3 \text{ \& } z = 5$$

52. $3|147$

$$7|49$$

$$7|7$$

$$|1$$

$$147 = 3 \times 7^2$$

$$2|56$$

$$2|28$$

$$2|14$$

$$7|7$$

$$|1$$

$$56 = 2^3 \times 7 \quad \text{HCF}(147, 56) \text{ is } 7$$

Maximum length of the rod = 7m. This rod is to use 21 times to measure the field

53. $2|420$

$$2|210$$

$$3|105$$

$$5|35$$

$$7|7$$

$$|1$$

$$420 = 2^2 \times 3 \times 5 \times 7$$

$$\begin{array}{r} 2|130 \\ 5|65 \\ 13|13 \\ |1 \end{array}$$

$$130 = 2 \times 5 \times 13$$

$$\text{HCF}(420, 130) = 10$$

No. of barfis in each stack = 10

IV. THREE MARKS QUESTIONS

54. Let us assume that $\sqrt{2}$ is a rational number

$$\sqrt{2} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$2 = \frac{a^2}{b^2}$$

$$2b^2 = a^2$$

a^2 divisible by 2, then a is also divisible by 2

'a' have 2 as common factor

We can write up $a = 2k$

$$a^2 = 4k^2$$

$$2b^2 = 4k^2$$

$$b^2 = 2k^2$$

b^2 divisible by 2 then b is also divisible by 2

'b' have 2 as common factor

a and b have at least 2 as a common factor

but this contradicts the fact that a and b are co-prime

this contradiction has arisen because of our incorrect assumption that $\sqrt{2}$

$\sqrt{2}$ is a rational number

55. Let us assume that $\sqrt{3}$ is a rational number

$$\sqrt{3} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$3 = \frac{a^2}{b^2}$$

$$3b^2 = a^2$$

a^2 divisible by 3, then a is also divisible by 3

'a' have 3 as common factor

We can write up $a = 3k$

$$a^2 = 9k^2$$

$$3b^2 = 9k^2$$

$$b^2 = 3k^2$$

b^2 divisible by 3 then b is also divisible by 3

'b' have 3 as common factor

a and b have at least 3 as a common factor

but this contradicts the fact that a and b are co-prime

this contradiction has arisen because of our incorrect assumption that $\sqrt{3}$

$\sqrt{3}$ is a rational number

56. Let us assume that $\sqrt{5}$ is a rational number

$$\sqrt{5} = \frac{a}{b} \quad (\text{a and b are co-prime, } b \neq 0)$$

$$5 = \frac{a^2}{b^2}$$

$$5b^2 = a^2$$

a^2 divisible by 5, then a is also divisible by 5

' a ' have 5 as common factor

We can write up $a = 5k$

$$a^2 = 25k^2$$

$$5b^2 = 25k^2$$

$$b^2 = 5k^2$$

b^2 divisible by 5 then b is also divisible by 5

' b ' have 5 as common factor

a and b have at least 5 as a common factor

but this contradicts the fact that a and b are co-prime

this contradiction has arisen because of our incorrect assumption that $\sqrt{5}$

$\sqrt{5}$ is a irrational number

57.

2	510
3	255
5	85
17	17
	1

$$510 = 2 \times 3 \times 5 \times 17$$

2	92
2	46
23	23
	1

$$92 = 2 \times 2 \times 23$$

$$\text{HCF of } (510, 92) = 2$$

$$\text{LCM of } (510, 92) = 2^2 \times 3 \times 5 \times 17 \times 23$$

$$\text{LCM} = 23460$$

$$H \times L = A \times B$$

$$2 \times 23460 = 510 \times 92$$

$$46920 = 46920$$

$$\text{LCM} \times \text{HCF} = \text{Product of two integers}$$

$$58. \quad 336 = 2 \times 2 \times 2 \times 2 \times 3 \times 7$$

$$54 = 2 \times 3 \times 3 \times 3$$

$$\text{LCM of } (336, 54) = 2 \times 3 \times 2 \times 2 \times 2 \times 7 \times 3 \times 3 = 3024$$

$$\text{HCF of } (336, 54) = 2 \times 3 = 6$$

$$\text{LCM} \times \text{HCF} = A \times B$$

$$336 \times 54 = 3024 \times 6$$

$$18144 = 18144$$

$$\text{LHS} = \text{RHS}$$

$$59. \quad 26 = 2 \times 13$$

$$91 = 7 \times 13$$

$$\text{HCF of } (26, 91) = 13$$

$$\text{LCM of } (26, 91) = 2 \times 7 \times 13 = 182$$

$$\text{HCF} \times \text{LCM} = A \times B$$

$$13 \times 182 = 26 \times 91$$

$$2366 = 2366$$

$$\text{LHS} = \text{RHS}$$

60.

3	135
3	45
3	15
5	5
	1

$$510 = 3 \times 3 \times 3 \times 5$$

3	75
5	25
5	5
	1

$$75 = 3 \times 5 \times 5$$

2	20
2	10
5	5
	1

$$20 = 2 \times 2 \times 5$$

$$\text{HCF of } (135, 75) = 15$$

$$\text{LCM of } (15, 20) = 2 \times 2 \times 5 \times 3 \times 5$$

$$\text{LCM} = 60$$

61. 12, and 21

$$12 = 2 \times 2 \times 3$$

$$15 = 3 \times 5$$

$$21 = 3 \times 7$$

$$\text{HCF of } (12, 15, 21) = 3$$

$$\text{LCM of } (12, 15, 21) = 3 \times 2 \times 2 \times 5 \times 7 = 420$$

62. $6 = 2 \times 3$

$$72 = 2 \times 2 \times 2 \times 3 \times 3$$

$$120 = 2 \times 2 \times 2 \times 3 \times 5$$

$$\text{HCF of } (6, 72, 120) = 3 \times 2 = 6$$

$$\text{LCM of } (6, 72, 120) = 2^2 \times 3^2 \times 5 = 360$$

63. $2|616$

$$2|308$$

$$2|154$$

$$7|77$$

$$11|11$$

$$|1$$

$$616 = 2^3 \times 7 \times 11$$

$$2|32$$

$$2|16$$

$$2|8$$

$$2|4$$

$$2|2$$

$$|1$$

$$32 = 2^5$$

$$\text{HCF } (616, 32) = 8$$

Maximum number of column in which they march = 8

Unit : 02 POLINOMIALS

I. Multiple choice questions :

- 1) A) 3
- 2) B) 1
- 3) C) 3
- 4) D) 2
- 5) C) 3
- 6) C) 2
- 7) A) 20
- 8) B) 3
- 9) B) 3
- 10) C) 3
- 11) C) 4
- 12) A) $x^2 + 2x + 8$
- 13) C) 2
- 14) C) -2 and -4
- 15) C) $\frac{c}{a}$
- 16) B) $\frac{-b}{a}$
- 17) A) 2
- 18) B) $\frac{-2}{3}$
- 19) D) $p(x) = x^2 - 4x + 5$
- 20) B) 2
- 21) D) -3 and 2

II. ONE MARKS QUESTIONS:

- 22) 3
- 23) 4
- 24) 3
- 25) 4
- 26) 3
- 27) 3
- 28) 4
- 29) 3
- 30) 4
- 31) 5
- 32) Product of zeros = $\frac{10}{2} = 5$
- 33) 7
- 34) 6
- 35) $x^2 + 3x + 2$
- 36) $p(x) = x^2 - 3$,
 $P(x) = 0$, $x = -\sqrt{3}$ & $x = +\sqrt{3}$
- 37) $P(x) = 0$,
 $x^2 - 25 = 0$
 $x^2 = 25$
 $x = -5$ & $x = +5$
- 38) $P(1) = 2(1)^3 + 3(1)^2 - 11(1) + 6$
 $= 2 + 3 - 11 + 6$
 $= 0$
- 39) C) -2 and -4

III. TWO MARKS QUESTIONS:

- 40) Linear polynomials = $bx + c$
 Quadratic polynomials = $ax^2 + bx + c$

41) $p(x) = 6x^2 - 7x - 3$
 $p(x) = 6x^2 - 9x + 2x - 3$
 $p(x) = 3x(2x - 3) + 1(2x - 3)$
 $p(x) = (2x - 3)(3x + 1)$
 $2x - 3 = 0$ or $3x + 1 = 0$
 $x = \frac{3}{2}$ or $x = \frac{-1}{3}$

$$\begin{array}{l} -18x^2 \swarrow \begin{array}{l} -9x \\ +2x \\ \hline -7x \end{array} \end{array}$$

42) $p(x) = 4x^2 - 4x - 3$
 $p(x) = 4x^2 - 6x + 2x - 3$
 $p(x) = 2x(2x - 3) + 1(2x - 3)$
 $p(x) = (2x - 3)(2x + 1)$
 $2x - 3 = 0$ or $2x + 1 = 0$
 $x = \frac{3}{2}$ or $x = \frac{-1}{2}$

$$\begin{array}{l} -12x^2 \swarrow \begin{array}{l} -6x \\ +2x \\ \hline -4x \end{array} \end{array}$$

43) $\alpha + \beta = \frac{-b}{a} = \frac{-3}{1} \rightarrow b = 3a \rightarrow (1)$
 $\alpha \times \beta = \frac{c}{a} = \frac{2}{1} = 2 \rightarrow c = 2a \rightarrow (2)$
 add (1) and (2)
 $b + c = 5a$

44) Sum of polynomials = $\alpha + \beta = \frac{-b}{a} = \frac{-12}{3} = 4$
 Product of polynomials = $\alpha \times \beta = \frac{c}{a} = \frac{-15}{3} = 5$
 $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2(\alpha \times \beta)$
 $= 4^2 - 2(5)$
 $= 16 - 10 = 6$

45) $P(x) = x^2 + 3x + 1$
 Sum of polynomials = $\alpha + \beta = \frac{-b}{a} = -3$
 Product of polynomials = $\alpha \times \beta = \frac{c}{a} = 1$
 $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha \times \beta} = \frac{-3}{1} = -3$

46) $P(x) = x^2 + 3x + 1$
 $a=1, b=3, c=1$
 Sum of polynomials = $\alpha + \beta = \frac{-b}{a} = -3$
 Product of polynomials = $\alpha \times \beta = \frac{c}{a} = 1$
 $\alpha^2\beta + \beta^2\alpha = \alpha\beta(\alpha + \beta) = 1(-3) = -3$

47) $P(x) = 2x^2 - 6x + k$
 α and β are zeros of $P(x)$,
 From data $\beta = 2\alpha$
 Sum of polynomials = $\alpha + \beta = \frac{-b}{a}$
 $\alpha + 2\alpha = \frac{-(-6)}{1}$
 $3\alpha = 6$
 $\alpha = 2$

$$\text{Product of polynomials} = \alpha \times \beta = \frac{c}{a}$$

$$\begin{aligned} \alpha (2\alpha) &= \frac{k}{1} \\ 2\alpha^2 &= k \\ 2(2)^2 &= k \\ \therefore K &= 8 \end{aligned}$$

48) $P(x) = ax^2 + bx - 4$

$$\text{Sum of polynomials} = \alpha + \beta = \frac{-b}{a} = \frac{1}{4}$$

$$\text{Product of polynomials} = \alpha \times \beta = \frac{c}{a} = -1 \quad c = -4$$

$$\therefore \text{Product of polynomials} = \frac{-4}{a} = -1$$

$$a = 4$$

$$\text{Sum of polynomials} = \frac{-b}{a} = \frac{1}{4}$$

$$= \frac{-b}{4} = \frac{1}{4}$$

$$b = -1$$

49) $p(x) = x^2 - 5x + 6$

$$p(x) = x^2 - 6x + x - 6$$

$$p(x) = x(x - 6) + 1(x - 6)$$

$$p(x) = (x - 6)(x + 1)$$

$$x - 6 = 0 \text{ and } x + 1 = 0$$

$$x = 6 \text{ and } x = -1$$

50) $\alpha = \sqrt{3} \quad \beta = -\sqrt{3}$

$$\alpha + \beta = \sqrt{3} + (-\sqrt{3}) = \sqrt{3} - \sqrt{3} = 0$$

$$\alpha \times \beta = \sqrt{3} (-\sqrt{3}) = -\sqrt{9} = -3$$

$$p(x) = x^2 - 0x - 3$$

$$p(x) = x^2 - 3$$

IV. THREE MARKS QUESTIONS:

51) $p(x) = x^2 - 2x - 8$

$$p(x) = x^2 - 4x + 2x - 8$$

$$p(x) = x(x - 4) + 2(x - 4)$$

$$p(x) = (x - 4)(x + 2)$$

$$x - 4 = 0 \text{ and } x + 2 = 0$$

$$x = 4 \text{ and } x = -2$$

$$\text{Sum of polynomials} = \alpha + \beta = \frac{-b}{a} = -(-2) = 2$$

$$(4) + (-2) = 2$$

$$\text{Product of polynomials} = \alpha \times \beta = \frac{c}{a} = -8$$

$$(4)(-2) = -8$$

52) $p(x) = x^2 + 7x + 10$

$$p(x) = x^2 + 5x + 2x + 10$$

$$p(x) = x(x + 5) + 2(x + 5)$$

$$p(x) = (x + 5)(x + 2)$$

$$x + 5 = 0 \text{ and } x + 2 = 0$$

$$x = -5 \text{ and } x = -2$$

$$\text{Sum of polynomials} = \alpha + \beta = \frac{-b}{a} = -7$$

$$\begin{array}{r} +10x^2 \\ \swarrow \quad \searrow \\ +5x \quad +2x \\ \hline +7x \end{array}$$

$$\begin{aligned} (-5) + (-2) &= -7 \\ \text{Product of polynomials} &= \alpha \times \beta = \frac{c}{a} = 10 \\ (-5)(-2) &= 10 \end{aligned}$$

53) Sum of polynomials $= \alpha + \beta = \frac{-b}{a} = -3$
 Product of polynomials $= \alpha \times \beta = \frac{c}{a} = 2$
 expected polynomial $p(x) = x^2 - (\alpha + \beta)x + \alpha \beta$
 $p(x) = x^2 - (-3)x + 2$
 $p(x) = x^2 + 3x + 2$
 $p(x) = 0$
 $x^2 + 3x + 2 = 0$
 $x^2 + 2x + x + 2 = 0$
 $x(x + 2) + 1(x + 2) = 0$
 $(x + 1)(x + 2) = 0$
 $x + 1 = 0$ and $x + 2 = 0$
 $x = -1$ and $x = -2$
 \therefore zeros $\alpha = -1$ and $\beta = -2$

54) Sum of polynomials $= \alpha + \beta = \frac{-b}{a} = -7$
 Product of polynomials $= \alpha \times \beta = \frac{c}{a} = 12$
 Expected polynomial $p(x) = x^2 - (\alpha + \beta)x + \alpha \beta$
 $p(x) = x^2 - (7)x + 12$
 $p(x) = x^2 - 7x + 12$
 zeros of polynomials $p(x) = 0$
 $x^2 - 7x + 12 = 0$
 $x^2 - 4x - 3x + 12 = 0$
 $x(x - 4) - 3(x - 4) = 0$
 $(x - 4)(x - 3) = 0$
 $x - 4 = 0$ and $x - 3 = 0$
 $x = 4$ and $x = 3$
 \therefore zeros $\alpha = 4$ and $\beta = 3$

V. FOUR MARKS QUESTIONS:

55) $\alpha = -1$ $\beta = 4$
 $\alpha + \beta = -1 + 4 = 3$
 $\alpha \times \beta = (-1) \times 4 = -4$
 $p(x) = x^2 - 3x - 4$
 zeros of polynomials $p(x) = 0$
 $x^2 - 4x + x - 4 = 0$
 $x(x - 4) + 1(x - 4) = 0$
 $(x + 1)(x - 4) = 0$
 $x + 1 = 0$ and $x - 4 = 0$
 $x = -1$ and $x = 4$

VI. FIVE MARKS QUESTIONS:

56) $\alpha = -1$ $\beta = 4$
 $\alpha + \beta = -1 + 4 = 3$
 $\alpha \times \beta = (-1) \times 4 = -4$
 $p(x) = x^2 - 3x - 4$
 zeros of polynomials $p(x) = 0$

$$\begin{aligned}
 x^2 - 4x + x - 4 &= 0 \\
 x(x - 4) + 1(x - 4) &= 0 \\
 (x + 1)(x - 4) &= 0 \\
 x + 1 = 0 \text{ and } x - 4 &= 0 \\
 x = -1 \text{ and } x &= 4
 \end{aligned}$$

Unit : 03 PAIR OF LINEAR EQUATIONS WITH TWO VARIABLES

I. Multiple Choice Questions :

- 1) A) $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$
- 2) A) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$
- 3) B) equations have unique solution
- 4) A) $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$
- 5) D) Co-incident lines
- 6) C) Parallel lines
- 7) C) A unique solution
- 8) A) Intersecting lines
- 9) B) parallel lines
- 10) B) parallel lines
- 11) B) Parallel lines
- 12) C) 6
- 13) B) $\frac{15}{4}$
- 14) B) $2x+3y=9$
 $4x+6y=18$
- 15) B) If the lines are perpendicular to each other, there is no solution
- 16) A) $x=5, y=2$

II. One mark questions

- 17) $a_1x+b_1y+c_1=0$ and $a_2x+b_2y+c_2=0$
- 18) No solution
- 19) unique solution
- 20) Many solutions
- 21) $2(1+b)$
- 22) $(2x+1) + y$
- 23) $a=3, b=6$
- 24) $p=4$
- 25) Equations have unique solution
- 26) Co-incident lines
- 27) One solution
- 28) One solution
- 29) One solution

III. Two mark questions

30) $2x+y=10,$
 $x - y= 2$

$$3x = 12$$

$$x=4$$

substitute the value of x in equation (1)

$$2x+y=10$$

$$2(4)+y=10$$

$$8+y=10$$

$$y=10 - 8$$

$$y= 2$$

31) $3x-y=15,$
 $2x-y=5$

$$5x=20$$

$$x=4$$

substitute the value of x in equation (1)

$$3x+y=15$$

$$3(4)+y=15$$

$$12+y=15$$

$$y=15-12$$

$$y=3$$

32) $2x+y=8$
 $x-y=1$

$$3x=9$$

$$x=3$$

substitute the value of x in equation (1)

$$2x+y=8$$

$$2(3)+y=8$$

$$6+y=8$$

$$y=8-6$$

$$y=2$$

$$y=1$$

33) $x+y=14$ -----(1)
 $x-y= 4$ -----(2)

$$x+y=14$$

$$y=14 - x$$

substitute the value of y in equation (2)

$$x-y= 4$$

$$x- (14- x) = 4$$

$$\begin{aligned}
 x - 14 + x &= 4 \\
 2x &= 4 + 14 \\
 2x &= 18 \\
 x &= 9
 \end{aligned}$$

substitute the value of x in equation (1)

$$\begin{aligned}
 x + y &= 14 \\
 9 + y &= 14 \\
 y &= 14 - 9 \\
 y &= 5
 \end{aligned}$$

34) $x + 2y = 8$ -----(1)
 $x - y = -1$ -----(2)

$$\begin{aligned}
 x + 2y &= 8 \\
 x &= 8 - 2y
 \end{aligned}$$

substitute the value of x in equation (2)

$$\begin{aligned}
 x - y &= -1 \\
 (8 - 2y) - y &= -1 \\
 8 - 2y - y &= -1 \\
 8 - 3y &= -1 \\
 -3y &= -1 - 8 \\
 -3y &= -9 \\
 y &= 3
 \end{aligned}$$

substitute the value of y in equation (1)

$$\begin{aligned}
 x + 2y &= 8 \\
 x + 2(3) &= 8 \\
 x + 6 &= 8 \\
 x &= 8 - 6 \\
 x &= 2
 \end{aligned}$$

35) $2x + y = 8$
 $3x - y = 7$

 $5x = 15$
 $x = 3$

substitute the value of x in equation (1)

$$\begin{aligned}
 2x + y &= 8 \\
 2(3) + y &= 8 \\
 6 + y &= 8 \\
 y &= 8 - 6 \\
 y &= 2
 \end{aligned}$$

36) Let the numbers be x & y

$$\begin{aligned}
 x + y &= 10 \\
 x - y &= 2
 \end{aligned}$$

 $2x = 12$
 $x = 6$

substitute the value of x in equation (1)

$$\begin{aligned}
 x + y &= 10 \\
 6 + y &= 10
 \end{aligned}$$

$$y = 10 - 6$$

$$y = 4$$

- 37) Let the numbers be x & y

$$x + y = 15 \quad \& \quad x + 1 = y$$

$$x + y = 15$$

$$x - y = -1$$

$$2x = 14$$

$$x = 7$$

substitute the value of x in equation (1)

$$x + y = 15$$

$$7 + y = 15$$

$$y = 15 - 7$$

$$y = 8$$

- 38) Multiply eqn (1) by 1 and eqn (2) by 2

$$(3x + 2y = 5) \quad 1$$

$$(x - y = 1) \quad 2$$

$$3x + 2y = 5$$

$$2x - 2y = 2$$

$$5x = 7$$

$$x = 7/5$$

$$x = 7/5$$

$$(3x + 2y = 5) \quad 1$$

$$(x - y = 1) \quad 3$$

$$3x + 2y = 5$$

$$3x - 3y = 3$$

$$5y = 2$$

$$y = 2/5$$

- 39) Multiply eqn (1) by 5 and eqn (2) by 2

$$(2x + 5y = 7) \quad 5$$

$$(5x + 2y = 7) \quad 2$$

$$10x + 25y = 35$$

$$10x + 4y = 14$$

$$(-) \quad (-) \quad (-)$$

$$21x = 21$$

$$x = 1$$

substitute the value of x in equation (1)

$$2x + 5y = 7$$

$$2(1) + 5y = 7$$

$$2 + 5y = 7$$

$$5y = 7 - 2$$

$$5y = 5$$

$$y = 1$$

IV. Three mark questions

40) Let the fraction be x/y

According to the equation

$$\frac{x+3}{y+2} = \frac{9}{11}$$

$$11x+22 = 9y+18$$

$$11x - 9y = -4 \quad \text{----- (1)}$$

$$\frac{x+3}{y+3} = \frac{5}{6}$$

$$6x+18=5y=15$$

$$6x-5y=15-18$$

$$6x+5y=-3 \quad \text{----- (2)}$$

From equation (1) & (2)

$$(11x-9y=-4) \times 5$$

$$(6x+5y=-3) \times 9$$

$$55x - 45y = -20$$

$$54x - 45y = -27$$

$$(-) \quad (+) \quad (+)$$

$$x=7$$

Substitute value of x in equation

$$11x - 9y = -4$$

$$11(7) - 9y = -4$$

$$77 - 9y = -4$$

$$-9y = -4 - 77$$

$$-9y = -81$$

$$9y = 81$$

$$y=9$$

$$x=7, y=9$$

The required fraction is $\frac{7}{9}$.

41) From given

$$x+10 = 2(y+10)$$

$$x+10 = 2y+20$$

$$x-2y = 10 \quad \text{----- (1)}$$

From given

$$x-10 = 6(y-10)$$

$$x-10 = 6y - 60$$

$$x-6y = -60+10$$

$$x-6y = -50 \quad \text{----- (2)}$$

subtract equation (2) from equation (1)

$$x-2y=10$$

$$x-6y=-50$$

$$(-) \quad (+) \quad (+)$$

$$4y=60$$

$$y=15$$

Substitute value of y in equation (1)

$$x-2y=10$$

$$x-2(15)=10$$

$$x-30=10$$

$$x=10+30$$

$$x=40$$

Present age of x is 40

Present age of y is 15

- 42) Let speed of boat in still water = x km/hr
Speed of current = y km/hr

Now speed of Ritu during down

$$\text{Stream} = (x+y) \text{ km/hr}$$

$$\text{Upstream} = (x-y) \text{ km/hr}$$

As per the questions given

$$2(x+y)=20$$

$$x+y=10 \quad \text{----- (1)}$$

$$2(x-y)=4$$

$$x-y=2 \quad \text{----- (2)}$$

adding equation (1) and (2)

$$x+y=10$$

$$x-y=2$$

$$2x=12$$

$$x=6$$

putting the value of x in equation (1)

$$x+y=10$$

$$6+y=10$$

$$y=10-6$$

$$y=4$$

Speed of Ritu in still water 6 km/hr

Speed of current = 4 km/hr

- 43) Let income and expenditure of persons be x & y

Income – expenditure = saving

$$(9x-4y = 2000) \quad 3$$

$$(7x-3y) = 2000) \quad 4$$

$$27x - 12y = 6000$$

$$28x - 12y = 8000$$

$$-1x = -2000$$

$$x = 2000$$

putting the value of x in equation (1)

$$9x-4y=2000$$

$$9(2000)-4y = 2000$$

$$18000 - 4y = 2000$$

$$-4y = -16000$$

$$y = 4000$$

* Now we can find monthly income.

$$\begin{aligned}\text{Income of first person} &= 9x \\ &= 9(2000) \\ &= 18000\end{aligned}$$

$$\begin{aligned}\text{Income of second person} &= 7(2000) \\ &= 14000\end{aligned}$$

44) Let age of A be = x

Son age be = y

According to question after five year

$$\begin{aligned}x+y &= 3(y+5) \\ x+y &= 3y+15 \\ x-3y &= 15-5 \\ x-3y &= 10 \quad \text{----- (1)}\end{aligned}$$

Five years age their ages be

$$\begin{aligned}x-y &= 7(y-5) \\ x-5 &= 7y-35 \\ x-7y &= -35+5 \\ x-7y &= -30 \quad \text{----- (2)}\end{aligned}$$

Subtract equation (2) from (1)

$$\begin{aligned}x-3y &= 10 \\ x-7y &= -30 \\ (-) \quad (+) \quad (+) \\ \text{-----}\end{aligned}$$

$$4y = 40$$

$$y = 10$$

substitute value of y in equation (1)

$$x-3y = 10$$

$$x-3(10) = 10$$

$$x-30 = 10$$

$$x = 40$$

* Present age of A is 40 years

* Present age of his son is 10 years.

V. Four mark questions

45)

$$2x + y = 6$$

X	0	3
Y	6	0

$$2x - y = -2$$

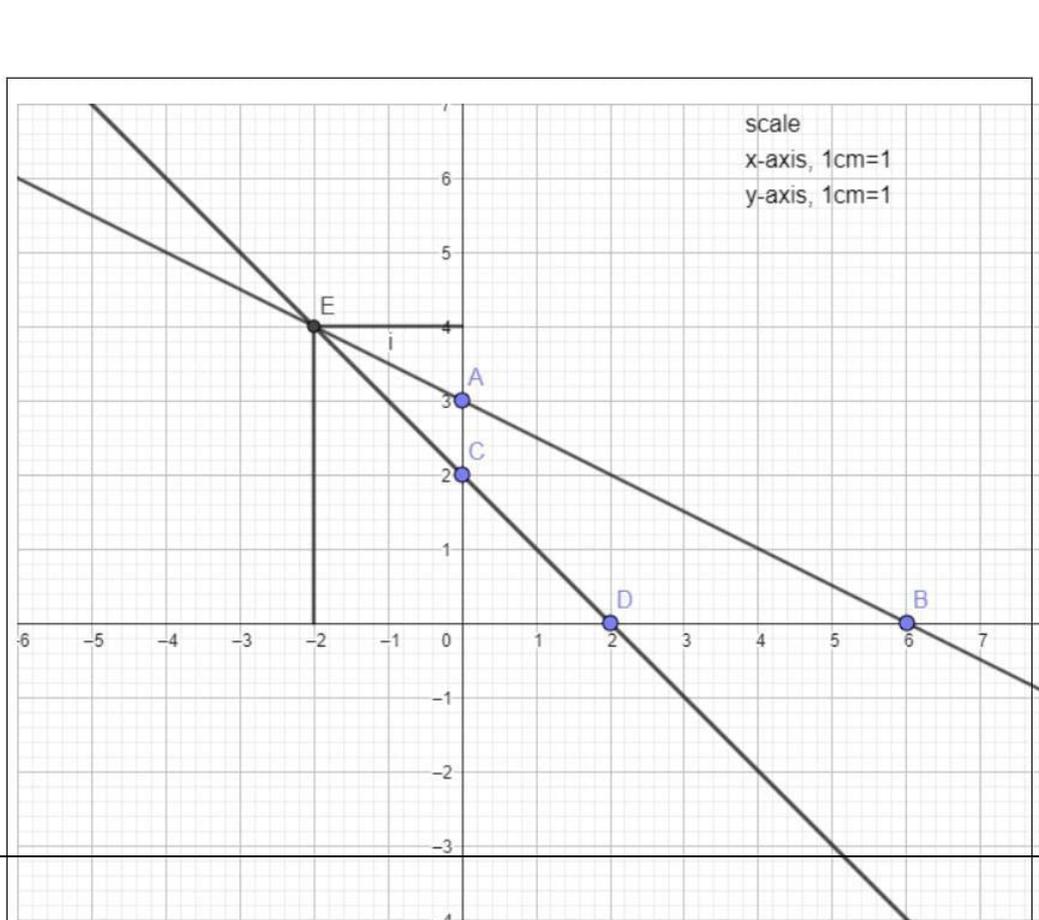
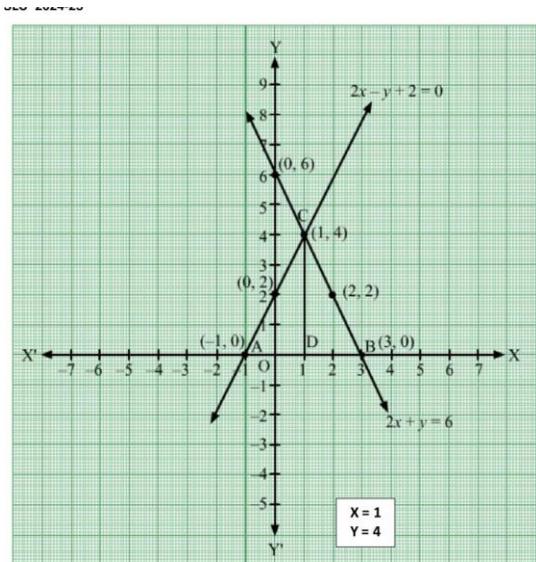
X	0	-1
Y	2	0

46) $x + 2y = 6$

X	0	3
Y	3	0
(x,y)	(0,3)	(6,0)

$$x + y = 2$$

X	0	2
Y	2	0
(x,y)	(0,5)	(5,0)



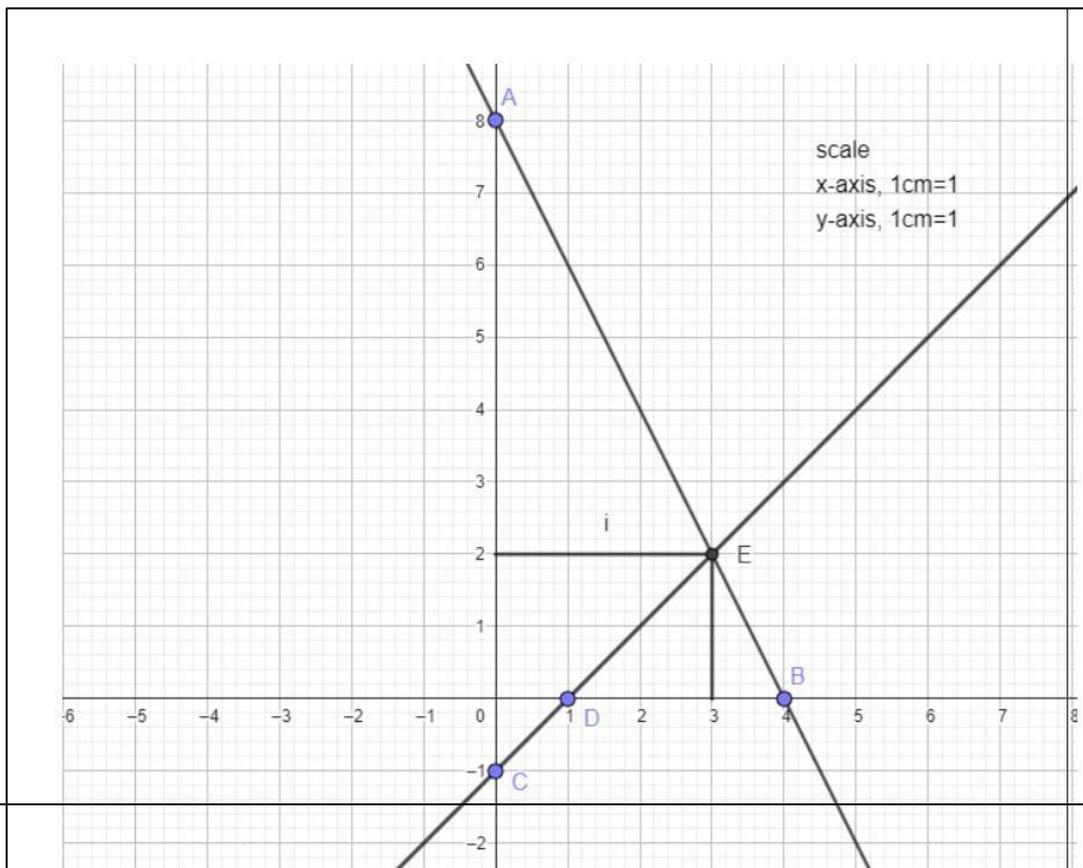
$$x=-2 \quad y=4$$

47) $2x+y = 8$

X	0	4
Y	8	0
(x,y)	(0,8)	(4,0)

$$x-y = 1$$

X	0	1
Y	-1	0
(x,y)	(0,-1)	(1,0)



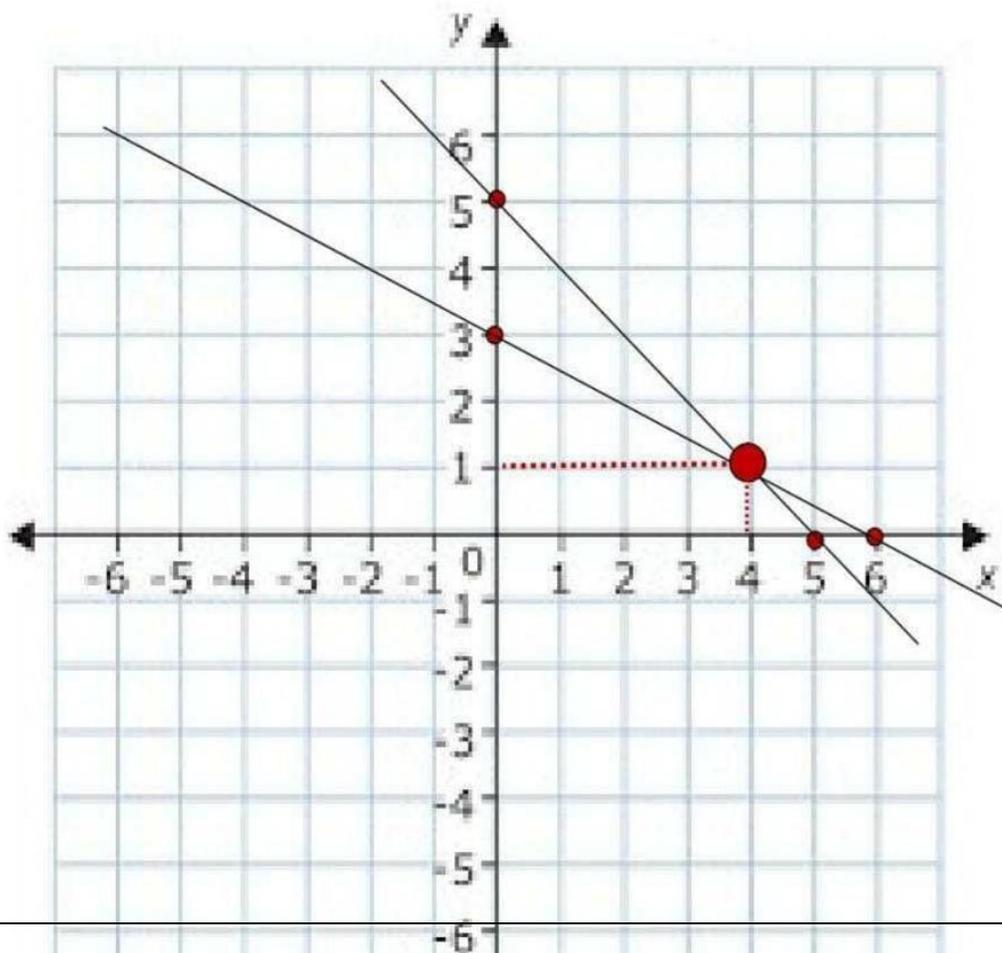
$$x=3 \quad y=2$$

48) $x+2y = 6$

X	0	6
Y	3	0

$$x+y = 5$$

X	0	5
Y	5	0



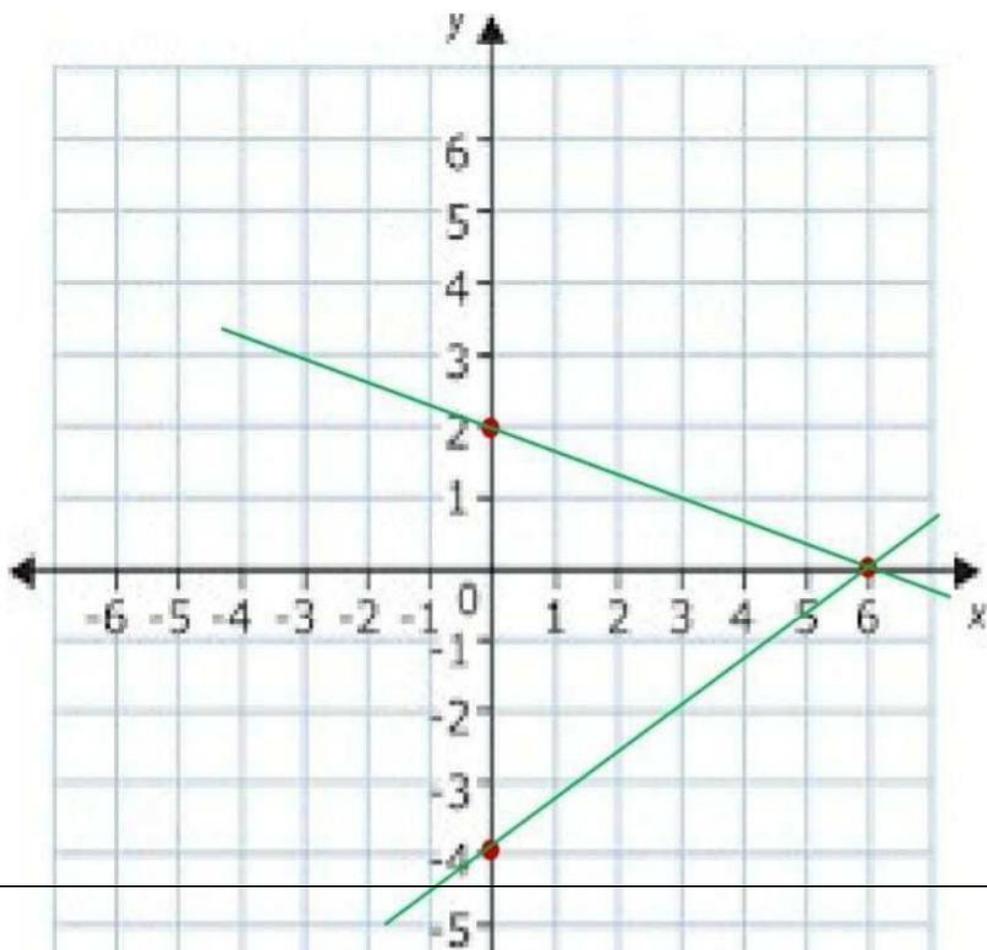
$$x=4 \quad y=1$$

49) $x+3y = 6$

X	0	6
Y	2	0

$$2x-3y = 12$$

X	0	6
Y	-4	0



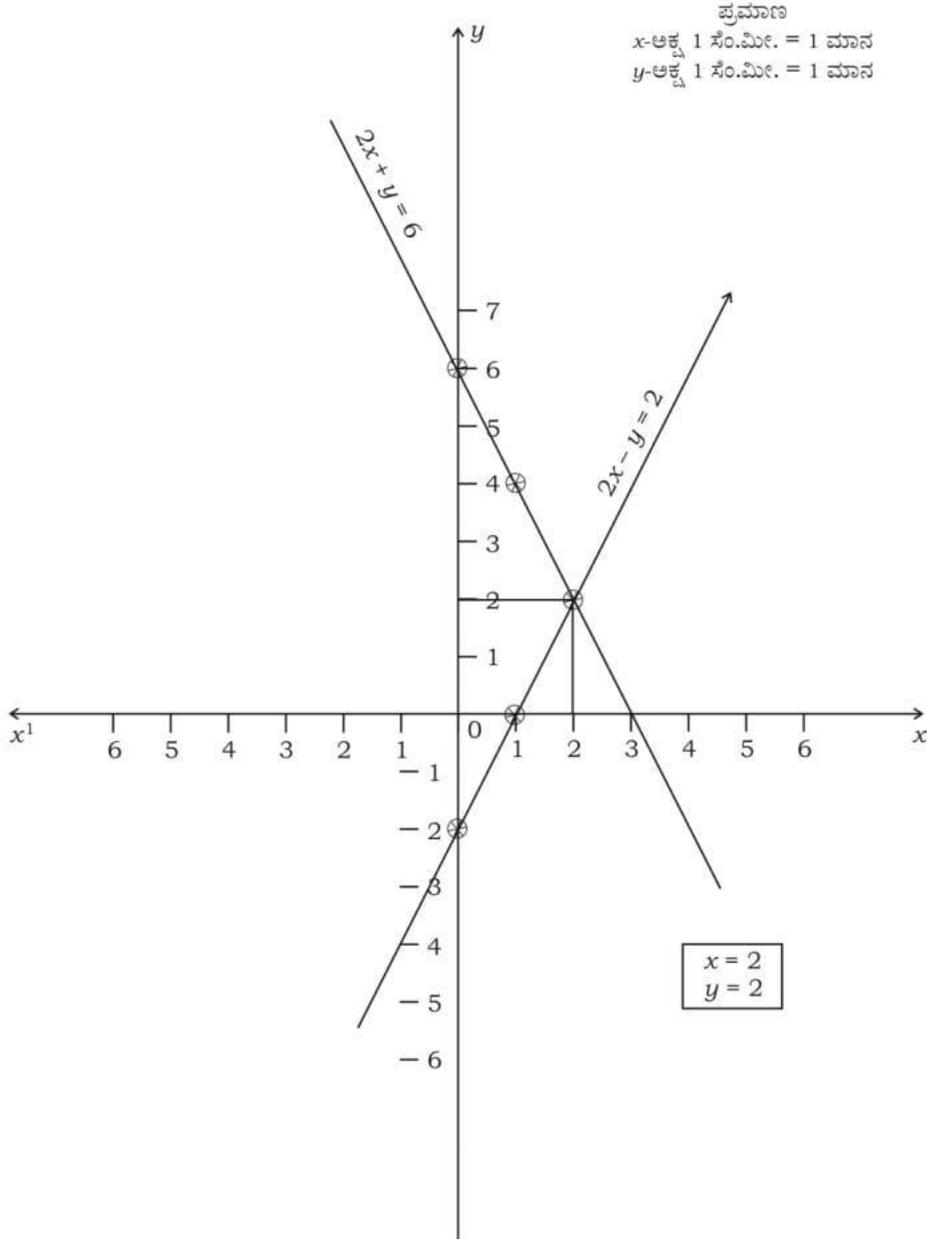
$$x=6 \quad y=0$$

50) $2x+y = 6$

X	0	1	2
Y	6	4	2

$$2x-y = 2$$

X	0	1	2
Y	-2	0	2



51) $2x - y = 7$

$y = 2x - 7$

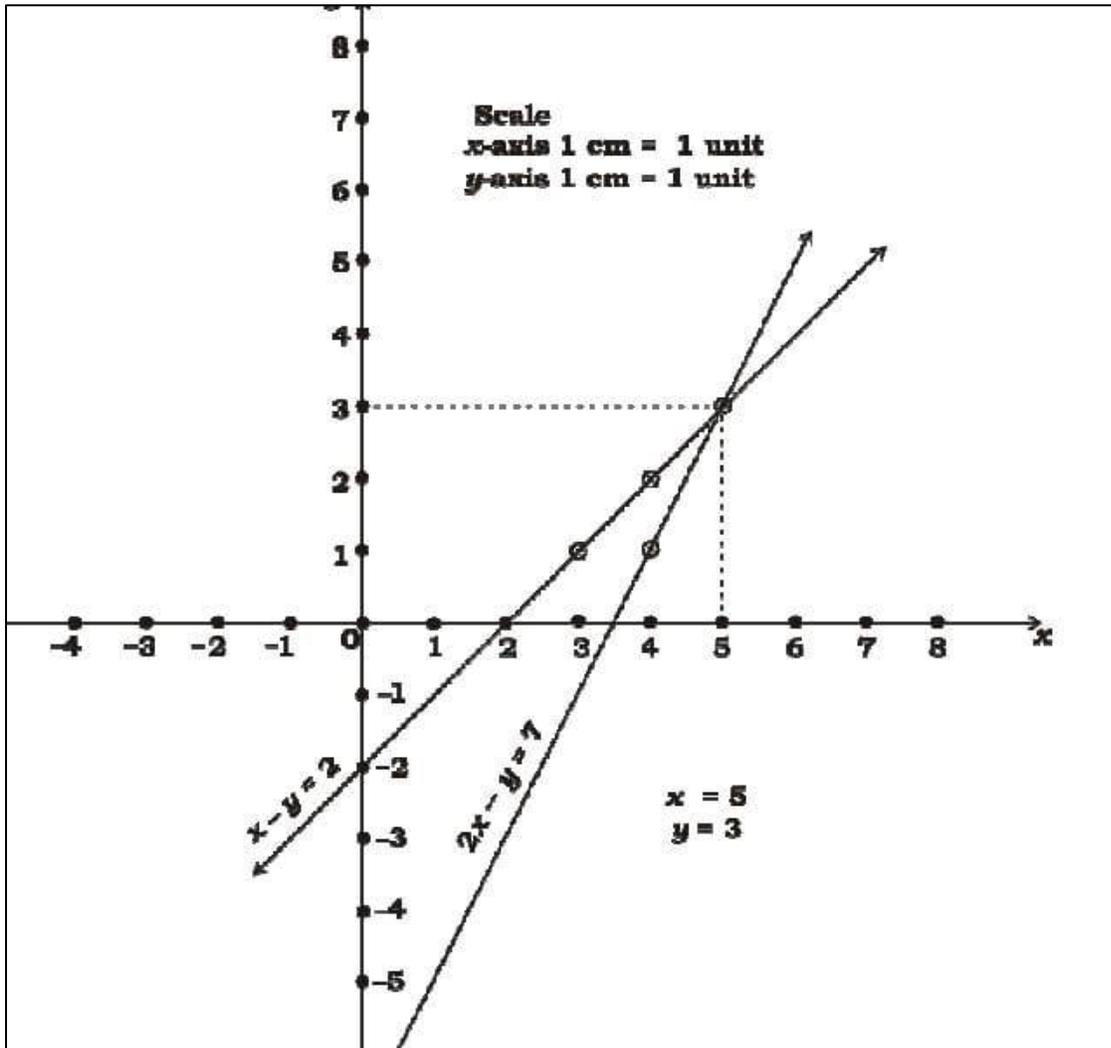
X	3	4	5
Y	-1	1	3

$x - y = 2$

$y = x - 2$

X	3	4	5
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Y	1	2	3
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Unit – 04 QUADRATIC EQUATIONS

I. Multiple Choice Questions :

1. B) $ax^2 + bx + c = 0$
2. D) $x^2 + 3x + 4 = 0$
3. C) $x^2 - 5x + 6 = 0$
4. D) -6

5. B) Quadratic equation

6. D) $2x^2 - 3x + 5 = 0$

7. D) $x(x+1)=30$

8 A) $b^2 - 4ac$

9. A) 0

10. B) Real and Equal

11. A) it has two equal real roots

12 A) 9

13. . D) $b^2 - 4ac > 0$

14 B) 3,-2

15 C) $\frac{3}{2}$

16. C) -7

II. One Mark Questions

17. $x(2+x)=3$

$$2x+x^2 = 3$$

$$2x+x^2 -3 = 0$$

18. $\frac{x+1}{2} = \frac{1}{x}$

$$x(x+1) = 2$$

$$x^2+x = 2$$

$$x^2+x-2=0$$

19. $px^2 +qx-r = 0$

$$\Delta = b^2 - 4ac$$

$$\Delta = q^2 + 4pr$$

20. $2x^2 - 4x + 3 = 0$

$$\Delta = b^2 - 4ac$$

$$\Delta = (-4)^2 - 4 \times 2 \times 3$$

$$\Delta = 16-4 \quad \Delta = -8$$

21. $(x+4)(x+3)=0$

$$(x+3)=0$$

$$x = -3$$

22. $x = 1, x = -3$

23. $x^2 - 5x + 1 = 0$

$$\Delta = b^2 - 4ac$$

$$\Delta = (-5)^2 - 4 \times 1 \times 1$$

$$\Delta = 25 - 4$$

$$\Delta = 21$$

$$24. x^2 - 9 = 0$$

$$x^2 = 9$$

$$x = 3$$

Roots are Real and Distinct

$$25. 2m^2 = 2 - m$$

$$2m^2 + m - 2 = 0$$

$$26. x^2 - x = 0$$

$$x(x-1) = 0$$

$$x = 0, x = 1$$

$$27. x(x+2) = 0$$

$$x=0, x+2=0$$

$$x=0, x = -2$$

$$28. x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$29. x(x+1) = 306$$

III. Two Marks Questions

$$30. x^2 + 7x + 12 = 0$$

$$x^2 + 4x + 3x + 12 = 0$$

$$x(x+4) + 3(x+4) = 0$$

$$(x+4)(x+3) = 0$$

$$(x+4) = 0, (x+3) = 0$$

$$x = -4, x = -3$$

$$31. x^2 + 4x - 60 = 0$$

$$x^2 + 10x - 6x - 60 = 0$$

$$x(x+10) - 6(x+10) = 0$$

$$(x+10)(x-6) = 0$$

$$(x+10) = 0, (x-6) = 0$$

$$x = -10, x = 6$$

$$32. x^2 + 3x + 2 = 0$$

$$x^2 + 1x + 2x + 2 = 0$$

$$\begin{aligned}
 x(x+1) + 2(x+1) &= 0 \\
 (x+1)(x+2) &= 0 \\
 (x+1) = 0, \quad (x+2) &= 0 \\
 x = -1, \quad x &= -2
 \end{aligned}$$

$$\begin{aligned}
 33. \quad 2x^2 + x - 6 &= 0 \\
 2x^2 + 4x - 3x - 6 &= 0 \\
 2x(x+2) - 3(x+2) &= 0 \\
 (x+2)(2x-3) &= 0 \\
 (x+2) = 0, \quad (2x-3) &= 0 \\
 x = -2, \quad x &= \frac{3}{2}
 \end{aligned}$$

$$\begin{aligned}
 34. \quad x^2 + 8x + 12 &= 0 \\
 x^2 + 6x + 2x + 12 &= 0 \\
 x(x+6) + 2(x+6) &= 0 \\
 (x+6)(x+2) &= 0 \\
 (x+6) = 0, \quad (x+2) &= 0 \\
 x = -6, \quad x &= -2
 \end{aligned}$$

$$\begin{aligned}
 35. \quad 2x^2 - 5x + 3 &= 0 \\
 a = 2, \quad b = -5, \quad c &= 3 \\
 \Delta = b^2 - 4ac \\
 \Delta = (-5)^2 - 4 \times 2 \times 3 \\
 \Delta = 25 - 24 = 1 > 0 \\
 \text{Roots are real and distinct}
 \end{aligned}$$

$$\begin{aligned}
 36. \quad 4x^2 - 4x + 1 &= 0 \\
 a = 4, \quad b = -4, \quad c &= 1 \\
 \Delta = b^2 - 4ac \\
 \Delta = (-4)^2 - 4 \times 4 \times 1 \\
 \Delta = 16 - 16 = 0
 \end{aligned}$$

Roots are real and equal

$$\begin{aligned}
 37. \quad 2x^2 - 6x + 3 &= 0 \\
 a = 2, \quad b = -6, \quad c &= 3 \\
 \Delta = b^2 - 4ac \\
 \Delta = (-6)^2 - 4 \times 2 \times 3 \\
 \Delta = 36 - 24 = 12 > 0
 \end{aligned}$$

Roots are real and distinct

$$\begin{aligned}
 38. \quad x^2 + 4x + 4 &= 0 \\
 a = 1, \quad b = 4, \quad c &= 4
 \end{aligned}$$

$$\Delta = b^2 - 4ac$$

$$\Delta = (4)^2 - 4 \times 1 \times 4$$

$$\Delta = 16 - 16 = 0$$

Roots are real and equal

$$39. 2x^2 - 5x - 1 = 0$$

$$a = 2, \quad b = -5, \quad c = -1$$

$$\Delta = b^2 - 4ac$$

$$\Delta = (-5)^2 - 4 \times 2 \times -1$$

$$\Delta = 25 + 8 = 33 > 0$$

Roots are real and distinct

$$40. x^2 + ax - 4 = 0$$

$$a = 1, \quad b = a, \quad c = -4$$

$$\Delta = b^2 - 4ac$$

$$\Delta = (a)^2 - 4 \times 1 \times -4$$

$$\Delta = a^2 + 16 > 0$$

Roots are real and distinct

$$41. kx^2 + 6x + 1 = 0$$

$$a = k, \quad b = 6, \quad c = 1$$

$$\Delta = b^2 - 4ac = 0$$

$$\Delta = (6)^2 - 4 \times k \times 1 = 0$$

$$36 - 4k = 0$$

$$4k = 36$$

$$k = 9$$

$$42. x^2 + bx + 9 = 0$$

$$a = 1, \quad b = b, \quad c = 9$$

$$b^2 - 4ac = 0$$

$$(b)^2 - 4 \times 1 \times 9 = 0$$

$$b^2 - 36 = 0$$

$$b^2 = 36$$

$$b = \sqrt{36}$$

$$b = \pm 6$$

Quadratic Equation $x^2 - 6x + 9 = 0$

$$43. 2x^2 + kx + 3 = 0$$

$$a = 2, \quad b = k, \quad c = 3$$

$$b^2 - 4ac = 0$$

$$(k)^2 - 4 \times 2 \times 3 = 0$$

$$k^2 - 24 = 0$$

$$k^2 = 24$$

$$k = \sqrt{24}$$

$$k = \sqrt{4 \times 6}$$

$$k = \pm 2\sqrt{6}$$

$$44. x^2 + 4x + 5 = 0$$

$$a = 1, b = 4, c = 5$$

$$\Delta = b^2 - 4ac$$

$$\Delta = (4)^2 - 4 \times 1 \times 5$$

$$\Delta = 16 - 20 = -4 < 0$$

No Real roots

$$45. 3x^2 - 5x + 2 = 0$$

$$3x^2 - 3x - 2x + 2 = 0$$

$$3x(x - 1) - 2(x - 1) = 0$$

$$(x - 1)(3x - 2) = 0$$

$$(x - 1) = 0, (3x - 2) = 0$$

$$x = 1, x = \frac{2}{3}$$

IV. Three Marks Questions

46. Length of the first side of the square be x mts.

Length of the second side of the square be y mts

Area of the first square x^2 & area of second square be y^2

Perimeter of the first square $4x$ and perimeter of the second square is $4y$

$$4x - 4y = 64$$

$$x - y = 16$$

$$x = (y + 16) \dots (1)$$

$$x^2 + y^2 = 640$$

$$(y + 16)^2 + y^2 = 640$$

$$y^2 + 32y + 256 + y^2 = 640$$

$$2y^2 + 32y - 384 = 0$$

$$y^2 + 16y - 192 = 0$$

$$y^2 + 24y - 8y - 192 = 0$$

$$y(y + 24) - 8(y + 24) = 0$$

$$(y + 24)(y - 8) = 0$$

$$(y + 24) = 0, (y - 8) = 0$$

$$y = -24, y = 8$$

Length of the second side of the square $y = 8$ mts

Length of the first side of the square be $x = 8 + 16 = 24$ mts

47. Let the two consecutive odd integers be x and $x + 2$

$$x^2 + (x + 2)^2 = 290$$

$$x^2 + x^2 + 4x + 4 = 290$$

$$\begin{aligned}
2x^2 + 4x - 286 &= 0 \\
x^2 + 2x - 143 &= 0 \\
x^2 + 13x - 11x - 143 &= 0 \\
x(x+13) - 11(x+13) &= 0 \\
(x+13)(x-11) &= 0 \\
x+13 = 0, \quad x-11 = 0 \\
x = -13, \quad x = 11
\end{aligned}$$

Two consecutive odd integers are 11 & 13

48. Present age of mother be x years and present age of son be y years

$$x = 2y^2$$

Age of mother after 8 years $(x+8)$ years and that of son is $(y+8)$ years

$$\begin{aligned}
x+8 &= 3(y+8) + 4 \\
2y^2 + 8 &= 3y + 24 + 4 \\
2y^2 + 8 &= 3y + 28 \\
2y^2 - 3y - 20 &= 0 \\
2y^2 - 8y + 5y - 20 &= 0 \\
2y(y-4) + 5(y-4) &= 0 \\
(y-4)(2y+5) &= 0 \\
y-4 = 0, \quad 2y+5 = 0 \\
y = 4, \quad y = \frac{-5}{2}
\end{aligned}$$

Present age of mother $x = 32$ years

Present age of son $y = 4$ years

49. Let Base = x cm, Altitude = $(x - 5)$ cm

$$\begin{aligned}
\frac{1}{2} \times x \times (x-5) &= 150 \\
x^2 - 5x - 300 &= 0 \\
x^2 - 20x + 15x - 300 &= 0 \\
x(x-20) + 15(x-20) &= 0 \\
(x-20)(x+15) &= 0 \\
x-20 = 0, \quad x+15 = 0 \\
x = 20, \quad x = -15 \\
\text{base} = x = 20 \text{ cm} \\
\text{Altitude} = (x-5) = 20-5 = 15 \text{ cm}
\end{aligned}$$

50. Let two consecutive even positive integers be x and $(x + 2)$

$$\begin{aligned}
x^2 + (x + 2)^2 &= 164 \\
x^2 + x^2 + 4x + 4 &= 164 \\
2x^2 + 4x - 160 &= 0 \\
x^2 + 2x - 80 &= 0 \\
x^2 + 10x - 8x - 80 &= 0 \\
x(x+10) - 8(x+10) &= 0 \\
(x+10)(x-8) &= 0 \\
x+10 = 0, \quad x-8 = 0 \\
x = -10, \quad x = 8
\end{aligned}$$

Two consecutive even positive integers 8 & 10

51. Let the numbers be x and y

$$\begin{aligned}x+y &= 27 \\y &= 27-x \\x(27-x) &= 182 \\27x - x^2 &= 182 \\x^2 - 27x + 182 &= 0 \\x^2 - 14x - 13x + 182 &= 0 \\x(x-14) - 13(x-14) &= 0 \\(x-14)(x-13) &= 0 \\x-14 = 0, \quad x-13 = 0 \\x = 14, \quad x = 13 \\ \text{The numbers are } 14 \text{ \& } 13\end{aligned}$$

52. Let Base = x cm, height = (x - 7) cm

$$\begin{aligned}x^2 + (x-7)^2 &= 13^2 \\x^2 + x^2 - 14x + 49 &= 169 \\2x^2 - 14x + 49 - 169 &= 0 \\x^2 - 7x - 60 &= 0 \\x^2 - 12x + 5x - 60 &= 0 \\x(x-12) + 5(x-12) &= 0 \\(x-12)(x+5) &= 0 \\x-12 = 0, \quad x+5 = 0 \\x = 12, \quad x = -5\end{aligned}$$

base = x = 12 cm & height = (x - 7) = 12 - 7 = 5 cm

53.

No. of books	Cost of each book (in Rs.)
x	$\frac{60}{x}$
x+5	$\frac{60}{x+5}$

$$\begin{aligned}\frac{60}{x} - \frac{60}{x+5} &= 1 \\ \frac{60(x+5) - 60x}{x(x+5)} &= 1 \\ \frac{60x + 300 - 60x}{x^2 + 5x} &= 1 \\ \frac{300}{x^2 + 5x} &= 1 \\ x^2 + 5x &= 300 \\ x^2 + 5x - 300 &= 0 \\ x^2 + 20x - 15x - 300 &= 0 \\ x(x+20) - 15(x+20) &= 0 \\ (x+20)(x-15) &= 0 \\ x+20 = 0, \quad x-15 = 0 \\ x = -20, \quad x = 15\end{aligned}$$

Number of books = 15

54. Let the age of son be x years and that of father is $(x + 30)$ years

After 5 years, The age of son is $(x+5)$ years and age of father is $(x+35)$ years

$$(x+5)(x+35) = 400$$

$$x^2 + 40x + 175 = 400$$

$$x^2 + 40x - 225 = 0$$

$$x^2 + 45x - 5x - 225 = 0$$

$$x(x+45) - 5(x+45) = 0$$

$$(x+45)(x-5) = 0$$

$$x+45 = 0, \quad x-5 = 0$$

$$x = -45, \quad x = 5$$

Age of son is 5 years and age of father is 35 years

55. Let the first number be x then the second number is $(x - 3)$

$$x^2 + (x - 3)^2 = 29$$

$$x^2 + x^2 - 6x + 9 = 29$$

$$2x^2 - 6x - 20 = 0$$

$$x^2 - 3x - 10 = 0$$

$$x(x-5) + 2(x-5) = 0$$

$$(x-5)(x+2) = 0$$

$$x-5 = 0, \quad x+2 = 0$$

$$x = 5, \quad x = -2$$

First number = $x = 5$ & second number = $x-3 = 5-3 = 2$

56. Let the base be $2x + 4$ cm and height = x cm

$$\frac{1}{2} \times x \times (2x+4) = 48$$

$$x^2 + 2x - 48 = 0$$

$$x^2 + 8x - 6x - 48 = 0$$

$$x(x+8) - 6(x+8) = 0$$

$$(x+8)(x-6) = 0$$

$$x+8 = 0, \quad x-6 = 0$$

$$x = -8, \quad x = 6$$

Base = $2(6) + 4 = 16$ cm and height = 6 cm

57. Let the number of students went for picnic be x

$$\frac{900}{x-10} - \frac{900}{x} = 15$$

$$900x - 900(x-10) = 15x(x-10)$$

$$900x - 900x + 9000 = 15x^2 - 150x$$

$$15x^2 - 150x - 9000 = 0$$

$$x^2 - 10x - 600 = 0$$

$$x^2 - 30x + 20x - 600 = 0$$

$$x(x-30) + 20(x-30) = 0$$

$$(x-30)(x+20) = 0$$

$$x-30 = 0, \quad x+20 = 0$$

$$x = 30, x = -20$$

$$\text{Number of students went for picnic} = 30 - 10 = 20$$

58.

Let the Length = x , Breadth = y

$$\text{Perimeter of the rectangular field} = 2x + 2y = 32$$

$$x + y = 16$$

$$y = 16 - x$$

$$\text{Area of the field} = xy = 60$$

$$x(16 - x) = 60$$

$$16 - x^2 = 60$$

$$x^2 - 16x + 60 = 0$$

$$x^2 - 10x - 6x + 60 = 0$$

$$x(x - 10) - 6(x - 10) = 0$$

$$(x - 10)(x - 6) = 0$$

$$x - 10 = 0, x - 6 = 0$$

$$x = 10, x = 6$$

$$\text{Length} = x = 10 \text{ m}, \text{Breadth} = y = 6 \text{ m}$$

59.

Speed of the train be x km/h

$$\frac{480}{x} - \frac{480}{x+10} = 4$$

$$480x(x+10) - 480x = 4(x+10)x$$

$$480x + 4800 - 480x = 4x^2 + 40x$$

$$4x^2 + 40x - 30x - 12000 = 0$$

$$x(x+40) - 30(x+40) = 0$$

$$(x+40)(x-30) = 0$$

$$x+40 = 0, x-30 = 0$$

$$x = -40, x = 30$$

$$\text{Speed of train } x = 30 \text{ km/h}$$

60.

Let the Length = x , Breadth = y

$$\text{Perimeter of the rectangular field} = 2x + 2y = 80$$

$$x + y = 40$$

$$y = 40 - x$$

$$\text{Area of the rectangular field} = xy = 400$$

$$x(40 - x) = 400$$

$$40x - x^2 = 400$$

$$x^2 - 40x + 400 = 0$$

$$x^2 - 20x - 20x + 400 = 0$$

$$x(x - 20) - 20(x - 20) = 0$$

$$(x - 20)(x - 20) = 0$$

$$x-20=0, x-20=0$$

$$x=20, x=20$$

$$\text{Length} = x = 20 \text{ m, Breadth} = y = 40 - x = 40 - 20 = 20 \text{ m}$$

61. Let the cycling speed of A be x km/h

$$\text{Time taken by A to reach the office} = \frac{\text{distance}}{\text{Speed}} = \frac{12}{x} \text{ hrs}$$

The Cycling speed of B is more than A hence the cycling speed of B = $(x+2)$ km/h

$$\text{Time taken by B to reach the office} = \frac{12}{x+2} \text{ hrs}$$

$$\frac{12}{x} - \frac{12}{x+2} = \frac{1}{2}, \quad 30 \text{ min} = \frac{1}{2} \text{ hr}$$

$$\frac{12}{x} - \frac{12}{x+2} = \frac{1}{2}$$

$$\frac{12(x+2) - 12x}{x(x+2)} = \frac{1}{2}$$

$$\frac{24}{x^2+2x} = \frac{1}{2}$$

$$x^2 + 8x - 6x - 48 = 0$$

$$x^2 + 2x - 48 = 0$$

$$x(x+8) - 6(x+8) = 0$$

$$(x+8)(x-6) = 0$$

$$x = -8, x = 6$$

Speed of A = 6 km/h & speed of B = $6+2 = 8$ km/h

$$\text{Time taken by A to reach the office} = \frac{\text{distance}}{\text{Speed}} = \frac{12}{6} = 2 \text{ hrs}$$

$$B = \frac{\text{distance}}{\text{Speed}} = \frac{12}{8} = 1.5 \text{ hrs}$$

62. Let the Cost price of the article be Rs. x

Selling price = Rs. 24

$$\text{Percentage Gain} = x + \frac{x^2}{100} = 24$$

$$x^2 + 100x - 2400 = 0$$

$$x^2 + 120x - 20x - 2400 = 0$$

$$x(x + 120) - 20(x + 120) = 0$$

$$(x+120)(x-20) = 0$$

$$x = -120, x = 20$$

Therefore cost price of the article $x = \text{Rs. } 20$

63. Let the Cost price of the article be Rs. x

Selling price = Rs 24

Loss = C.P. - S.P

$$\text{Loss Percentage} \frac{x}{100} \times x = x - 24$$

$$\frac{x^2}{100} - x = 24$$

$$x^2 - 100x - 2400 = 0$$

$$x^2 - 120x + 20x - 2400 = 0$$

$$x(x - 120) + 20(x - 120) = 0$$

$$(x-120)(x+20) = 0$$

$$x = 120, x = -20$$

Therefore Cost price of the article = Rs. 120

$$64. (1+m^2)x^2 + 2mcx + c^2 - a^2 = 0$$

$$a = (1+m^2), \quad b = 2mc, \quad c = c^2 - a^2$$

$$\text{If roots are equal, } \Delta = b^2 - 4ac = 0$$

$$(2mc)^2 - 4(1+m^2)(c^2 - a^2) = 0$$

$$4m^2c^2 - 4(c^2 - a^2 + m^2c^2 - a^2m^2) = 0$$

$$m^2c^2 - c^2 + a^2 - m^2c^2 + a^2m^2 = 0$$

$$-c^2 + a^2(1+m^2) = 0$$

$$c^2 = a^2(1+m^2) = 0$$

$$65. (b-c)x^2 + (c-a)x + (a-b) = 0$$

$$ax^2 + bx + c = 0$$

$$a = (b-c) \quad b = (c-a) \quad c = (a-b)$$

$$b^2 - 4ac = 0$$

$$(c-a)^2 - 4[b-c](a-b) = 0$$

$$c^2 - 2ac + a^2 - 4(ab - ac - b^2 + ab) = 0$$

$$c^2 - 2ac + a^2 - 4ab + 4ac + 4b^2 - 4cb = 0$$

$$a^2 + 4b^2 + c^2 - 4ab - 4bc + 2ac = 0$$

$$(a - 2b + c)^2 = 0$$

$$a - 2b + c = 0$$

$$a + c = 2b$$

$$2b = a + c$$

V. Four Marks Questions

$$66. \text{ Let the Speed of Stream} = x \text{ km/h}$$

$$\text{Speed of motor boat in still water} = 11 \text{ km/h}$$

$$\text{Speed upstream} = (11-x) \text{ km/h}$$

$$\text{Speed downstream} = (11+x) \text{ km/h}$$

$$\text{Time taken by the boat to travel upstream} = t_1 = \frac{12}{11-x} \text{ hrs}$$

$$\text{Time taken by the boat to travel downstream} = t_2 = \frac{12}{11+x} \text{ hrs}$$

$$t_1 + t_2 = 2\frac{3}{4}$$

$$\frac{12}{11-x} + \frac{12}{11+x} = 2\frac{3}{4}$$

$$\frac{12(11+x)+12(11-x)}{(11-x)(11+x)} = \frac{11}{4}$$

$$48(11+x)+48(11-x) = 11(11-x)(11+x)$$

$$528+48x+528-48x = 11(121-x^2)$$

$$1056 = 1331- 11x^2$$

$$11x^2 = 1331-1056$$

$$11x^2 = 275$$

$$x^2 = \frac{275}{11}$$

$$x^2 = 25$$

$$x = \pm 5$$

Speed of Stream = $x = 5$ km/h

67. Let the age be x years

$$(19+x)(15+x) = 480$$

$$x^2 - 34x - 195 = 0$$

$$x^2 + 39x - 5x - 195 = 0$$

$$x(x+39) - 5(x+39) = 0$$

$$(x+39)(x-5) = 0$$

$$x+39=0, x-5=0$$

$$x = -39, x = 5$$

Product of their ages becomes 480 after 5 years

68. Let the speed of motor boat in still water = x km/h

Speed of motor boat upstream = $(x-5)$ km/h

Speed of motor boat downstream = $(x+5)$ km/h

Time taken by the motor boat to travel upstream = $t_1 = \frac{30}{x-5}$ hrs

Time taken by the motor boat to travel downstream = $t_2 = \frac{30}{x+5}$ hrs

$$t_1 + t_2 = \frac{9}{2}$$

$$\frac{30}{x-5} + \frac{30}{x+5} = \frac{9}{2}$$

$$\frac{30(x+5)+30(x-5)}{(x-5)(x+5)} = \frac{9}{2}$$

$$30(x+5)2 + 30(x-5)2 = 9(x+5)(x-5)$$

$$60x+300+60x-300 = 9x^2-225$$

$$120x = 9x^2 - 225$$

$$3x^2 - 40x - 75 = 0$$

$$3x^2 - 40x + 5x - 75 = 0$$

$$3x(x-15) + 5(x-15) = 0$$

$$(x-15)(3x+5) = 0$$

$$x-15=0, 3x+5=0$$

$$x = 15, x = \frac{-5}{3}$$

Speed of Motor boat in still water = $x = 15$ km/h

69. Let speed of Passenger train be x km/h

Speed of express train = $(x+11)$ km/h

$$\text{Time} = \frac{\text{distance}}{\text{speed}}$$

$$\text{Time taken by the passenger train to travel 132 km} = t_1 = \frac{132}{x} \text{ hrs}$$

$$\text{Time taken by the express train to travel 132 km} = t_2 = \frac{132}{x+11} \text{ hrs}$$

$$\frac{132}{x} - \frac{132}{x+11} = 1$$

$$\frac{132(x+11) - 132x}{x(x+11)} = 1$$

$$12 + 1452 - 132x = x^2 + 11x$$

$$x^2 + 11x - 1452 = 0$$

$$3x^2 - 33x + 44x - 1452 = 0$$

$$x(x-33) + 44(x-33) = 0$$

$$(x-33)(x+44) = 0$$

$$x-33=0, \quad x+44=0$$

$$x = 33, \quad x = -44$$

$$\text{Speed of Passenger train } x = 33 \text{ km/h}$$

$$\text{Speed of Express Train} = (x+11) = 33+11 = 44 \text{ km/h}$$

$$\text{Average Speed} = \frac{33+44}{2} = \frac{77}{2} = 38.5 \text{ km/h}$$

70. Present age of B be x years

$$\text{Present age of A} = (x + 26) \text{ years}$$

$$\text{Age of A after 3 years is } (x+29), \quad \text{B is } (x+3) \text{ years}$$

$$(x+29)(x+3) = 360$$

$$x^2 + 3x + 2x + 87 = 360$$

$$x(x+39) - 7(x+39) = 0$$

$$(x+39)(x-7) = 0$$

$$x+39=0, \quad x-7=0$$

$$x = -39, \quad x = 7$$

$$\text{Present age of B } x = 7 \text{ years}$$

$$\text{Present age of A} = x + 26 = 7 + 26 = 33 \text{ years}$$

71. Let the Length and breadth of rectangle respectively be AB = x mts , BC = y mts , CD be the length of wall

$$\text{Length of fence} = 30\text{m}$$

$$x^2 = 4y$$

$$y + x + y = 30$$

$$x + 2y = 30$$

$$y = \left(\frac{30-x}{2} \right) \dots\dots\dots(1)$$

$$\text{Area of rectangular field } 100\text{m}^2$$

$$xy = 100$$

$$x \left(\frac{30-x}{2} \right) = 100$$

$$30x - x^2 = 200$$

$$x^2 - 30x + 200 = 0$$

$$x^2 - 10x - 20x + 200 = 0$$

$$x(x-10) - 20(x-10) = 0$$

$$(x-10)(x-20) = 0$$

$$x-10=0, x-20=0$$

$$x = 10, x = 20$$

$$\text{Substitute } x = 10 \text{ in (1) } y = \left(\frac{30-10}{2}\right) = 10$$

Length and breadth of rectangular field

$$AB = 10\text{m}, BC = 10\text{m}$$

72. Let the numerator of the fraction be x

$$\text{Denominator} = 2x+1$$

$$\text{Fraction} = \frac{\text{Numerator}}{\text{Denominator}} = \frac{x}{2x+1}$$

$$\text{Reciprocal of the fraction} = \frac{2x+1}{x}$$

$$\frac{x}{2x+1} + \frac{2x+1}{x} = \frac{29}{10}$$

$$\frac{x^2 + (2x+1)^2}{(x(2x+1))} = \frac{29}{10}$$

$$\frac{5x^2 + 1 + 4x}{2x^2 + x}$$

$$10(5x^2 + 1 + 4x) = 29(2x^2 + x)$$

$$50x^2 + 10 + 40x - 58x^2 - 29x = 0$$

$$8x^2 - 16x + 15x - 10 = 0$$

$$8x(x-2) + 5(x-2) = 0$$

$$(x-2)(8x+5) = 0$$

$$x = 2, x = \frac{-5}{8}$$

$$x = 2$$

$$\text{Numerator} = 2$$

$$\text{Denominator} = 2x+1 = 2(2)+1 = 5$$

$$\text{Fraction} = \frac{2}{5}$$

73.

Number of Students	Amount that each student secure
x	$\frac{1500}{x}$
$x+5$	$\frac{1500}{x+5}$

$$\frac{1500}{x} - \frac{1500}{x+5} = 25$$

$$\frac{1500(x+5) - 1500x}{x(x+5)} = 25$$

$$\frac{7500}{x^2+5x} = 25$$

$$25(x^2+5x) = 7500$$

$$x^2 + 5x - 300 = 0$$

$$x^2 + 20x - 15x - 300 = 0$$

$$x(x+20) - 15(x+20) = 0$$

$$(x + 20)(x - 15) = 0$$

$$x + 20 = 0, \quad x - 15 = 0$$

$$x = -20, \quad x = 15$$

Number of students who secured A+ grade after examination = $15 + 5 = 20$

Unit : 05 ARITHMETIC PROGRESSION

I. Multiple Choice Questions :

1. D) 5, 9, 13, 17
2. B) -2
3. A) -7
4. B) $a_n = a + (n - 1)d$
5. B) 18
6. D) 25
7. A) 18
8. B) 7
9. C) $3n + 7$
10. C) 2
11. A) 10
12. A) 17
13. A) 48
14. D) $m + 27$
15. A) 4
16. A) 10, 16
17. C) 2, 6, 10
18. A) $a_n = 4n - 1$
19. A) $s_n = \frac{n}{2}(a + l)$
20. B) $a_n = s_n - s_{n-1}$

II. One Mark Questions :

21. $a_n = \frac{n}{2}[a + a_n]$
22. $b_n = b + (n - 1)d$
23. $a_n = l - (n - 1)d$
24. Let the first three terms of the A.P
 $a - d, a, a + d$

$$a - d + a + a + d = 21$$

$$3a = 21$$

$$a = 7$$

25. Let the first term of the A.P be 'a' and common difference be 'd'

$$a_m = a + (m - 1)d = n \quad \text{--- --> (i)}$$

$$a_n = a + (n - 1)d = m \quad \text{--- --> (ii)}$$

$$(i) - (ii)$$

$$a + (m - 1)d - [a + (n - 1)d] = n - m$$

$$(m - 1)d - (n - 1)d = n - m$$

$$(m - n)d = -(m - n)$$

$$d = -1$$

26. $a_n = s_n - s_{n-1}$

$$a_4 = s_4 - s_3$$

$$a_4 = 12 - 8$$

$$a_4 = 4$$

27. $d = a_4 - a_3 = 11 - 7 = 4$

28.

$$a + 2d = 13 \quad \text{..... (1)}$$

$$a + d = 8 \quad \text{.....(2)}$$

$$(1) - (2)$$

$$d = 5$$

Substitute value of d in equation (2)

$$a + d = 8$$

$$a + 5 = 8$$

$$a = 8 - 5$$

$$a = 3$$

29. $a_n = a + (n - 1)d$

30 $x = \frac{28+4}{2}$

$$x = \frac{32}{2}$$

$$x = 16$$

$$31. a_1 = [7 - 4(1)] \quad a_2 = [7 - 4(2)]$$

$$a_1 = 3 \quad a_2 = -1$$

$$d = a_2 - a_1$$

$$= -1 - 3$$

$$d = -4$$

$$32. \quad a_n = 4n + 1$$

$$a_1 = 4(1) + 1 \quad a_2 = 4(2) + 1 \quad a_3 = 4(3) + 1$$

$$= 4 + 1 \quad = 8 + 1 \quad = 12 + 1$$

$$a_1 = 5 \quad a_2 = 9 \quad a_3 = 13$$

III. TWO MARKS QUESTIONS:

$$33. a=2, d=7-2=5, n= 15, a_n=?$$

$$a_n = a + (n - 1)d$$

$$a_{15} = 2 + (15 - 1)5$$

$$a_{15} = 2 + (14)5$$

$$a_{15} = 2 + 70$$

$$a_{15} = 72$$

$$34. \quad a=100, d=96-100=-4, a_n=12, n= ?$$

$$a_n = a + (n - 1)d$$

$$12 = 100 + (n - 1)(-4)$$

$$12 = 100 - 4n + 4$$

$$4n = 92$$

$$n = \frac{92}{4} = 23$$

$$35. a_{10} = a + 9d$$

$$34 = a + 9(3)$$

$$34 = a + 27$$

$$a = 34 - 27$$

$$a = 7$$

$$36. \quad a = -1, d = 3 - (-1) = 4, a_n = 95, n = ?$$

$$a_n = a + (n - 1)d$$

$$95 = -1 + (n - 1)4$$

$$95 = -1 + 4n - 4$$

$$4n = 100$$

$$n = \frac{100}{4} = 25$$

∴ The 25th term of an A.P is 95

37 . $a = 1, d = 5 - 1 = 4, a_n = 77$

$$a_n = a + (n - 1)d$$

$$77 = 1 + (n - 1)4$$

$$77 = 1 + (4n - 4)$$

$$77 = 1 + 4n - 4$$

$$4n = 80$$

$$n = \frac{80}{4} = 20$$

∴ 77 is an term of an A.P.

38 . $5, 8, 11, \dots$

$5, 8, 11, \dots$

here $a = 5, d = 8 - 5 = 3$ and $n = 26$

$$a_n = a + (n - 1)d$$

$$a_{26} = 5 + (26 - 1)3$$

$$a_{26} = 5 + 25 \times 3$$

$$= 5 + 75$$

$$a_{26} = 80$$

. 39. $2, 5, 8, \dots$

Here $a = 2, d = 5 - 2 = 3$ and $n = 30$

$$a_n = a + (n - 1)d$$

$$a_{30} = 2 + (30 - 1)3$$

$$a_{30} = 2 + 29 \times 3$$

$$= 2 + 87$$

$$a_{30} = 89$$

$$40. a = 3, d = 7 - 3 = 4, n = 10, S_{10} = ?$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$S_n = \frac{10}{2} [2(3) + (10 - 1)4]$$

$$S_n = 5 (6 + 9 \times 4)$$

$$= 5 (6 + 36)$$

$$S_{10} = 5 (42)$$

$$S_{10} = 210$$

$$41. a = 24, d = 4, a_n = 100, n = ?$$

$$a_n = a + (n - 1)d$$

$$100 = 24 + (n - 1)4$$

$$100 = 24 + 4n - 4$$

$$100 = 20 + 4n$$

$$n = \frac{80}{4}$$

$$n = 20. (20 - 1) = 19 \text{ minutes or } 20^{\text{th}} \text{ minute}$$

$$42. a = 5, d = 8 - 5 = 3, n = 10, S_{10} = ?$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$S_n = \frac{10}{2} [2(5) + (10 - 1)3]$$

$$S_n = 5 (10 + 9 \times 3)$$

$$= 5 (10 + 27)$$

$$S_{10} = 5 (37)$$

$$S_{10} = 185$$

$$43. S_n = \frac{n(n+1)}{2}$$

$$S_{20} = \frac{20(20+1)}{2}$$

$$S_{20} = \frac{20(20+1)}{2}$$

$$S_{20} = 10 \times 21$$

$$S_{20} = 210$$

44. $a = 21, d = 42 - 21 = 21, s_n = 210$

$$s_n = \frac{n}{2} [2a + (n - 1)d]$$

$$210 = \frac{n}{2} [2(21) + (n - 1)21]$$

$$420 = n [42 + 21n - 21]$$

$$420 = n [21n + 21]$$

$$420 = 21n^2 + 21n$$

$$21n^2 + 21n - 420 = 0$$

$$n^2 + n - 210 = 0$$

$$n^2 + 15n - 14n - 210 = 0$$

$$n(n + 15) - 14(n + 15) = 0$$

$$(n + 15)(n - 14) = 0$$

$$n + 15 = 0 \quad \text{or} \quad n - 14 = 0$$

$$n = -15 \quad n = 14$$

45. 1,3,5,7,.....

$$a = 1, d = 3 - 1 = 2, n = ?, S_n = ?$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$S_n = \frac{n}{2} [2(1) + (n - 1)2]$$

$$S_n = \frac{n}{2} [2 + 2n - 2]$$

$$S_n = \frac{n}{2} [2n]$$

$$S_n = n^2$$

46. 2,4,6,8,.....

$$a = 2, d = 4 - 2 = 2, n = ?, S_n = ?$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$S_n = \frac{n}{2} [2(2) + (n - 1)2]$$

$$S_n = \frac{n}{2} [4 + 2n - 2]$$

$$S_n = \frac{n}{2} [2n + 2]$$

$$S_n = \frac{n}{2} \times 2(n + 1)$$

$$S_n = n(n + 1)$$

47. 12,15,1899

$$a = 12, d = 3, a_n = 99$$

$$a_n = a + (n-1) d$$

$$99 = 12 + (n-1) 3$$

$$n-1 = \frac{87}{3}$$

$$n = 30$$

48. 5,10,15.....200

$$a = 5, d = 10 - 5 = 5 \text{ and } a_n = 200$$

$$a_n = a + (n-1) d$$

$$200 = 5 + (n-1)d$$

$$195 = (n-1)5$$

$$n-1 = \frac{195}{5} = 39$$

$$n = 39 + 1$$

$$n = 40$$

49. a,A,b are in A.P

$$A - a = b - A$$

$$A + A = a + b$$

$$2A = a + b$$

$$A = \frac{a+b}{2}$$

50. $a_n = a + (n-1) d$

$$a_n = 25 + (n-1) (-5)$$

$$a_n = 25 - 5n + 5 = 30 - 5n$$

\therefore if $n > 6$ then only we get the first negative term..

$$\therefore n = 7$$

7th term is the first negative term.

51. $a_n = a + (n-1) d$

$$47 = 2 + (n-1) 5$$

$$47 - 2 = 5n - 5$$

$$5n = 45 + 5$$

$$n = \frac{50}{5}$$

$$n = 10$$

∴ The th term of an A.P Is 47

$$\begin{aligned} 52. a_{54} &= a + 53d \\ &= 3 + (54 - 1) 12 \\ &= 3 + 53 \times 12 \\ &= 3 + 636 \\ &= 639 \end{aligned}$$

The term we need = $a_{54} + 132 = 639 + 132 = 771$

$$\begin{aligned} a_n &= a + (n - 1) d \\ 771 &= 3 + (n - 1) 12 \\ n - 1 &= \frac{771 - 3}{12} = \frac{768}{12} = 64 \\ n &= 65 \end{aligned}$$

The 65th term is 132 more than the 54th term.

53. $a = 3$ $d = 6 - 3 = 3$, $n = ?$ $S_n = 165$

$$\begin{aligned} S_n &= \frac{n}{2} [2a + (n - 1) d] \\ 165 &= \frac{n}{2} [2(3) + (n - 1) 3] \\ 330 &= n [6 + 3n - 3] \\ 330 &= n(3n + 3) \\ 3n^2 + 3n &= 330 \\ 3n(n + 1) &= 330 \\ n(n + 1) &= 110 \\ 10(10 + 1) &= 110 \\ n &= 10 \end{aligned}$$

54. $S_n = \frac{n}{2} [2a + (n-1) d]$

$$\begin{aligned} 114 &= \frac{6}{2} [2a + (6 - 1) d] \\ 228 &= 6 [2a + 5d] \end{aligned}$$

$$38 = 2a + 5d \dots\dots\dots(1)$$

$$34 = a + 5d$$

$$a = 4$$

$$a_n = S_n - S_{n-1}$$

$$a_6 = 114 - 80$$

$$a + 5d = 34 \dots\dots\dots(2)$$

substitute value of a in equation (1)

$$38 = 2(4) + 5d$$

$$5d = 38 - 8$$

$$5d = 30$$

$$d = \frac{30}{5}$$

$$d = 6$$

A.P $a, a + d, a + 2d$

$$4, 4 + 6, 4 + 2(6)$$

$$4, 10, 16$$

55. $a_7 = 4a_2$

$$a + 6d = 4(a + d)$$

$$a + 6d = 4a + 4d$$

$$6d - 4d = 4a - a$$

$$2d = 3a$$

$$a_{12} = 3(a_4) + 2$$

$$a + 11d = 3(a + 3d) + 2$$

$$a + 11d = 3a + 9d + 2$$

$$11d - 9d = 3a - a + 2$$

$$2d = 2a + 2 \quad \dots\dots\dots(ii)$$

substitute equation (2) in equation(1)

$$3a = 2a + 2$$

$$3a - 2a = 2$$

$$a = 2$$

$$2d = 3a \quad \dots\dots\dots(i)$$

$$2d = 3(2)$$

$$2d = 6$$

$$d = 3$$

The required sequence

$$a, a+d, a+2d$$

$$2, 2+3, 2+2(3)$$

$$2, 5, 8$$

$$56. a + 2d = 16$$

$$a_7 = a_5 + 12$$

$$a + 6d = a + 4d + 12$$

$$2d = 12$$

$$d = 6$$

$$a + 2(6) = 16$$

$$a + 12 = 16$$

$$a = 16 - 12$$

$$a = 4$$

Arithmetic Progression is

$$a, a + d, a + 2d$$

$$4, 4 + 6, 4 + 2(6)$$

$$4, 10, 16$$

57. First term = a , common difference = $3a$

$$a_5 = a + (5 - 1)d$$

$$26 = a + 4(3a)$$

$$13a = 26$$

$$a = \frac{26}{13} = 2$$

$$d = 3a = 3 \times 2 = 6$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$S_n = \frac{20[2(2) + (20-1)6]}{2}$$

$$\begin{aligned}
 S_{20} &= \frac{20(4+114)}{2} \\
 &= \frac{20 \times 118}{2} \\
 &= 1180
 \end{aligned}$$

58. The 3 digits of a number are $(a - d), a, (a + d)$

$$\therefore a - d + a + a + d = 15$$

$$\therefore a = 5$$

$$\text{Original number} = 100(5 - d) + 10(5) + (5 + d)$$

$$\text{New number} = 100(5 + d) + 10(5) + (5 - d)$$

$$= 500 - 100d + 50 + 5 + d$$

$$500 - 100d + 50 + 5 + d = 500 + 100d + 50 + 5 - d + 594$$

$$= -200d + 2d = 594$$

$$-198d = 594$$

$$d = -3$$

$$\therefore \text{original number} = (5 + 3), 5, (5 - 3) = 8, 5, 2$$

59. Four parts are $a - 3d, a - d, a + d, a + 3d$

$$a - 3d + a - d + a + d + a + 3d = 56$$

$$4a = 56$$

$$a = \frac{56}{4} = 14$$

$$\frac{(a-3d)(a+3d)}{(a-d)(a+d)} = \frac{5}{6}$$

$$= \frac{a^2 - 9d^2}{a^2 - d^2} = \frac{5}{6}$$

$$= 6a^2 - 54d^2 = 5a^2 - 5d^2$$

$$d^2 = \frac{14 \times 14}{49}$$

$$d = 2$$

Four parts

$$a - 3d = 14 - 3(2) = 14 - 6 = 8$$

$$a - d = 14 - 2 = 12$$

$$a + d = 14 + 2 = 16$$

$$a + 3d = 14 + 3(2) = 20$$

60. Five parts are $a - 2d, a - d, a, a + d, a + 2d$

$$a - 2d + a - d + a + a + d + a + 2d = 25$$

$$5a = 25 \Rightarrow a = 5$$

$$(a - 2d)^2 + (a - d)^2 + a^2 + (a + d)^2 + (a + 2d)^2 = 135$$

$$a^2 - 4ad + 4d^2 + a^2 - 2ad + 2d^2 + a^2 + a^2 + 2ad + d^2 + a^2 + 4ad + 4d^2 = 135$$

$$5a^2 + 10d^2 = 135$$

$$5(25) + 10d^2 = 135$$

$$10d^2 = 135 - 125$$

$$10d^2 = 10$$

$$d = \pm 1$$

61. $a_9 = 1 + 5a_2$

$$a_{12} = 7 + 2a_5$$

$$a + 8d = 1 + 5(a + d)$$

$$a + 11d = 7 + 2(a + 4d)$$

$$a + 8d = 1 + 5a + 5d$$

$$a + 11d = 7 + 2a + 8d$$

$$4a - 3d = -1 \text{ --- -- -- -- --} \rightarrow (1)$$

$$a - 3d = -7 \text{ --- -- -- -- --} \rightarrow (2)$$

By (1) and (2)

$$4a - 3d = -1$$

$$a - 3d = -7$$

$$\begin{array}{r} (-) \quad (+) \quad (+) \\ \hline \end{array}$$

$$3a = 6$$

$$a = 2$$

$$3d = a + 7$$

$$d = \frac{2+7}{3} = 3$$

Arithmetic progression is 2, 5, 8, 11,

62. $S_n = 6 + 11 + 16 \dots \dots \dots + 96$

$$a_n = a + (n - 1)d$$

$$96 = 6 + (n - 1)5$$

$$96 = 6 + 5n - 5$$

$$95 = 5n$$

$$n = \frac{95}{5} = 19$$

$$S_n = \frac{n(a+l)}{2}$$

$$S_{19} = \frac{19(6+96)}{2} = \frac{19 \times 102}{2} = 969$$

63. Numbers are $a - d, a, a + d$

$$a - d + a + a + d = 216$$

$$3a = 216$$

$$a = 72$$

$$a + d = 7(a - d)$$

$$72 + d = 7(72 - d)$$

$$72 + d = 504 - 7d$$

$$8d = 432$$

$$d = \frac{432}{8} = 54$$

$$\text{Numbers } (72 - 54), \quad 72, \quad (72 + 54)$$

$$18 \quad 72, \quad 126$$

64. $a + 3d + a + 7d = 24$

$$a + 5d + a + 9d = 44$$

$$2a + 10d = 24$$

$$2a + 14d = 44$$

$$a + 5d = 12$$

$$a + 7d = 22$$

$$a + 5d = 12$$

$$a + 7d = 22$$

$$\begin{array}{r} (-) \quad (-) \quad (-) \\ \hline \end{array}$$

$$-2d = -10$$

$$d = 5$$

$$a + 5d = 12$$

$$a + 5(5) = 12 \Rightarrow a = 12 - 25 = -13$$

Three terms are $-13, -8, -3$.

65.

Let angles be $a - d, a, a + d$

$$a - d + a + a + d = 180 \Rightarrow 3a = 180^\circ \Rightarrow a = 60^\circ$$

$$2(a - d) = a + d \Rightarrow 2a - 2d = a + d \Rightarrow a = 3d$$

$$3d = 60^\circ \Rightarrow d = 20^\circ$$

Angles be 40° , 60° , 80°

$$66. \quad a_m = \frac{1}{n}, \quad a_n = \frac{1}{m}$$

$$\frac{1}{n} = a + (m - 1) d \dots\dots\dots(1)$$

$$\frac{1}{m} = a + (n - 1) d \dots\dots\dots(2)$$

$$(1) - (2) \Rightarrow \frac{1}{n} - \frac{1}{m} = d[(m -) - (n + 1)]$$

$$\Rightarrow \frac{m-n}{mn} = d(m - n)$$

$$\therefore d = \frac{m-n}{mn(m-n)} = \frac{1}{mn} \dots\dots\dots(3)$$

$$\frac{1}{n} = a + (m - 1) \frac{1}{mn}$$

$$\Rightarrow a = \frac{1}{n} - (m - 1) \frac{1}{mn}$$

$$= \frac{m-m+1}{mn} = \frac{1}{mn} \dots\dots\dots(4)$$

$$a_{mn} = a + (mn - 1) d$$

$$= \frac{1}{mn} + (mn - 1) \frac{1}{mn}$$

$$= \frac{1}{mn} (1 + mn - 1)$$

$$= \frac{1}{mn} (mn)$$

$$a_{mn} = 1$$

$$67. \quad a = a + (p - 1) d \dots\dots\dots(1)$$

$$b = a + (q - 1) d \dots\dots\dots(2)$$

$$c = a + (r - 1) d \dots\dots\dots(3)$$

Multiply equation (1) by (q-r) equation (2) by (r-p) and equation (3) by (p - q)

$$(1) + (2) + (3)$$

$$= a(q - r) + b(r - p) + c(p - q) = d[(p - 1)(q - r) + (q - 1)(r - p) + (r - 1)(p - q)]$$

$$= a(q-r) + b(r-p) + c(p-q) = dpq + pr - q + r + qr - pq - r + p + rp - rp - p + q$$

$$= a(q-r) + b(r-p) + c(p-q) = d(0)$$

$$= a(q-r) + b(r-p) + c(p-q) = 0$$

$$68. S_n = \frac{n}{2} [2a + (n-1)d] \quad a + 8d = 28 \dots\dots\dots (1)$$

$$S_9 = \frac{9}{2} [2a + (9-1)d]$$

$$144 = \frac{9}{2} [2a + (9-1)d]$$

$$288 = 18a + 72d \text{ (divide by 18)}$$

$$16 = a + 4d \dots\dots\dots (2)$$

$$28 = a + 8d \dots\dots\dots (1)$$

$$(1) - (2)$$

$$12 = 4d$$

$$d = \frac{12}{4}$$

$$d = 3$$

substitute value of d in equation (2)

$$16 = a + 4d$$

$$16 = a + 4(3)$$

$$16 = a + 12$$

$$a = 16 - 12$$

$$a = 4$$

V. FOUR MARKS QUESTIONS:

$$69. a = 22, l = -11 \text{ ಮತ್ತು } \frac{n}{2}(a + l) = 66$$

$$S_n = \frac{n}{2}(a + l)$$

$$66 = \frac{n}{2}(22 - 11)$$

$$66 = \frac{n}{2}(11)$$

$$11n = 132 \Rightarrow n = \frac{132}{11} = 12$$

Number of terms = 12

$$a_n = a + (n - 1)d$$

$$-11 = 22 + (12 - 1)d \Rightarrow 11d + 22 = -11$$

$$11d = -33 \Rightarrow d = -3$$

70.

Let the five terms of an A.P be $a - 2d$, $a - d$, a , $a + d$, $a + 2d$

$$(a + 2d)^2 - (a - 2d)^2 = 192, \quad a - d + a + d = 16 \Rightarrow 2a = 16 \Rightarrow a = 8$$

$$a^2 + 4ad + 4d^2 - a^2 + 4ad - 4d^2 = 192 \Rightarrow 8ad = 192$$

$$d = \frac{192}{8a} = \frac{192}{8 \times 8} = 3$$

The terms of an A.P $(8 - 6)$, $(8 - 3)$, 8 , $(8 + 3)$, $(8 + 6)$

2, 5, 8, 11, 14

71.

$$a_n = S_n - S_{n-1}$$

$$a + (n - 1)d = 210 - 171$$

$$a_n = 39$$

$$S_n = \frac{n}{2} [a + a_n]$$

$$210 = \frac{n}{2} [3 + 39]$$

$$210 = \frac{n}{2} [42]$$

$$210 = 21n$$

$$n = \frac{210}{21}$$

$$n = 10$$

$$a_n = a + (n - 1)d = 39$$

$$3 + 9d = 39$$

$$9d = 39 - 3$$

$$9d = 36$$

$$d = \frac{36}{9}$$

$$d = 4$$

\therefore A.P is a , $a+d$, $a+2d$

3 , $3+4$, $3+2(4)$

3, 7, 11,

$$\begin{aligned} a_{20} &= a + 19d \\ &= 3 + 19 \times 4 \\ &= 3 + 76 \\ &= 79 \end{aligned}$$

72.

The angles of a pentagon are $a, a+d, a+2d, a+3d, a+4d$

$$\begin{aligned} \text{The sum of Interior angles of pentagon are} &= (n - 2) 180^\circ \\ &= (5 - 2)180^\circ \\ &= 3 \times 180^\circ \\ &= 540^\circ \end{aligned}$$

$$a, a + d, a + 2d, a + 3d, a + 4d = 540^\circ$$

$$72, 72 + d, 72 + 2d, 72 + 3d, 72 + 4d = 540^\circ$$

$$360^\circ + 10d = 540^\circ$$

$$10d = 540^\circ - 360^\circ$$

$$10d = 180^\circ$$

$$d = \frac{180}{10}$$

$$d = 18^\circ$$

Angles of pentagon are $a, a+d, a+2d, a+3d, a+4d$

$$72, 72 + 18, 72 + 2(18), 72 + 3(18), 72 + 4(18)$$

$$72^\circ, 90^\circ, 108^\circ, 126^\circ, 144^\circ$$

73.

The earnings from Monday to Saturday

$$a, a + d, a+2d, a + 3d, a + 4d, a + 5d$$

From the data $a + a + d + a+2d = 525$

$$3a + 3d = 525 \text{ (divide by 3)}$$

$$a + d = 175 \text{ (1)}$$

$$a + 4d = a + 100$$

$$4d = 100$$

$$d = \frac{100}{4}$$

$$d = 25$$

substitute the value of 'd' in equation (1)

$$a + d = 175$$

$$a + 25 = 175$$

$$a = 175 - 25$$

$$a = 150$$

Daily earnings of a man =

$$a, a + d, a + 2d, a + 3d, a + 4d, a + 5d$$

$$150, 150 + 25, 150 + 2 \times 25, 150 + 3 \times 25, 150 + 4 \times 25, 150 + 5 \times 25$$

$$150, 175, 200, 225, 250, 275$$

74.

angles of quadrilateral be $a, a+d, a, a + 2d, a + 3d$

$$\therefore a + a + d + a + a + 2d + a + 3d = 360^\circ.$$

$$4a + 6d = 360^\circ \quad (\text{divide by } 2)$$

$$2a + 3d = 180^\circ$$

sum of opposite angles = 130°

$$a + a + 2d = 130^\circ$$

$$a + d + a + 3d = 130^\circ$$

$$2a + 2d = 130^\circ \quad (\text{divide by } 2)$$

$$2a + 4d = 130^\circ$$

$$a + 2d = 65^\circ$$

$$a + d = 65^\circ \dots\dots\dots(2)$$

$$2a + 3d = 180^\circ \dots\dots\dots(1) \times 1$$

$$a + d = 65^\circ \dots\dots\dots(2) \times 2$$

$$2a + 3d = 180^\circ$$

$$2a + 2d = 130^\circ$$

$$(-) \quad (-) \quad (-)$$

$$d = 50^\circ$$

substitute value of d in equation (2)

$$a + d = 65^\circ$$

$$a + 50^0 = 65^0$$

$$a = 65^0 - 50^0$$

$$a = 15^0$$

∴ angles of a quadrilateral a, a+d, a, a + 2d, a + 3d

$$15^0, 15^0 + 50^0, 15^0 + 2(50^0), 15^0 + 3(50^0)$$

$$15^0, 65^0, 115^0, 165^0$$

75.

$$n = 16$$

$$S_{16} = 768$$

$$a_n = 1 = 93$$

$$S_n = \frac{n}{2} [a + a_n]$$

$$768 = \frac{16}{2} [a + 93]$$

$$= 8 [a + 93]$$

$$\frac{768}{8} = a + 93$$

$$a + 93 = 96$$

$$a = 96 - 93$$

$$a = 3$$

$$a_n = a + (n - 1)d$$

$$93 = 3 + (16 - 1)d$$

$$93 = 3 + 15d$$

$$93 - 3 = 15d$$

$$90 = 15d$$

$$\frac{90}{15} = d$$

$$d = 6$$

A.P is 3,9,15,21,27

$$S_{16} = 3+9+15+21+27 \dots\dots\dots 16 \text{ terms}$$

$$= 3 (1+3+5+7\dots\dots 16 \text{ terms})$$

$$= 3 \times 16^2 \quad [S_n=n^2] \{ \text{the sum of first n odd numbers} \}$$

$$= 3 \times 256$$

$$768 = 768$$

76.

$$a_n = a + (n - 1)d$$

$$a_7 = 5 \times a_2$$

$$a + 6d = 5(a + d)$$

$$a + 6d = 5a + 5d$$

$$6d - 5d = 5a - a$$

$$d = 4a \dots\dots\dots (1)$$

$$a_5 = 2a_3 - 1$$

$$a + 4d = 2(a + 2d) - 1$$

$$a + 4d = 2a + 4d - 1$$

$$1 = 2a + 4d - 4d - a$$

$$a = 1$$

from equation (1) $d = 4a = 4 \times 1$

$$d = 4$$

Arithmetic progression is

$$= a, a + d, a + 2d \dots\dots$$

$$= 1, 1 + 4, 1 + 2(4) \dots\dots$$

$$= 1, 5, 9 \dots\dots\dots$$

$$a_{15} = a + (n - 1)d$$

$$= 1 + (15 - 1)4$$

$$= 1 + 14 \times 4$$

$$= 1 + 56$$

$$a_{15} = 57$$

77.

$$\frac{S_8}{S_{11}} = \frac{3}{2}$$

$$2 [S_8] = 3 [S_{11}]$$

$$2 [4(3a + 7d)] = 3 \left[\frac{11}{2} (2a + 10d) \right]$$

$$2 [12a + 28d] = 3 [11a + 55d]$$

$$24a + 56d = 33a + 165d$$

$$9a + 109d = 0$$

77.

$$a_7 = 4a_2$$

$$a + 6d = 4(a + d)$$

$$a + 6d = 4a + 4d$$

$$3a = 2d \dots\dots\dots(1)$$

$$a_{12} = 3a_4 + 2$$

$$a + 11d = 3(a + 3d) + 2$$

$$a + 11d = 3a + 9d + 2$$

$$2a - 2d = - 2$$

$$a - d = -1$$

$$a = d - 1 \dots\dots\dots(2)$$

substitute equation (2) in equation (1)

$$3(d - 1) = 2d$$

$$3d - 3 = 2d$$

$$d = 3$$

substitute the value of 'd' in equation (2)

$$a = 3 - 1$$

$$a = 2$$

Arithmetic Progression is

$$a, a + d, a + 2d, \dots\dots\dots$$

$$2, 2 + 3, 2 + 2(3)$$

$$2, 5, 8, \dots\dots$$

79.

$$a_p = q, \quad a_q = p, \quad a_r = ?$$

$$q = a + (p - 1)d$$

$$p = a + (q - 1)d$$

$$q - p = a + (p - 1)d - [a + (q - 1)d] = a + d(p - 1 - q + 1) - a = d(p - q)$$

$$\therefore d = \frac{q - p}{p - q} = -1 \quad \dots\dots\dots(1)$$

$$a = q + p - 1 \quad \dots\dots\dots(2)$$

$$a_r = a + (r - 1)d = q + p - 1 + (r - 1)(-1)$$

$$= q + p - 1 - r + 1 = p + q - r$$

$$80. S_5 = \frac{5}{2} [2a + (5 - 1) d]$$

$$a_4 = (a_1 + a_2) + 5$$

$$S_5 = \frac{5}{2} [2a + 4d]$$

$$a + 3d = (2a + d) + 5$$

$$S_5 = 5 (a + 2d)$$

$$a - 2d = -5 \dots\dots\dots (2)$$

$$55 = 5 (a + 2d)$$

$$11 = a + 2d \dots\dots\dots (1)$$

$$-5 = a - 2d \dots\dots\dots (2)$$

$$(1) + (2)$$

$$2a = 6$$

$$a = 3$$

substitute the value of a in equation in (1)

$$11 = 3 + 2d$$

$$8 = 2d$$

$$d = 4$$

Let the five terms of an A.P be

$$a , a+d, a+2d , a+3d , a+4d$$

$$3 , 3+4 , 3+2(4) , 3+3(4) , 3+4(4)$$

$$3, 7, 11, 15, 19$$

$$3 , 7 , 11 , 15 , 19$$

81.

$$a+(6-1)d = 2 (a+(3-1)d)+1$$

$$a + 5d = 2a + 4d + 1$$

$$d - a = 1 \text{ or } a = d - 1 \dots\dots\dots(1)$$

$$a_4 + a_5 = 5a_2$$

$$(a+(4-1)d) + (a + (5-1)d) = 5 (a + d)$$

$$a + 3d + a + 4d = 5a + 5d$$

$$2a + 7d = 5a + 5d$$

$$2d = 3a \dots\dots\dots(2)$$

substitute equation (1) in equation (2)

$$2d = 3a$$

$$2d = 3(d - 1)$$

$$2d = 3d - 3$$

$$d = 3$$

substitute value of d in equation (2)

$$2d = 3a$$

$$2(3) = 3a$$

$$a = 2$$

$$a_{10} = a + 9d$$

$$a_{10} = 2 + 9(3)$$

$$a_{10} = 2 + 27$$

$$a_{10} = 29$$

82.

$$S_n = 5n - n^2$$

$$S_1 = 5(1) - (1)^2 = 5 - 1 = 4 \quad a_1 = 4$$

$$S_2 = 5(2) - (2)^2 = 10 - 4 = 6 \quad a_2 = S_2 - S_1 = 6 - 4 = 2$$

$$S_3 = 5(3) - (3)^2 = 15 - 9 = 6 \quad a_3 = S_3 - S_2 = 6 - 6 = 0$$

$$S_4 = 5(4) - (4)^2 = 20 - 16 = 4 \quad a_4 = S_4 - S_3 = 4 - 6 = -2$$

$$S_{21} = 5(21) - (21)^2 = 105 - 441 = -336$$

$$a_{21} = a + 20d = 4 + 20(-2) = 4 - 40 = -36$$

83.

$$a = b + 3 \quad \dots\dots(i)$$

$$a_7 = 28$$

$$a + 6d = 28 \quad \dots\dots(ii)$$

$$b_8 = 29$$

$$b + 7d = 29 \quad \dots\dots(iii)$$

substitute equation (2) in equation (1)

$$b + 3 + 6d = 28$$

$$b + 6d = 25 \quad \dots\dots(iv)$$

$$(iii) - (iv)$$

$$b + 7d = 29$$

$$b + 6d = 25$$

$$\begin{array}{r} (-) \quad (-) \quad (-) \\ \hline \end{array}$$

$$d = 4$$

substitute the value of $d = 4$ in equation (ii)

$$a + 6d = 28$$

$$a + 6(4) = 28$$

$$a + 24 = 28$$

$$a = 28 - 24$$

$$a = 4$$

substitute $d = 4$ in equation (iii)

$$b + 7d = 29$$

$$b + 7(4) = 29$$

$$b = 29 - 28$$

$$b = 1$$

First A.P is

$$a, a+d, a+2d, \dots$$

$$4, 4+4, 4+2(4), \dots$$

$$4, 8, 12, \dots$$

Second A.P is

$$b, b+d, b+2d, \dots$$

$$1, 1+4, 1+2(4), \dots$$

$$1, 5, 9, \dots$$

84.

$$a_{17} = 3a_5 + 4$$

$$a_{10} = 31 \quad a_{30}, a_{29}, a_{28} = ? \quad \text{A.P} = ?$$

$$a + 16d = 3(a + 4d) + 4$$

$$a + 9d = 31 \quad \dots \dots (2)$$

$$a + 16d = 3a + 12d + 4$$

$$a - 3a + 16d - 12d = 4$$

$$-2a + 4d = 4 \quad (\text{Divide by 2})$$

$$-a + 2d = 2 \quad \dots \dots (1)$$

$$(1) + (2) =$$

$$-a + 2d = 2$$

$$a + 9d = 31$$

$$11d = 33$$

$$d = \frac{33}{11}$$

$$d = 3$$

substitute value of d in equation (2)

$$a + 9d = 31$$

$$a + 9(3) = 31$$

$$a + 27 = 31$$

$$a = 31 - 27$$

$$a = 4$$

The last three terms of an A.P be

$$a_{30}, a_{29}, a_{28}$$

$$a + 29d, a + 28d, a + 27d$$

$$4 + 29(3), 4 + 28(3), 4 + 27(3)$$

$$4 + 87, 4 + 84, 4 + 81$$

$$91, 88, 85$$

Arithmetic Progression = $a, a+d, a+2d, \dots$

$$4, 4 + 3, 4 + 2(3), \dots$$

$$4, 7, 10, \dots$$

Unit : 06 TRIANGLES

I. Multiple choice Questions :

1. A) Any two equiangular triangle
2. A) Two isosceles triangles
3. C) 4.5 cm
4. C) 5 cm
5. C) $\angle B = \angle D$
6. B) 3
7. B) 4
8. C) 16
9. C) 1.5

10. C) $x = \frac{ay}{a+b}$
 11. C) 30cm
 12. C) 3 cm
 13. C) 8 cm
 14. B) 70°
 15. B) 3 cm
 16. C) 60cm
 17. B) $DP/PL = DC/BL$
 18. A) 64 cm
 19. A) 25m
 20. B) similar but not congruent
 21. B) $\frac{AD}{DE} = \frac{AE}{BC}$
 22. C) 8cm
 23. C) $\frac{AY}{AC}$
 24. A) $\frac{DG}{GB}$
 25. B) 7.5cm
 26. D) $\frac{x}{x+y} = \frac{m}{m+n}$
 27. A) PQ & AB
 28. B) 3 cm

II. One mark answering questions:

- 29) If any two polygons have same corresponding angles and same ratio of corresponding sides then the two polygons are called similar polygons.
- 30) 1. Corresponding angles should be same
 2. The ratio of Corresponding sides should be same.
- 31) Thales Theorem : “If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points , the other two sides are divided in the same ratio”
- 32) Angle-Angle-Angle(A-A-A) Criterion of similarity of two triangles :
 “If in two triangles, corresponding angles are equal, then their corresponding sides are in the same ratio(or proportion) and hence the two triangles are similar”
- 33) Angle-Angle-Angle(A-A-A) Criterion of similarity of two triangles
- 34) PR
- 35) 6CM
- 36) 6CM

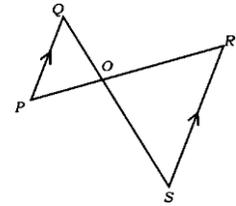
37) 2 cm

38) $OS:OQ = 2 : 1$

$\Delta POQ \sim \Delta ROS$

$$\therefore \frac{PQ}{SR} = \frac{OQ}{OS} = \frac{1}{2}$$

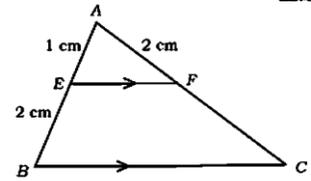
$$\therefore OS : OQ = 2: 1$$



39) $\frac{AE}{EB} = \frac{AF}{FC}$

$$\frac{1}{2} = \frac{2}{FC}$$

$$FC = 2 \times 2 = 4$$



III. Two marks questions

40)

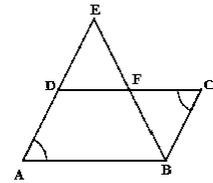
1) In ΔABC and ΔCFB

$\angle A = \angle C$ (opposite angles of parallelogram))

$\angle AEB = \angle CBF$ ($AF \parallel BC$, alternate angles)

So, by AA similarity criteria

$\Delta ABC \sim \Delta CFB$



41) According Thales

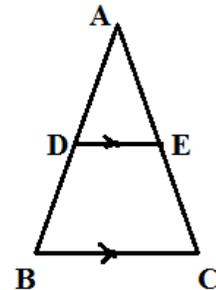
$$\frac{AD}{AB} = \frac{AE}{AC}$$

$$\frac{2.4}{3} = \frac{AE}{5}$$

$$AE = \frac{2.4 \times 5}{3}$$

$$AE = 0.8 \times 5$$

$$AE = 4 \text{ cm}$$



42) Length of vertical pole , $AB = 6 \text{ cm}$

Length of shadow casts by pole , $BC = 4 \text{ cm}$

Length of shadow casts by tower, $EF = 28 \text{ cm}$

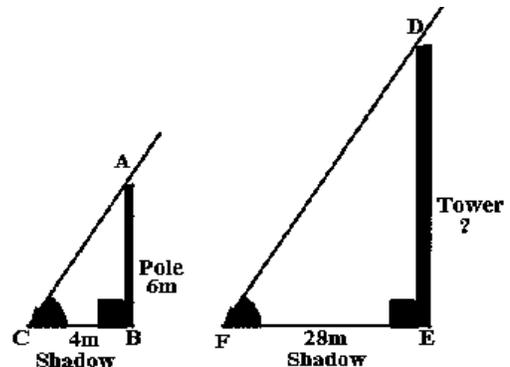
Let the height of the tower be , $DE = h$

In ΔABC and ΔDEF

$$\angle C = \angle F$$

$$\angle B = \angle E = 90^\circ$$

$\Delta ABC \sim \Delta DEF$ (AA Similarity criteria)



$$\therefore \frac{AB}{NE} = \frac{BC}{EF} \quad (\text{corresponding sides of the similar triangles})$$

$$\frac{6}{h} = \frac{4}{28}$$

$$h = \frac{6 \times 28}{4}$$

$$h = 6 \times 7$$

$$h = 42 \text{ cm}$$

Hight of the tower

43)

In $\triangle ACO$ and $\triangle BDO$

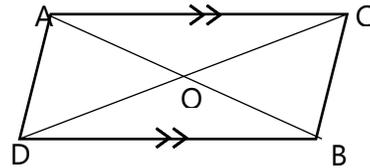
$$\angle CAO = \angle DBO \quad (\text{alternate angles } AC \parallel BD)$$

$$\angle ACO = \angle BDO$$

$$\angle AOC = \angle BOD \quad (\text{verticle angles})$$

By A A A Similarity criteria

$$\therefore \triangle AOC \sim \triangle BOD$$

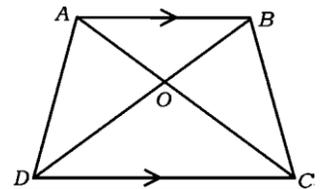


44) In $\triangle AOB$ and $\triangle DOC$ $\angle AOB = \angle DOC$ AND $\angle ABO = \angle ODC$

$$\angle BAO = \angle OCD$$

$$\therefore \triangle AOB \sim \triangle DOC$$

$$\therefore \frac{AO}{BO} = \frac{CO}{DO}$$



45) In $\triangle ABC$, $DE \parallel BC$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC} \quad [\because \text{Thales Theorem}]$$

$$\frac{x}{x-2} = \frac{x+2}{x-1}$$

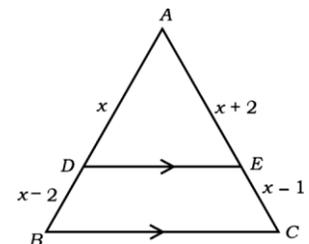
Cross multiplication

$$x(x-1) = (x-2)(x+2)$$

$$x^2 - x = x^2 - 4$$

$$-x = -4$$

$$x = 4$$



$$\therefore \frac{AD}{DB} = \frac{X}{X-2} = \frac{4}{4-2} = \frac{4}{2} = \frac{2}{1}$$

$$\therefore AD:DB = 2:1$$

46) DOB is a straight line

$$\therefore \angle DOC + \angle COB = 180^\circ$$

$$\therefore \angle DOC = 180^\circ - 125^\circ = 55^\circ$$

In $\triangle DOC$

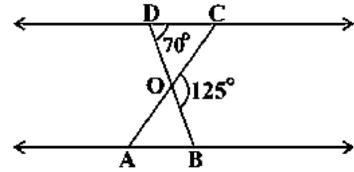
$$\angle DCO + \angle CDO + \angle DOC = 180^\circ$$

$$\angle DCO + 70^\circ + 55^\circ = 180^\circ$$

$$\angle DCO = 180^\circ - 125^\circ = 55^\circ$$

So $\triangle ODC \sim \triangle OBA$

$$\therefore \angle OAB = 55^\circ$$



47. ABC is an isosceles triangle

$$AB = AC$$

$$\angle B = \angle C \text{ (opposite sides of equal angles)}$$

$$\angle ABD = \angle ECF$$

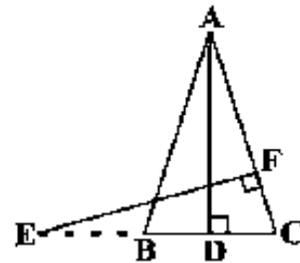
In $\triangle ABD$ and $\triangle ECF$

$$\angle ADB = \angle EFC = 90^\circ$$

$$\therefore \angle ABD = \angle ECF$$

By AA similarity criteria

$$\triangle ABD \sim \triangle ECF$$



48) In $\triangle PQR$

$$\angle PQR = \angle PRQ \text{ (data)}$$

$$PQ = PR$$

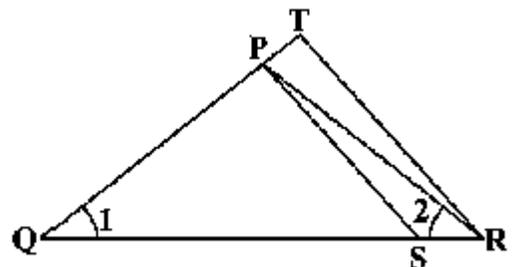
but

$$\frac{QR}{QS} = \frac{QT}{PR}$$

from (1)

$$\frac{QR}{QS} = \frac{QT}{PQ} \text{ -----2}$$

In $\triangle PQS$ and $\triangle TQR$



$$\frac{QR}{QS} = \frac{QT}{PQ} \quad (\text{from equation 2})$$

$$\angle Q = \angle Q \quad (\text{common angle})$$

$$\therefore \triangle PQS \sim \triangle TQR$$

IV. Three marks questions

49) In $\triangle ABC$ and $\triangle ADC$

$$\angle BAC = \angle ADC \quad [\text{data}]$$

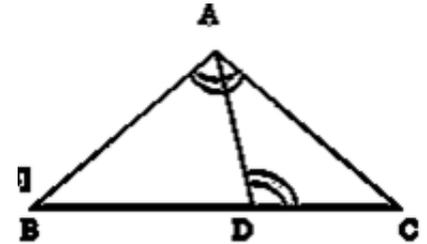
$$\angle ACB = \angle ACD \quad (\text{common angle})$$

$$\therefore \angle ABC = \angle DAC$$

$$\therefore \triangle ABC \sim \triangle DAC \quad [\text{A A similarity criteria}]$$

$$\frac{AC}{CD} = \frac{BC}{AC}$$

$$\therefore AC^2 = BC \cdot CD$$



50)

In $\triangle OAP$ and $\triangle OQC$

$$\angle OAP = \angle QCO \quad (\because AB \parallel CD \text{ alternate angles})$$

$$\angle AOP = \angle QOC \quad (\because \text{verticle angle})$$

$$\angle APO = \angle OQC \quad (\because \text{third angle})$$

$$\therefore \triangle OAP \sim \triangle OQC \quad (\because \text{A A criteria})$$

$$\frac{OA}{OC} = \frac{AP}{CQ}$$

$$\text{so } CQ = \frac{1}{5} CD \text{ and } AP = \frac{2}{5} AB$$

$$\frac{OA}{OC} = \frac{\frac{2}{5} AB}{\frac{1}{5} CD}$$

But $AB = CD$ (opposite angles of the parallelogram)

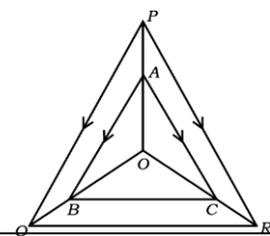
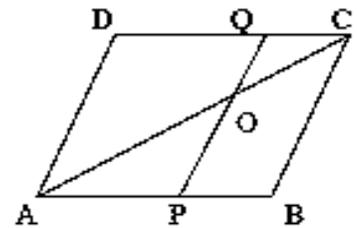
$$\frac{OA}{OC} = \frac{\frac{2}{5} AB}{\frac{1}{5} CD}$$

$$\frac{OA}{OC} = \frac{2}{5} \times \frac{5}{1}$$

$$\frac{OA}{OC} = 2$$

$$\therefore OA = 2OC$$

51) In $\triangle OPQ$, $AB \parallel PQ$



$$\therefore \frac{OA}{AP} = \frac{OB}{BQ} \dots \dots \dots (1) \quad (\because \text{Thales theorem})$$

In $\triangle OPR$, $AC \parallel PR$

$$\therefore \frac{OC}{CR} = \frac{OA}{AP} \dots \dots \dots (2) \quad (\text{Thales theorem})$$

From (1) and (2), we get

$$\frac{OB}{BQ} = \frac{OC}{CR}$$

$$\therefore BC \parallel QR \quad (\because \text{Converse of Thales theorem})$$

52)

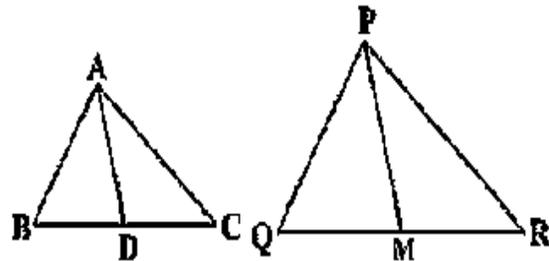
In $\triangle ABC$ and $\triangle PQR$

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AD}{PM}$$

To prove : $\triangle ABC \sim \triangle PQR$

Proof :

$$\frac{AB}{PQ} = \frac{\frac{1}{2}BC}{\frac{1}{2}QR} = \frac{AD}{PM} \dots \dots \dots (1)$$



$$\frac{AB}{PQ} = \frac{BD}{QM} = \frac{AD}{PM} \quad (\text{D is midpoint of BC \& M is midpoint of QR})$$

$\Rightarrow \triangle ABD \sim \triangle PQM$ (S S S similarity criteria)

$\therefore \angle ABD = \angle PQM$ (Corresponding angles of similar triangles)

$\therefore \angle ABC = \angle PQR$

Now In $\triangle ABC$ and $\triangle PQR$

$$\frac{AB}{PQ} = \frac{BC}{QR}$$

$\angle ABC = \angle PQR$

$\therefore \triangle ABC \sim \triangle PQR$

53)

$ST \parallel QR$ (\because Converse of Thales theorem)

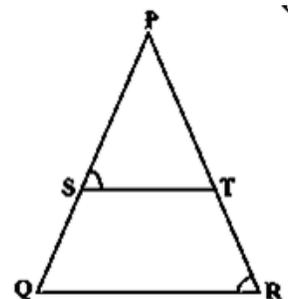
$$\angle PST = \angle PQR \quad (\because \text{Corresponding angles}) \dots \dots (1)$$

$$\angle PST = \angle PRQ \quad (\because \text{data}) \dots \dots (2)$$

$$\Rightarrow \angle PRQ = \angle PQR$$

$$\therefore PQ = PR$$

$\triangle PQR$ is an isosceles triangle



V. Four/ Five marks questions

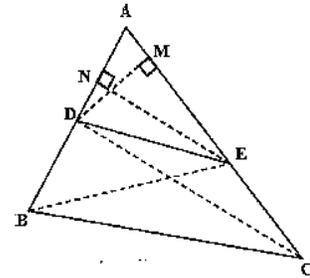
54) State and prove Thales theorem.

Statement : “If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points , the other two sides are divided in the same ratio” (Thales theorem)

Data : In $\triangle ABC$, the line DE drawn parallel to intersects AB and AC at D and E

To prove : $\frac{AD}{DB} = \frac{AE}{EC}$

Construction : join BE and DC , draw $DM \perp AC$, and $EN \perp AB$



Proof : In $\triangle ADE$ & $\triangle DBE$

$$\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle DBE} = \frac{\frac{1}{2}AD \times EN}{\frac{1}{2}BD \times EN}$$

$$\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle DBE} = \frac{AD}{BD} \text{ -----1}$$

In $\triangle ADE$ & $\triangle ECD$

$$\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle ECD} = \frac{\frac{1}{2}AE \times DM}{\frac{1}{2}EC \times DM}$$

$$\frac{\text{Area of } \triangle ADE}{\text{Area of } \triangle ECD} = \frac{AE}{EC} \text{ -----2}$$

$\triangle BDE$ and $\triangle DEC$ stand on same base DE and in between $BC \parallel DE$

\therefore Area of $\triangle BDE$ = Area of $\triangle ECD$

From (1) and (2)

$$\frac{AD}{DB} = \frac{AE}{EC}$$

55) Prove that “ If in two triangles, corresponding angles are equal, then their

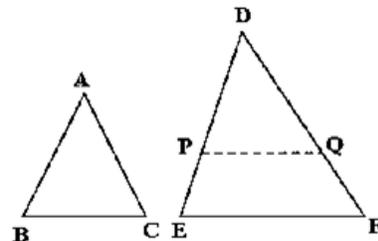
corresponding sides are in the same ratio (or proportion) and hence the two triangles are similar

Data : In triangles $\triangle ABC$ and $\triangle DEF$ $\angle A = \angle D$, $\angle B = \angle E$, $\angle C = \angle F$

To prove : $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$

Construction : Cut $AB=DP$, and $AC = DQ$ on DE & DF at P & Q , join PQ

Proof : In $\triangle ABC$ and $\triangle DPQ$,



$AB = DP, AC = DQ$ (construction)
 $\triangle BAC = \triangle PDQ$ (data)
 $\triangle ABC \cong \triangle DPQ$ (SAS congruency rule .)

$$\triangle ABC = \triangle DPQ$$

But $\triangle ABC = \triangle DEF$

$$\therefore \triangle DPQ = \triangle DEF$$

$PQ \parallel EF$ (Since corresponding angles equal.)

$$\frac{DP}{DE} = \frac{PQ}{EF} = \frac{DQ}{DF} \text{-----1}$$

But $AB = DP, BC = DQ$

$$\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$$

56) Data : In $\triangle ABC$ and $\triangle DEF$ $\frac{AB}{DE} = \frac{AC}{DF} = \frac{BC}{EF}$ ----- (1)

To prove : $\angle A = \angle D, \angle B = \angle E$ and $\angle C = \angle F$ and $\triangle ABC \cong \triangle DEF$

Construction : take P and Q points on DE and DF so that $AB = DP$ and $AC = DQ$ then join PQ

Proof : $\frac{AB}{DE} = \frac{AC}{DF} \Rightarrow \frac{DP}{DE} = \frac{DQ}{DF}$ ($\because DP = AB, DQ = AC$)

$$\Rightarrow \frac{DE}{DP} = \frac{DF}{DQ} \text{ (Inverse)}$$

$$\Rightarrow \frac{DE}{DP} - 1, \frac{DF}{DQ} - 1,$$

$$\Rightarrow \frac{DE-DP}{DP} = \frac{DF-DQ}{DQ}$$

$$\Rightarrow \frac{PE}{DP} = \frac{QE}{DQ}$$

$$\Rightarrow \frac{DP}{PE} = \frac{DQ}{QE} \text{ (inverse)}$$

$\therefore PQ \parallel EF$ (\because Thales theorem)

$$\therefore \angle P = \angle E \text{ and } \angle Q = \angle F$$

$\therefore \triangle DPQ = \triangle DEF$ (AA similarity criteria)

There fore $\frac{DP}{DE} = \frac{DQ}{DF} = \frac{PQ}{EF}$ ----- (2)

If $AB = DP, AC = DQ$

$$\frac{DP}{DE} = \frac{DQ}{DF} = \frac{BC}{EF} \text{----- (3)}$$

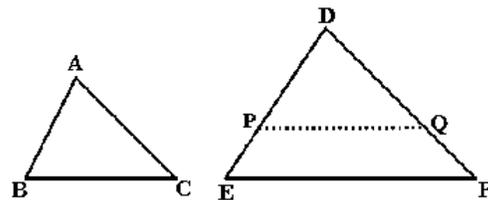
From (2)and (3)

$$BC = PQ$$

In $\triangle ABC$ and $\triangle DPQ$

$$BC = PQ$$

$$AB = DP$$



$$AC = DQ$$

$$\Delta ABC \cong \Delta DPQ$$

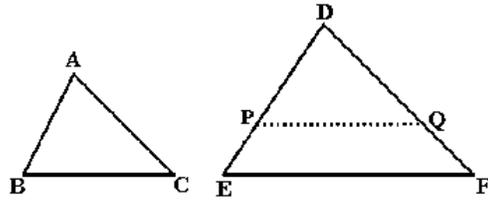
$$\therefore \angle A = \angle D, \angle B = \angle P, \text{ \& } \angle C = \angle Q,$$

$$\Rightarrow \angle A = \angle D, \angle B = \angle E, \text{ \& } \angle C = \angle F \\ \text{ \& } \Delta ABC \sim \Delta DEF$$

57)

Data :In ΔABC and ΔDEF

$$\angle A = \angle D, \text{ and } \frac{AB}{DE} = \frac{AC}{DF}$$



To prove : $\Delta ABC \sim \Delta DEF$

Construction: take P and Q points on DE and DF so that $AB = DP$ and $AC = DQ$ then join PQ

Proof :

In ΔABC and ΔDPQ

$$AB = DP \quad (\text{construction})$$

$$AC = DQ \quad (\text{construction})$$

$$\angle A = \angle D, \quad (\text{data})$$

$$\Delta ABC \cong \Delta DPQ \quad (\text{SAS})$$

$$\therefore \angle B = \angle P,$$

$$\angle C = \angle Q, \quad (\text{corresponding sides of similar triangles}) \text{ ----- (1)}$$

$$\frac{AB}{DE} = \frac{AC}{DF} \quad (\text{data})$$

$$\frac{DP}{DE} = \frac{DQ}{DF} \quad (\text{AB} = \text{DP} \text{ \& } \text{AC} = \text{DQ})$$

$$\therefore PQ \parallel EF \quad (\text{converse of thales})$$

$$\therefore \angle E = \angle P,$$

$$\angle F = \angle Q, \quad \text{-----(2)}$$

From (1) and (2)

$$\angle B = \angle E, \quad \angle C = \angle F, \text{ \& } \angle A = \angle D,$$

$$\therefore \Delta ABC \sim \Delta DEF$$

Unit : 07 COORDINATE GEOMETRY

I. Multiple Choice questions

- 1) A) (x , 0)
- 2) D) (0 , y)
- 3) A) 2 Units
- 4) D) -4 Units
- 5) C) (0, 0)
- 6) D) $\sqrt{a^2 + b^2}$
- 7) C) $\sqrt{x^2 + y^2}$

- 8) A) ± 3
 9) C) (3, 5)
 10) B) (-3, 4)
 11) B) 3
 12) A) $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
 13) D) -5
 14) D) (-2, 0)

II. One Mark Questions :

- 15) $P(-3, 5) = (x, y)$ $OP = \sqrt{x^2 + y^2}$
 $OP = \sqrt{(-3)^2 + 5^2}$
 $OP = \sqrt{9 + 25} = \sqrt{34}$ Units
- 16) $P(6, 8) = (x, y)$ $OP = \sqrt{x^2 + y^2}$
 $OP = \sqrt{6^2 + 8^2} = \sqrt{36 + 64} = \sqrt{100} = 10$ Units
- 17) $P(x, y) = \left[\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right]$
- 18) $(5, 4) = (x_1, y_1),$ $(1, 4) = (x_2, y_2)$
 $P(x, y) = \left[\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right]$
 $P(x, y) = \left[\frac{5 + 1}{2}, \frac{4 + 4}{2} \right]$
 $P(x, y) = \left[\frac{6}{2}, \frac{8}{2} \right] = (3, 4)$
- 19) $(2, 3) = (x_1, y_1),$ $(4, 3) = (x_2, y_2)$
 $P(x, y) = \left[\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right]$
 $P(x, y) = \left[\frac{2 + 4}{2}, \frac{3 + 3}{2} \right]$
 $P(x, y) = \left[\frac{6}{2}, \frac{6}{2} \right] = (3, 3)$
- 20) $(3, 4) = (x_1, y_1),$ $(5, 6) = (x_2, y_2)$
 $P(x, y) = \left[\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right]$

$$P(x, y) = \left[\frac{3+5}{2}, \frac{4+6}{2} \right]$$

$$P(x, y) = \left[\frac{8}{2}, \frac{10}{2} \right] = (4, 5)$$

21) $(6, 3) = (x_1, y_1), \quad (4, 5) = (x_2, y_2) \quad P(x, y) = (5, 5)$

$$P(x, y) = \left[\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right]$$

$$(5, 5) = \left[\frac{6+4}{2}, \frac{3+y}{2} \right]$$

$$(5, 5) = \left[\frac{10}{2}, \frac{3+y}{2} \right]$$

$$5 = \frac{3+y}{2}$$

$$\Rightarrow 10 = 3 + y$$

$$10 - 3 = y \Rightarrow y = 7$$

$$\therefore y = 7$$

22) $P(x, y) = \left[\frac{m_1x_2+m_2x_1}{m_1+m_2}, \frac{m_1y_2+m_2y_1}{m_1+m_2} \right]$

23) $P(x, y) = \left[\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right]$

III. Two Marks Questions :-

IV.

24) $P(2, 3) = (x_1, y_1), \quad Q(4, 1) = (x_2, y_2)$

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(4 - 2)^2 + (1 - 3)^2}$$

$$= \sqrt{2^2 + (-2)^2}$$

$$= \sqrt{4 + 4} = \sqrt{8} = \sqrt{4 \times 2} = 2\sqrt{2}$$

$$\therefore PQ = 2\sqrt{2} \text{ Units}$$

25) $P(2, 4) = (x_1, y_1), \quad Q(8, 12) = (x_2, y_2)$

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(8 - 2)^2 + (12 - 4)^2}$$

$$= \sqrt{6^2 + 8^2}$$

$$= \sqrt{36 + 64} = \sqrt{100} = 10$$

$$\therefore PQ = 10 \text{ Units}$$

26) $P(5, 6) = (x_1, y_1), \quad Q(1, 3) = (x_2, y_2)$

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\begin{aligned}
&= \sqrt{(1-5)^2 + (3-6)^2} \\
&= \sqrt{(-4)^2 + (-3)^2} \\
&= \sqrt{16+9} = \sqrt{25} = 5
\end{aligned}$$

$\therefore \mathbf{PQ} = \mathbf{5}$ Units

27) $P(-5, 7) = (x_1, y_1), \quad Q(-1, 3) = (x_2, y_2)$

$$\begin{aligned}
PQ &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
&= \sqrt{[-1 - (-5)]^2 + (3 - 7)^2} \\
&= \sqrt{(-1 + 5)^2 + (-4)^2} \\
&= \sqrt{4^2 + 16} = \sqrt{16 + 16} = \sqrt{16 \times 2} = 4\sqrt{2}
\end{aligned}$$

$\therefore \mathbf{PQ} = 4\sqrt{2}$ Units

28) $A(2, 6) = (x_1, y_1), \quad B(5, 10) = (x_2, y_2)$

$$\begin{aligned}
AB &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
&= \sqrt{(5 - 2)^2 + (10 - 6)^2} \\
&= \sqrt{3^2 + 4^2} \\
&= \sqrt{9 + 16} = \sqrt{25} = 5
\end{aligned}$$

$\therefore \mathbf{AB} = \mathbf{5}$ Units

29) $A(5, -7) = (x_1, y_1), \quad B(1, -3) = (x_2, y_2)$

$$\begin{aligned}
PQ &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
&= \sqrt{(1 - 5)^2 + [-3 - (-7)]^2} \\
&= \sqrt{(-4)^2 + (-3 + 7)^2} \\
&= \sqrt{16 + (4)^2} = \sqrt{16 + 16} = \sqrt{32} = \sqrt{16 \times 2} = 4\sqrt{2}
\end{aligned}$$

$\therefore \mathbf{PQ} = 4\sqrt{2}$ Units

30) $P(2, -3) = (x_1, y_1) \quad Q(10, y) = (x_2, y_2), \quad \text{Distance between PQ} = 10 \text{ Units} \quad y = ?$

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$10 = \sqrt{(10 - 2)^2 + [(y - (-3))]^2}$$

$$10 = \sqrt{(8)^2 + (y + 3)^2}$$

$$10 = \sqrt{64 + (y + 3)^2} \quad \text{[Squaring on both sides]}$$

$$10^2 = [\sqrt{64 + (y + 3)^2}]^2$$

$$100 = 64 + (y + 3)^2$$

$$100 - 64 = (y + 3)^2$$

$$36 = (y + 3)^2$$

$$\sqrt{36} = (y + 3)$$

$$(y + 3) = \sqrt{36} = \pm 6$$

$$(y + 3) = \mp 6$$

$$y + 3 = +6 \quad \text{OR} \quad y + 3 = -6$$

$$y = 6 - 3 \quad y = -6 - 3$$

$$y = 3 \quad y = -9$$

$$\therefore y = 3 \quad \text{OR} \quad y = -9$$

$$31) P(3, 1) = (x_1, y_1) \quad Q(0, x) = (x_2, y_2), \quad \text{Distance between PQ} = 5 \text{ Units} \quad x = ?$$

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$5 = \sqrt{(0 - 3)^2 + (x - 1)^2}$$

$$5 = \sqrt{(-3)^2 + (x - 1)^2}$$

$$5 = \sqrt{9 + (x - 1)^2} \quad [\text{Squaring on both sides}]$$

$$5^2 = [\sqrt{9 + (x - 1)^2}]^2$$

$$25 = 9 + (x - 1)^2$$

$$25 - 9 = (x - 1)^2$$

$$16 = (x - 1)^2$$

$$\sqrt{16} = (x - 1)$$

$$4 = x - 1 \Rightarrow 4 + 1 = x$$

$$\Rightarrow x = 5$$

$$32) \text{ Coordinates of the point } P = P(1, 1) = (x_1, y_1),$$

$$\text{Coordinates of the point } Q = Q(5, 4) = (x_2, y_2),$$

$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(5 - 1)^2 + (4 - 1)^2}$$

$$= \sqrt{(4)^2 + (3)^2}$$

$$= \sqrt{16 + 9} = \sqrt{25} = 5$$

$$\therefore PQ = 5 \text{ Units}$$

33) $A(-6, 10) = (x_1, y_1)$, $B(3, -8) = (x_2, y_2)$, $P(-4, 6) = (x, y)$, $m_1 : m_2 = ?$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$(-4, 6) = \left[\frac{m_1(3) + m_2(-6)}{m_1 + m_2}, \frac{m_1(-8) + m_2(10)}{m_1 + m_2} \right]$$

$$(-4, 6) = \left[\frac{3m_1 - 6m_2}{m_1 + m_2}, \frac{-8m_1 + 10m_2}{m_1 + m_2} \right]$$

$$-4 = \frac{3m_1 - 6m_2}{m_1 + m_2} \quad \text{OR} \quad 6 = \frac{-8m_1 + 10m_2}{m_1 + m_2}$$

$$-4(m_1 + m_2) = 3m_1 - 6m_2$$

$$-4m_1 - 4m_2 = 3m_1 - 6m_2$$

$$-4m_1 - 3m_1 = -6m_2 + 4m_2$$

$$-7m_1 = -2m_2$$

$$\frac{m_1}{m_2} = \frac{-2}{-7} = \frac{2}{7}$$

$$\therefore m_1 : m_2 = 2 : 7$$

34) $A(4, -3) = (x_1, y_1)$, $B(8, 5) = (x_2, y_2)$, $m_1 : m_2 = 3 : 1$, $P(x, y) = ?$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{3(8) + 1(4)}{3 + 1}, \frac{3(5) + 1(-3)}{3 + 1} \right]$$

$$= \left[\frac{24 + 4}{4}, \frac{15 - 3}{4} \right]$$

$$= \left[\frac{28}{4}, \frac{12}{4} \right] = [7, 3]$$

$$\therefore P(x, y) = [7, 3]$$

35) $A(-1, 7) = (x_1, y_1)$, $B(4, -3) = (x_2, y_2)$, $m_1 : m_2 = 2 : 3$, $P(x, y) = ?$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{2(4) + 3(-1)}{2 + 3}, \frac{2(-3) + 3(7)}{2 + 3} \right]$$

$$= \left[\frac{8 - 3}{5}, \frac{-6 + 21}{5} \right]$$

$$= \left[\frac{5}{5}, \frac{15}{5} \right] = [1, 3]$$

$$\therefore P(x, y) = [1, 3]$$

36) $(1, 6) = (x_1, y_1)$, $(4, 3) = (x_2, y_2)$, $m_1 : m_2 = 1 : 2$, $P(x, y) = ?$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$\begin{aligned}
 P(x, y) &= \left[\frac{1(4) + 2(1)}{1+2}, \frac{1(3) + 2(6)}{1+2} \right] \\
 &= \left[\frac{4+2}{3}, \frac{3+12}{3} \right] \\
 &= \left[\frac{6}{3}, \frac{15}{3} \right] = [2, 5]
 \end{aligned}$$

$$\therefore P(x, y) = [2, 5]$$

37) $A(1, -3) = (x_1, y_1)$, $B(8, 5) = (x_2, y_2)$, $m_1 : m_2 = 3 : 1$ $P(x, y) = ?$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{3(8) + 1(1)}{3 + 1}, \frac{3(5) + 1(-3)}{3 + 1} \right]$$

$$= \left[\frac{24 + 1}{4}, \frac{15 - 3}{4} \right]$$

$$= \left[\frac{25}{4}, \frac{12}{4} \right] = \left[\frac{25}{4}, 3 \right]$$

$$\therefore P(x, y) = \left[\frac{25}{4}, 3 \right]$$

38) Center of the circle is the mid point of the diameter

$B(x_2, y_2) = (1, 4)$, $P(x, y) = (2, -3)$, $A(x_1, y_1) = ?$

$$P(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$P(2, -3) = \left(\frac{x_1 + 1}{2}, \frac{y_1 + 4}{2} \right)$$

$$2 = \frac{x_1 + 1}{2}, \quad -3 = \frac{y_1 + 4}{2}$$

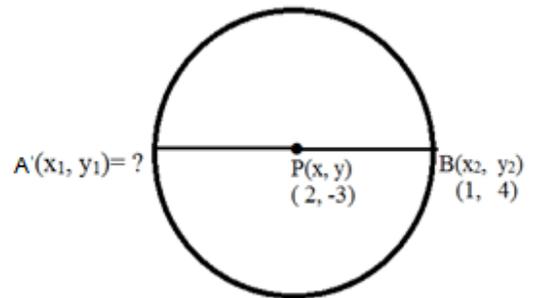
$$2 \times 2 = x_1 + 1 \quad -3 \times 2 = y_1 + 4$$

$$4 = x_1 + 1, \quad -6 = y_1 + 4$$

$$x_1 = 4 - 1 = 3, \quad y_1 = -6 - 4 = -10$$

$$x_1 = 3, \quad y_1 = -10$$

\therefore Coordinates of the point A = A (3, -10)



39) Centre of the circle is the mid point of the diameter

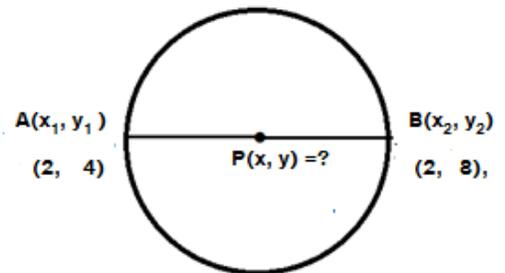
$A(x_1, y_1) = (2, 4)$ $B(x_2, y_2) = (2, 8)$, $P(x, y) = ?$

$$P(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$P(x, y) = \left(\frac{2 + 2}{2}, \frac{4 + 8}{2} \right)$$

$$= \left(\frac{4}{2}, \frac{12}{2} \right) = (2, 6)$$

\therefore Coordinates of the mid point $P(x, y) = (2, 6)$



40) $O(x_1, y_1) = (-5, 4)$ $A(x_2, y_2) = (-7, 1)$,

$$\begin{aligned} OA &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\ &= \sqrt{[-7 - (-5)]^2 + (1 - 4)^2} \\ &= \sqrt{(-7 + 5)^2 + (-3)^2} \\ &= \sqrt{(-2)^2 + 9} \end{aligned}$$

$$OA = \sqrt{4 + 9} = \sqrt{13}$$

$$\therefore \mathbf{OA = \sqrt{13} \text{ Units}}$$

IV. Three Marks Questions : -

41) Coordinates of the point A = (0, 6) = (x₁, y₁),

Coordinates of the point B = (3, 0) = (x₂, y₂),

Coordinates of the point P = (2, 2) = (x, y),

$m_1 : m_2 = ?$

$$P(x, y) = \left[\frac{m_1x_2 + m_2x_1}{m_1 + m_2}, \frac{m_1y_2 + m_2y_1}{m_1 + m_2} \right]$$

$$(2, 2) = \left[\frac{m_1(3) + m_2(0)}{m_1 + m_2}, \frac{m_1(0) + m_2(6)}{m_1 + m_2} \right]$$

$$(2, 2) = \left[\frac{3m_1 + 0}{m_1 + m_2}, \frac{0 + 6m_2}{m_1 + m_2} \right]$$

$$(2, 2) = \left[\frac{3m_1}{m_1 + m_2}, \frac{6m_2}{m_1 + m_2} \right]$$

$$2 = \frac{3m_1}{m_1 + m_2} \quad \mathbf{OR} \quad 2 = \frac{6m_2}{m_1 + m_2}$$

$$2(m_1 + m_2) = 3m_1$$

$$2(m_1 + m_2) = 6m_2$$

$$2m_1 + 2m_2 = 3m_1$$

$$2m_1 + 2m_2 = 6m_2$$

$$2m_2 = 3m_1 - 2m_1$$

$$2m_1 = 6m_2 - 2m_2$$

$$2m_2 = m_1$$

$$2m_1 = 4m_2$$

$$\frac{2}{1} = \frac{m_1}{m_2}$$

$$\frac{m_1}{m_2} = \frac{4}{2}$$

$$\therefore \mathbf{m_1 : m_2 = 2 : 1}$$

42) Coordinates of the point A : A (2, 5) = (x₁, y₁),

$m_1 : m_2 = 1 : 2$,

P (x, y) = ?

Coordinates of the point B : B (5, 2) = (x₂, y₂),

$$P(x, y) = \left[\frac{m_1x_2 + m_2x_1}{m_1 + m_2}, \frac{m_1y_2 + m_2y_1}{m_1 + m_2} \right]$$

$$= \left[\frac{1(5) + 2(2)}{1 + 2}, \frac{1(2) + 2(5)}{1 + 2} \right]$$

$$= \left[\frac{5 + 4}{3}, \frac{2 + 10}{3} \right]$$

$$= \left[\frac{9}{3}, \frac{12}{3} \right] = (3, 4)$$

$$P(x, y) = (3, 4)$$

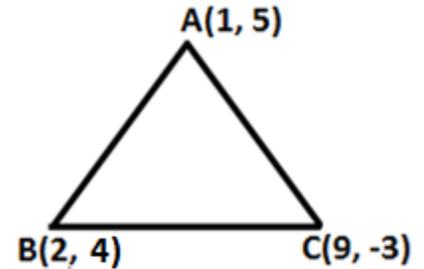
43) Distance between the points $AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$A(1, 5) = (x_1, y_1), \quad B(2, 4) = (x_2, y_2)$$

$$= \sqrt{(2 - 1)^2 + (3 - 4)^2}$$

$$= \sqrt{(1)^2 + (-1)^2}$$

$$\Rightarrow AB = \sqrt{1 + 1} = \sqrt{2} = 1.414$$



Distance between the points $BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$B(2, 4) = (x_1, y_1), \quad C(9, -3) = (x_2, y_2)$$

$$= \sqrt{(9 - 2)^2 + (-3 - 4)^2}$$

$$= \sqrt{(7)^2 + (-7)^2}$$

$$\Rightarrow BC = \sqrt{49 + 49} = \sqrt{98} = 9.899$$

Distance between the points $AC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$A(1, 5) = (x_1, y_1), \quad C(9, -3) = (x_2, y_2)$$

$$= \sqrt{[9 - 1]^2 + (-3 - 5)^2}$$

$$= \sqrt{(8)^2 + (-8)^2}$$

$$\Rightarrow AC = \sqrt{64 + 64} = \sqrt{128} = 11.313$$

$$1.414 + 9.899 = 11.313$$

$$11.313 = 11.313$$

$AB + BC = AC \quad \therefore$ The given points are collinear

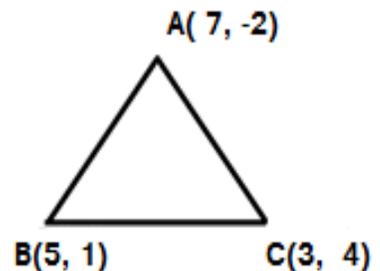
44) Distance between the points $AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$A(7, -2) = (x_1, y_1), \quad B(5, 1) = (x_2, y_2)$$

$$= \sqrt{(5 - 7)^2 + [1 - (-2)]^2}$$

$$= \sqrt{(-2)^2 + (1 + 2)^2}$$

$$\Rightarrow AB = \sqrt{4 + 9} = \sqrt{13} = 3.605$$



Distance between the points $BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$B(5, 1) = (x_1, y_1), \quad C(3, 4) = (x_2, y_2)$$

$$\begin{aligned}
&= \sqrt{(3-5)^2 + (4-1)^2} \\
&= \sqrt{(-2)^2 + (-3)^2} \\
\Rightarrow \mathbf{BC} &= \sqrt{4+9} = \sqrt{13} = \mathbf{3.605}
\end{aligned}$$

Distance between the points $\mathbf{AC} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$A(7, -2) = (x_1, y_1), \quad C(3, 4) = (x_2, y_2)$$

$$\begin{aligned}
&= \sqrt{[3-7]^2 + [4-(-2)]^2} \\
&= \sqrt{(-4)^2 + (4+2)^2}
\end{aligned}$$

$$\Rightarrow \mathbf{AC} = \sqrt{16+36} = \sqrt{52} = \mathbf{7.211}$$

$$\mathbf{3.605 + 3.605 \neq 7.21}$$

$$\mathbf{7.21 = 7.21}$$

$\mathbf{AB + BC = AC} \quad \therefore$ **The given points are collinear**

45) Distance between the points $\mathbf{AB} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$A(5, -2) = (x_1, y_1), \quad B(6, 4) = (x_2, y_2)$$

$$\begin{aligned}
&= \sqrt{(6-5)^2 + [4-(-2)]^2} \\
&= \sqrt{(1)^2 + (4+2)^2}
\end{aligned}$$

$$\Rightarrow \mathbf{AB} = \sqrt{1+(6)^2} = \sqrt{1+36} = \mathbf{\sqrt{37}}$$

Distance between the points $\mathbf{BC} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$B(6, 4) = (x_1, y_1) \quad C(7, -2) = (x_2, y_2)$$

$$\begin{aligned}
&= \sqrt{(7-6)^2 + (-2-4)^2} \\
&= \sqrt{(1)^2 + (-6)^2}
\end{aligned}$$

$$\Rightarrow \mathbf{BC} = \sqrt{1+36} = \mathbf{\sqrt{37}}$$

Distance between the points $\mathbf{CA} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

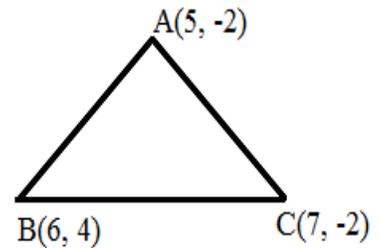
$$C(7, -2) = (x_1, y_1), \quad A(5, -2) = (x_2, y_2)$$

$$\begin{aligned}
&= \sqrt{(7-5)^2 + [-2-(-2)]^2} \\
&= \sqrt{(2)^2 + (-2+4)^2}
\end{aligned}$$

$$\Rightarrow \mathbf{AC} = \sqrt{4+(2)^2} = \sqrt{4+4} = \mathbf{\sqrt{8}}$$

$$\mathbf{AB = BC = \sqrt{37}}$$

\therefore The given points are vertices of an isosceles triangle



46) Distance between the points $\mathbf{AB} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$A(8, -4) = (x_1, y_1), \quad B(9, 5) = (x_2, y_2)$$

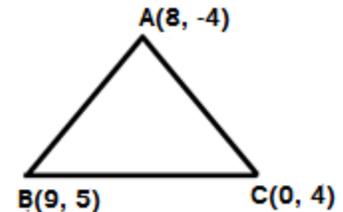
$$\begin{aligned}
&= \sqrt{(9-8)^2 + [5-(-4)]^2} \\
&= \sqrt{(1)^2 + (5+4)^2}
\end{aligned}$$

$$\Rightarrow \mathbf{AB} = \sqrt{1+(9)^2} = \sqrt{1+81} = \mathbf{\sqrt{82}}$$

Distance between the points $\mathbf{BC} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$B(9, 5) = (x_1, y_1), \quad C(0, 4) = (x_2, y_2)$$

$$= \sqrt{(0-9)^2 + (4-5)^2}$$



$$= \sqrt{(-9)^2 + (-1)^2}$$

$$\Rightarrow \mathbf{BC} = \sqrt{81 + 1} = \sqrt{82}$$

Distance between the points $\mathbf{AC} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$C(0, 4) = (x_1, y_1), \quad A(8, -4) = (x_2, y_2)$$

$$= \sqrt{(8 - 0)^2 + [-4 - (4)]^2}$$

$$= \sqrt{(8)^2 + (0)^2}$$

$$\Rightarrow \mathbf{AC} = \sqrt{64}$$

$$\mathbf{AB} = \mathbf{BC} = \sqrt{82}$$

\therefore The given points are vertices of an isosceles triangle

$$47) \quad A(x_1, y_1) = (x_1, y_1), \quad B(x_2, y_2) = (4, 3) = (x, y)$$

$$x = \frac{x_1 + x_2}{2}, \quad y = \frac{y_1 + y_2}{2}$$

$$4 = \frac{x + 0}{2}, \quad 3 = \frac{0 + y}{2}$$

$$8 = x, \quad 6 = y$$

$$A(8, 0) = (x_1, y_1), \quad B(0, 6) = (x_2, y_2),$$

$$\mathbf{AB} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(0 - 8)^2 + (6 - 0)^2}$$

$$\mathbf{AB} = \sqrt{(8)^2 + (6)^2} = \sqrt{64 + 36} = \sqrt{100} = 10 \text{ Units}$$

48)



Let P and Q are the trisection points of AB $\therefore \mathbf{AP} = \mathbf{PQ} = \mathbf{QB}$

The point P divides AB internally in the ratio 1 : 2

$$A(4, -1) = (x_1, y_1), \quad B(-2, -3) = (x_2, y_2) \quad m_1 : m_2 \Rightarrow 1 : 2 \quad P(x, y) = ?$$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{1(-2) + 2(4)}{1 + 2}, \frac{1(-3) + 2(-1)}{1 + 2} \right]$$

$$= \left[\frac{-2 + 8}{3}, \frac{-3 - 2}{3} \right]$$

$$= \left[\frac{6}{3}, \frac{-5}{3} \right] = \left[2, \frac{-5}{3} \right]$$

$$\mathbf{P(x, y) = \left[2, \frac{-5}{3} \right]}$$

The point Q divides AB internally in the ratio 2 : 1 $\therefore m_1 : m_2 \Rightarrow 2 : 1$

$P(x, y) = ?$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{2(-2) + 1(4)}{2 + 1}, \frac{2(-3) + 1(-1)}{2 + 1} \right]$$

$$= \left[\frac{-4+4}{3}, \frac{-6-1}{3} \right]$$

$$= \left[\frac{0}{3}, \frac{-7}{3} \right] = \left[0, \frac{-7}{3} \right]$$

$$\mathbf{P(x, y) = \left[0, \frac{-7}{3} \right]}$$

∴ Trisection points of A and B are : $\left[2, \frac{-5}{3} \right]$ and $\left[0, \frac{-7}{3} \right]$

49)



Let P and Q are the trisection points of AB ∴ AP = PQ = QB

The point P divides AB internally in the ratio 1 : 2

$$A(2, -2) = (x_1, y_1), \quad B(-7, 4) = (x_2, y_2) \quad m_1 : m_2 \Rightarrow 1 : 2 \quad P(x, y) = ?$$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{1(-7) + 2(2)}{1+2}, \frac{1(4) + 2(-2)}{1+2} \right]$$

$$= \left[\frac{-7+4}{3}, \frac{4-4}{3} \right]$$

$$\mathbf{P(x, y) = \left[\frac{-3}{3}, \frac{0}{3} \right] = [-1, 0]}$$

The point Q divides AB internally in the ratio 2 : 1

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, y) = \left[\frac{2(-7) + 1(2)}{2+1}, \frac{2(4) + 1(-2)}{2+1} \right]$$

$$= \left[\frac{-14+2}{3}, \frac{8-2}{3} \right]$$

$$\mathbf{P(x, y) = \left[\frac{-12}{3}, \frac{6}{3} \right] = (-4, 2)}$$

∴ Trisection points of A and B are : $(-1, 0)$ & $(-4, 2)$

50)

The point on the x-axis is of the form (X, 0) ∴ P(x, y) = (x, 0)

Let ratio be k : 1 ∴ $m_1 : m_2 = k : 1$

$$A(1, -5) = (x_1, y_1) \quad B(-4, 5) = (x_2, y_2)$$

$$P(x, y) = \left[\frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}, \frac{m_1 y_2 + m_2 y_1}{m_1 + m_2} \right]$$

$$P(x, 0) = \left[\frac{k(-4) + 1(1)}{k+1}, \frac{k(5) + 1(-5)}{k+1} \right]$$

$$(x, 0) = \left[\frac{-4k+1}{k+1}, \frac{5k-5}{k+1} \right]$$

$$x = \frac{-4k+1}{k+1} \quad \text{---(1)}$$

$$0 = \frac{5k-5}{k+1}$$

$$0(k+1) = 5k-5$$

$$0 = 5k-5$$

$$5k = 5 \quad k = \frac{5}{5} = 1 \quad \therefore k = 1$$

Put $k = 1$ in eqn. (1)

$$x = \frac{-4(1)+1}{1+1}$$

$$x = \frac{-4+1}{1+1} = \frac{-3}{2}$$

$$x = \frac{-3}{2}$$

The coordinates of the point of division = $(x, 0) = \left(\frac{-3}{2}, 0 \right)$

- 51). The point P(x,y) is equidistant from (3, 6) and (-3, 4), $PA = PB$

$$PA = PB$$

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x-(-3))^2 + (y-4)^2}$$

$$\sqrt{(x-3)^2 + (y-6)^2} = \sqrt{(x+3)^2 + (y-4)^2}$$

By squaring on both sides

$$(x-3)^2 + (y-6)^2 = (x+3)^2 + (y-4)^2$$

$$x^2 + 9 - 6x + y^2 + 36 - 12y = x^2 + 9 + 6x + y^2 + 16 - 8y$$

$$-6x - 6x + 8y - 12y + 36 - 16 = 0$$

$$-12x - 4y + 20 = 0 \quad (\div 4)$$

$$-3x - y + 5 = 0$$

$$5 = 3x + y \quad \text{OR} \quad 3x + y = 5$$

- 52) The point P(x,y) is equidistant from (7, 1) and (3, 5), $PA = PB$

$$AP = BP$$

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(x-7)^2 + (y-1)^2} = \sqrt{(x-3)^2 + (y-5)^2}$$

By squaring on both sides

$$(x-7)^2 + (y-1)^2 = (x-3)^2 + (y-5)^2$$

$$x^2 + 49 - 14x + y^2 + 1 - 2y = x^2 + 9 - 6x + y^2 + 25 - 10y$$

$$-14x + 6x - 2y + 10y = -50 + 34$$

$$-8x + 8y = -16$$

$$8(y-x) = -16$$

$$y-x = \frac{-16}{8} = -2 \Rightarrow y-x = -2$$

$$\Rightarrow x-y = 2$$

$$P(x, y) = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

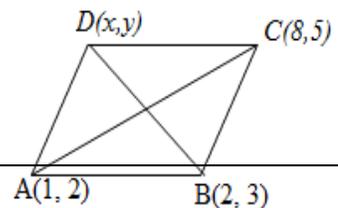
$$= \left(\frac{7+3}{2}, \frac{1+5}{2} \right) = \left(\frac{10}{2}, \frac{6}{2} \right) = (5, 3) \quad \therefore P(x, y) = (5, 3)$$

- 53) Let the coordinates of D are D(x,y)

In the parallelogram ABCD diagonals AC and BD bisect each other.

Mid point of AC = Mid point of BD

$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right) = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$



$$\begin{aligned}
A(1, 2) &= (x_1, y_1) & B(2, 3) &= (x_1, y_1) \\
C(8, 5) &= (x_2, y_2) & D(x, y) &= (x_2, y_2) \\
\left(\frac{1+8}{2}, \frac{2+5}{2}\right) &= \left(\frac{2+x}{2}, \frac{3+y}{2}\right) \\
\left(\frac{9}{2}, \frac{7}{2}\right) &= \left(\frac{2+x}{2}, \frac{3+y}{2}\right) \\
\frac{9}{2} &= \frac{2+x}{2}, & \frac{7}{2} &= \frac{3+y}{2} \\
2 \times \frac{9}{2} &= 2+x, & 2 \times \frac{7}{2} &= 3+y \\
9 &= 2+x, & 7 &= 3+y \\
x &= 9-2=7, & y &= 7-3=4 \\
\therefore x &= 7 & \therefore y &= 4
\end{aligned}$$

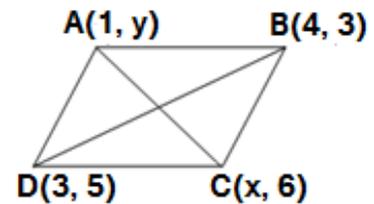
\therefore the coordinates of D are $D(x, y) = D(7,4)$

54)

In the parallelogram ABCD diagonals AC and BD bisect each other.

Mid point of AC = Mid point of BD

$$\begin{aligned}
\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) &= \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) \\
A(1, y) &= (x_1, y_1) & B(4, 3) &= (x_1, y_1) \\
C(x, 6) &= (x_2, y_2) & D(3, 5) &= (x_2, y_2) \\
\left(\frac{1+x}{2}, \frac{y+6}{2}\right) &= \left(\frac{4+3}{2}, \frac{3+5}{2}\right) \\
\left(\frac{1+x}{2}, \frac{y+6}{2}\right) &= \left(\frac{7}{2}, \frac{8}{2}\right) \\
\frac{1+x}{2} &= \frac{7}{2} & \frac{y+6}{2} &= \frac{8}{2} \\
1+x &= 7 & y+6 &= 8 \\
x &= 7-1 & y &= 8-6 \\
\therefore x &= 6 & \text{and } y &= 2
\end{aligned}$$

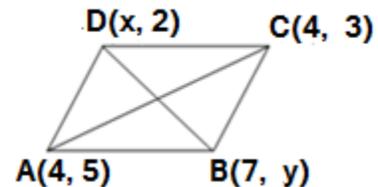


55)

In the parallelogram ABCD diagonals AC and BD bisect each other.

Mid point of AC = Mid point of BD

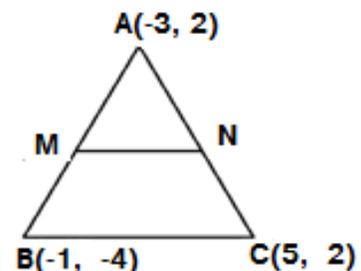
$$\begin{aligned}
\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) &= \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) \\
A(4, 5) &= (x_1, y_1) & B(7, y) &= (x_1, y_1) \\
C(4, 3) &= (x_2, y_2) & D(x, 2) &= (x_2, y_2) \\
\left(\frac{4+4}{2}, \frac{5+3}{2}\right) &= \left(\frac{7+x}{2}, \frac{y+2}{2}\right) \\
\left(\frac{8}{2}, \frac{8}{2}\right) &= \left(\frac{7+x}{2}, \frac{y+2}{2}\right) \\
(4, 4) &= \left(\frac{7+x}{2}, \frac{y+2}{2}\right) \\
4 &= \frac{7+x}{2} & 4 &= \frac{y+2}{2} \\
8 &= 7+x & y+2 &= 8 \\
x &= 8-7=1 & y &= 8-2=6 \\
\therefore x &= 6 & \& \ y &= 6
\end{aligned}$$



56) coordinates of the point M

By using mid point formula $P(x, y) = \left[\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right]$

$$\begin{aligned}
M(x_1, y_1) &= \left[\frac{-3+(-1)}{2}, \frac{2+(-4)}{2}\right] \\
&= \left[\frac{-3-1}{2}, \frac{2-4}{2}\right] \\
&= \left[\frac{-4}{2}, \frac{-2}{2}\right] \\
M(x_1, y_1) &= (-2, -1)
\end{aligned}$$



coordinates of the point N

$$N(x_2, y_2) = \left[\frac{-3 + 5}{2}, \frac{2 + 2}{2} \right]$$

$$= \left[\frac{2}{2}, \frac{4}{2} \right]$$

$$N(x_2, y_2) = (1, 2)$$

$$MN = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$M(x_1, y_1) = (-2, -1) \quad N(x_2, y_2) = (1, 2)$$

$$= \sqrt{[1 - (-2)]^2 + [2 - (-1)]^2}$$

$$= \sqrt{(1 + 2)^2 + (2 + 1)^2} = \sqrt{3^2 + 3^2}$$

$$= \sqrt{9 + 9} = \sqrt{18} = \sqrt{9 \times 2} = 3\sqrt{2}$$

$$MN = 3\sqrt{2} \text{ Units} \text{ ----- (1)}$$

$$BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$B(x_1, y_1) = (-1, -4), \quad C(x_2, y_2) = (5, 2)$$

$$BC = \sqrt{[5 - (-1)]^2 + [2 - (-4)]^2}$$

$$= \sqrt{(5 + 1)^2 + (2 + 4)^2} = \sqrt{6^2 + 6^2}$$

$$= \sqrt{36 + 36} = \sqrt{72} = \sqrt{36 \times 2} = 6\sqrt{2}$$

$$BC = 6\sqrt{2} \text{ Units} \text{ ----- (2)}$$

$$\text{From eqn (1) and (2)} \Rightarrow \mathbf{BC = 2 MN}$$

57) coordinates of the point E :

$$\text{By using mid point formula } P(x, y) = \left[\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right]$$

$$E(x_1, y_1) = \left[\frac{7 + 9}{2}, \frac{2 + 10}{2} \right]$$

$$= \left[\frac{16}{2}, \frac{12}{2} \right] = (8, 6)$$

$$E(x_1, y_1) = (8, 6)$$

coordinates of the point F :

$$F(x_2, y_2) = \left[\frac{7 + 1}{2}, \frac{4 + 2}{2} \right]$$

$$= \left[\frac{8}{2}, \frac{6}{2} \right] = (4, 3)$$

$$F(x_2, y_2) = (4, 3)$$

$$EF = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$E(x_1, y_1) = (8, 6), \quad F(x_2, y_2) = (4, 3)$$

$$= \sqrt{(4 - 8)^2 + (3 - 6)^2}$$

$$= \sqrt{(-4)^2 + (-3)^2} =$$

$$= \sqrt{16 + 9} = \sqrt{25}$$

$$EF = 5 \text{ Units} \text{ ----- (1)}$$

$$BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$B(x_1, y_1) = (9, 10), \quad C(x_2, y_2) = (1, 4)$$

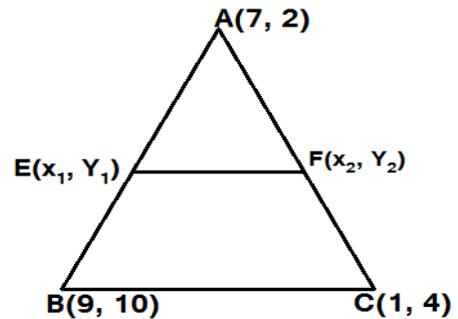
$$BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(1 - 9)^2 + (4 - 10)^2}$$

$$= \sqrt{(-8)^2 + (-6)^2}$$

$$= \sqrt{64 + 36} = \sqrt{100} = 10$$

$$BC = 10 \text{ Units} \text{ ----- (1)}$$



$$\text{From Eqn (1) and (2)} \Rightarrow \mathbf{EF} = \frac{1}{2}\mathbf{BC}$$

58) $A(1, 7), B(4, 2), C(-1, -1), D(-4, 4),$

$$\text{Distance between AB} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$A(1, 7) = (x_1, y_1) \quad B(4, 2) = (x_2, y_2)$$

$$= \sqrt{(4 - 1)^2 + (2 - 7)^2}$$

$$= \sqrt{(3)^2 + (-5)^2}$$

$$= \sqrt{9 + 25}$$

$$\text{Distance between AB} = \sqrt{34} \text{ ----- (1)}$$

$$\text{Distance between BC} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$B(4, 2) = (x_1, y_1) \quad C(-1, -1) = (x_2, y_2)$$

$$= \sqrt{(-1 - 4)^2 + (-1 - 2)^2}$$

$$= \sqrt{(-5)^2 + (-3)^2} = \sqrt{25 + 9}$$

$$\mathbf{BC} = \sqrt{34} \text{ ----- (2)}$$

$$\text{Distance between CD} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$C(-1, -1) = (x_1, y_1) \quad D(-4, 4) = (x_2, y_2)$$

$$= \sqrt{[(-4 - (-1))]^2 + [(4 - (-1))]^2}$$

$$= \sqrt{(-4 + 1)^2 + (4 + 1)^2} =$$

$$= \sqrt{(-3)^2 + (5)^2} = \sqrt{9 + 25}$$

$$\mathbf{CD} = \sqrt{34} \text{ ----- (3)}$$

$$\text{Distance between DA} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$D(-4, 4) = (x_1, y_1) \quad A(1, 7) = (x_2, y_2)$$

$$= \sqrt{[(1 - (-4))]^2 + (7 - 4)^2}$$

$$= \sqrt{(1 + 4)^2 + (3)^2} =$$

$$= \sqrt{(5)^2 + (3)^2} = \sqrt{25 + 9}$$

$$\mathbf{DA} = \sqrt{34} \text{ ----- (4)}$$

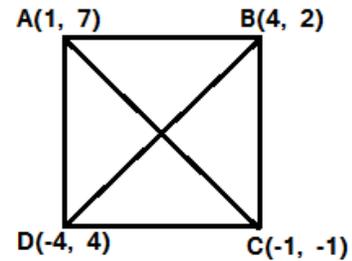
$$\text{Distance between the Diagonal AC} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$A(1, 7) = (x_1, y_1) \quad C(-1, -1) = (x_2, y_2)$$

$$= \sqrt{(-1 - 1)^2 + (-1 - 7)^2}$$

$$= \sqrt{(-2)^2 + (-8)^2} = \sqrt{4 + 64}$$

$$\mathbf{AC} = \sqrt{68} \text{ ----- (5)}$$



$$\text{Distance between the Diagonal BD} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$B(4, 2) = (x_1, y_1) \quad D(-4, 4) = (x_2, y_2)$$

$$= \sqrt{(-4 - 4)^2 + (4 - 2)^2}$$

$$= \sqrt{(-8)^2 + (-2)^2}$$

$$= \sqrt{64 + 4}$$

$$BD = \sqrt{68} \text{ ----- (6)}$$

AB = BC = CD = DA and Diagonals AC = BD

∴ ABCD is a square

Unit : 08 Introduction to Trigonometry

I. Multiple choice Questions :

1. B) $\frac{PR}{QR}$
2. B) $\cot L$
3. C) $\frac{1}{2}$
4. A) $\frac{13}{5}$
5. B) $\frac{1}{4}$
6. D) 1
7. D) 45^0
8. B) $\frac{3}{5}$
9. D) $\frac{13}{12}$
10. D) 1
11. D) $\frac{1}{2}$
12. C) 1
13. C) 30^0
14. D) $\frac{\sqrt{y^2-x^2}}{y}$
15. D) 1
16. A) $\frac{9}{25}$
17. D) $\sin^2\theta + \cos^2\theta = 1$
18. A) 0
19. A) $4 + \tan^2 A$
20. B) 1
21. C) $\sec^2 \theta$
22. A) -1
23. B) 1
24. D) $\frac{1}{k}$
25. D) $\frac{7}{17}$
26. B) $\frac{7}{8}$

II. One Mark Questions :

$$27. AB:AC = \sin\theta = 30^\circ = \frac{1}{2} \therefore AB:AC = 1 : 2$$

$$28. \sin^2\theta + \cos^2\theta = \frac{3^2}{5^2} + \frac{4^2}{5^2} = \frac{9}{25} + \frac{16}{25} = \frac{9+16}{25} = \frac{25}{25} = 1$$

$$\therefore \sin^2\theta + \cos^2\theta = 1$$

$$29. \operatorname{cosec}60^\circ + \sec30^\circ = \frac{2}{\sqrt{3}} + \frac{2}{\sqrt{3}} = \frac{4}{\sqrt{3}}$$

$$30. \sin90^\circ + \tan45^\circ = 1 + 1 = 2$$

$$31. \frac{AB}{BC} = \tan30^\circ = \frac{1}{\sqrt{3}}$$

$$\frac{AB}{BC} = \frac{15}{BC} = \frac{1}{\sqrt{3}}$$

$$\therefore BC = 15\sqrt{3} \text{ mts}$$

$$32. \tan45^\circ + \cot45^\circ = 1 + 1 = 2$$

$$\therefore \tan45^\circ + \cot45^\circ = 2$$

$$33. \sec\theta = \frac{1}{\cos\theta} = \frac{1}{\frac{24}{25}} = \frac{25}{24}$$

$$\therefore \sec\theta = \frac{25}{24}$$

$$34. \sin^2A + \cos^2A = 1$$

$$0 + \cos^2A = 1$$

$$\therefore \cos^2A = 1$$

$$35. 15\cot A = 8$$

$$\therefore \cot A = \frac{8}{15} = \frac{1}{\tan A}$$

$$\therefore \tan A = \frac{15}{8}$$

$$36. \frac{AC}{AB} = \operatorname{cosec}\theta = 30^\circ$$

$$\frac{AC}{12} = 2$$

$$\therefore AC = 24 \text{ cm}$$

$$37. x \cdot \tan 45^\circ \cdot \sin 30^\circ = \cos 30^\circ \tan 30^\circ$$

$$x(1)\left(\frac{1}{2}\right) = \frac{\sqrt{3}}{2} \cdot \sqrt{3}$$

$$\therefore x = 3$$

$$38. 5 \tan^2 A - 5 \sec^2 A + 1 = 5 \tan^2 A - 5(1 + \tan^2 A) + 1 \\ = 5 \tan^2 A - 5 - 5 \tan^2 A + 1 = 1 - 5 = -4$$

$$\therefore 5 \tan^2 A - 5 \sec^2 A + 1 = -4$$

$$39. \sin A \cdot \operatorname{cosec} A = 1$$

$$40. \tan A \cdot \cot A - \cos A \cdot \sec A = 0$$

$$41. \tan^2 45^\circ - \sin^2 45^\circ = (1)^2 - \left(\frac{1}{\sqrt{2}}\right)^2 = 1 - \frac{1}{2} = \frac{1}{2}$$

$$\therefore \tan^2 45^\circ - \sin^2 45^\circ = \frac{1}{2}$$

$$42. \sin A = \cos A$$

$$\frac{\sin A}{\cos A} = 1$$

$$\tan A = 1$$

$$\tan A = 45^\circ$$

$$\therefore A = 45^\circ$$

III. **Two Marks Questions :**

$$43. \sec \theta = \frac{1}{\cos \theta} = \frac{1}{\frac{5}{13}} = \frac{13}{5}$$

$$\therefore \sec \theta = \frac{13}{5}$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\frac{12}{13}}{\frac{5}{13}} = \frac{12}{5}$$

$$\therefore \tan \theta = \frac{12}{5}$$

$$44. \operatorname{cosec} \theta = \frac{13}{12} = \frac{1}{\sin \theta} \quad \therefore \sin \theta = \frac{12}{13}$$

$$\tan \theta = \frac{5}{12} = \frac{\cos \theta}{\sin \theta}$$

$$\therefore \frac{\cos \theta}{\frac{12}{13}} = \frac{5}{12}$$

$$\therefore \cos \theta = \frac{5}{12} \times \frac{12}{13}$$

$$\therefore \cos \theta = \frac{5}{13}$$

$$45. \sin \alpha = \frac{24}{25} \quad \cos \alpha = \frac{7}{25}$$

$$46. \sin P = \frac{1}{2} \quad \text{သို့} \quad \tan R = \frac{\sqrt{3}}{1} = \sqrt{3}$$

$$47. \tan P - \cot R = \frac{5}{12} - \frac{5}{12} = 0$$

$$48. \sin \alpha = \frac{3}{5} \quad \text{and} \quad \tan \theta = \frac{4}{3}$$

$$49. \sin \alpha = \frac{4}{5} \quad \text{and} \quad \cos \theta = \frac{3}{5}$$

$$50. 2\tan^2 45^\circ + \cos^2 30^\circ - \sin^2 60^\circ$$

$$= 2(1)^2 + \left(\frac{\sqrt{3}}{2}\right)^2 - \left(\frac{\sqrt{3}}{2}\right)^2$$

$$= 2$$

$$51. \sqrt{3} \tan \theta = 1 \quad \therefore \tan \theta = \frac{1}{\sqrt{3}}$$

$$\therefore \tan \theta = \tan 30^\circ$$

$$\therefore \theta = 30^\circ$$

$$\sin 3\theta + \cos 3\theta = \sin(3 \times 30^\circ) + \cos(2 \times 30^\circ) = \sin 90^\circ + \cos 60^\circ$$

$$\sin 3\theta + \cos 3\theta = 1 + \frac{1}{2}$$

$$\therefore \sin 3\theta + \cos 3\theta = \frac{3}{2}$$

$$\begin{aligned} 52. \text{ LHS} &= (\tan A \sin A) + \cos A \\ &= \frac{\sin A}{\cos A} \times \sin A + \cos A \\ &= \frac{\sin^2 A}{\cos A} + \cos A \\ &= \frac{\cos A}{\sin^2 A + \cos^2 A} \\ &= \frac{1}{\cos A} \\ &= \sec A = \text{RHS} \end{aligned}$$

$$\begin{aligned} 53. \text{ LHS} &= 5 \sin \theta - 3 \tan \theta \\ &= 5 \sin \theta - 3 \frac{\sin A}{\cos A} \\ &= \frac{5 \sin \theta \times \cos \theta - 3 \sin A}{\cos A} \\ &= \frac{5 \sin \theta \times 0.6 - 3 \sin A}{0.6} \\ &= \frac{5 \sin \theta - 5 \sin \theta}{0.6} \\ &= 0 = \text{RHS} \end{aligned}$$

$$\begin{aligned} 54. \text{ LHS} &= \sec^4 \theta - \sec^2 \theta \\ &= \sec^2 \theta (\sec^2 \theta - 1) \\ &= (1 + \tan^2 \theta) \times \tan^2 \theta \\ &= \tan^4 \theta + \tan^2 \theta = \text{RHS} \end{aligned}$$

$$\begin{aligned} 55. \text{ LHS} &= \operatorname{cosec} A (1 - \cos A) (\operatorname{cosec} A + \cot A) \\ &= \frac{1}{\sin A} (1 - \cos A) \left(\frac{1}{\sin A} + \frac{\cos A}{\sin A} \right) \\ &= \frac{1}{\sin A} (1 - \cos A) \left(\frac{1 + \cos A}{\sin A} \right) \\ &= \frac{1 - \cos^2 A}{\sin^2 A} \\ &= \frac{\sin^2 A}{\sin^2 A} \\ &= 1 = \text{RHS} \end{aligned}$$

$$\begin{aligned} 56. \text{ LHS} &= \tan^2 \theta - \sin^2 \theta \\ &= \frac{\sin^2 \theta}{\cos^2 \theta} - \sin^2 \theta \\ &= \frac{\sin^2 \theta - \sin^2 \theta \times \cos^2 \theta}{\cos^2 \theta} \\ &= \sin^2 \theta \left(\frac{1 - \cos^2 \theta}{\cos^2 \theta} \right) \\ &= \sin^2 \theta \left(\frac{\sin^2 \theta}{\cos^2 \theta} \right) \\ &= \sin^2 \theta \cdot \tan^2 \theta = \text{RHS} \end{aligned}$$

$$57. \text{ LHS} = \cot^2 \theta - \cos^2 \theta$$

$$\begin{aligned}
&= \frac{\cos^2\theta}{\sin^2\theta} - \cos^2\theta \\
&= \frac{\cos^2\theta - \sin^2\theta \cos^2\theta}{\sin^2\theta} \\
&= \cos^2\theta \left(\frac{1 - \sin^2\theta}{\sin^2\theta} \right) \\
&= \cos^2\theta \left(\frac{\cos^2\theta}{\sin^2\theta} \right) \\
&= \cos^2\theta \cdot \cot^2\theta = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
58. \text{ LHS} &= \sin 30^\circ + \cos 60^\circ + \tan 45^\circ \\
&= \frac{1}{2} + \frac{1}{2} + 1 \\
&= 1 + 1 \\
&= 2
\end{aligned}$$

$$\begin{aligned}
&= \sec 60^\circ = \text{RHS} \\
59. \text{ LHS} &= \frac{\sin 30^\circ + \cos 60^\circ}{\operatorname{cosec} 30^\circ - \cos 45^\circ} \\
&= \frac{\frac{1}{2} + \frac{1}{2}}{2 - 1} \\
&= \frac{1}{1} \\
&= 1 \\
&= \sin 90^\circ = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
60. \frac{\cos 45^\circ \cdot \sin 45^\circ}{\sec 30^\circ - \cot 60^\circ} &= \frac{\frac{1}{\sqrt{2}} \cdot \frac{1}{\sqrt{2}}}{\frac{2}{\sqrt{3}} - \frac{1}{\sqrt{3}}} \\
&= \frac{\frac{1}{2}}{\frac{2-1}{\sqrt{3}}} \\
&= \frac{\frac{1}{2}}{\frac{1}{\sqrt{3}}} \\
&= \frac{1}{2} \times \frac{\sqrt{3}}{1} \\
&= \frac{\sqrt{3}}{2}
\end{aligned}$$

$$\begin{aligned}
61. \text{ LHS} &= \frac{1 + \cos A}{1 - \cos A} \times \frac{1 + \cos A}{1 + \cos A} \\
&= \frac{(1 + \cos A)^2}{1 - \cos^2 A} \\
&= \frac{(1 + \cos A)^2}{\sin^2 A} \\
&= \left(\frac{1 + \cos A}{\sin A} \right)^2 \\
&= \left(\frac{1}{\sin A} + \frac{\cos A}{\sin A} \right)^2 \\
&= (\operatorname{cosec} A + \cot A)^2 = \text{RHS}
\end{aligned}$$

$$62. \text{ LHS} = \frac{1 + \sin A}{1 - \sin A} \times \frac{1 + \sin A}{1 + \sin A}$$

$$\begin{aligned}
&= \frac{(1+\sin A)^2}{1-\sin^2 A} \\
&= \frac{(1+\sin A)^2}{\cos^2 A} \\
&= \left(\frac{1+\sin A}{\cos A}\right)^2 \\
&= \left(\frac{1}{\cos A} + \frac{\sin A}{\cos A}\right)^2 \\
&= (\sec A + \tan A)^2 = \text{RHS} \\
63. \text{ LHS} &= \frac{\cos A}{1+\sin A} + \frac{1+\sin A}{\cos A} \\
&= \frac{\cos^2 A + (1+\sin A)^2}{(1+\sin A)\cos A} \\
&= \frac{\cos^2 A + 1 + \sin^2 A + 2\sin A}{(1+\sin A)\cos A} \\
&= \frac{1+1+2\sin A}{(1+\sin A)\cos A} \\
&= \frac{2+2\sin A}{(1+\sin A)\cos A} \\
&= \frac{2(1+\sin A)}{(1+\sin A)\cos A} \\
&= \frac{2}{\cos A} \\
&= 2\sec A = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
64. \text{ LHS} &= \frac{\sin A}{1+\cos A} + \frac{1+\cos A}{\sin A} \\
&= \frac{\sin^2 A + (1+\cos A)^2}{(1+\cos A)\sin A} \\
&= \frac{\sin^2 A + 1 + \cos^2 A + 2\cos A}{(1+\cos A)\sin A} \\
&= \frac{1+1+2\sin A}{(1+\cos A)\sin A} \\
&= \frac{2+2\cos A}{(1+\cos A)\sin A} \\
&= \frac{2(1+\cos A)}{(1+\cos A)\sin A} \\
&= \frac{2}{\sin A} \\
&= 2\operatorname{cosec} A \\
&= \text{RHS}
\end{aligned}$$

$$\begin{aligned}
65. \text{ LHS} &= \frac{\cos A - \sin A \cdot \cos A}{\cos A + \sin A \cdot \cos A} \\
&= \frac{\cos A(1-\sin A)}{\cos A(1+\sin A)} \\
&= \frac{1-\sin A}{1+\sin A}
\end{aligned}$$

$$\begin{aligned}
&= \frac{\left(1 - \frac{1}{\operatorname{Cosec}A}\right)}{\left(1 + \frac{1}{\operatorname{Cosec}A}\right)} \\
&= \frac{\left(\frac{1 - \operatorname{Cosec}A}{\operatorname{Cosec}A}\right)}{\left(\frac{1 + \operatorname{Cosec}A}{\operatorname{Cosec}A}\right)} \\
&= \frac{1 - \operatorname{Cosec}A}{1 + \operatorname{Cosec}A} \\
&= \text{RHS}
\end{aligned}$$

$$66. \sin 30^\circ \cdot \cos 60^\circ + \cos 30^\circ \cdot \sin 60^\circ$$

$$\begin{aligned}
&= \frac{1}{2} \cdot \frac{1}{2} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} \\
&= \frac{1}{4} + \frac{3}{4} \\
&= \frac{1+3}{4} \\
&= \frac{4}{4} \\
&= 1 \\
&= \sin 90^\circ
\end{aligned}$$

$$67. \frac{\frac{\sqrt{3}}{1} \cdot \frac{1}{\operatorname{Cosec}A}}{\frac{1}{\operatorname{Sin}A}} = 1$$

$$\sqrt{3} \times \frac{1}{\operatorname{cos}A} \times \frac{\operatorname{sin}A}{1} = 1$$

$$\sqrt{3} \tan A = 1$$

$$\tan A = \frac{1}{\sqrt{3}}$$

$$\tan A = \tan 30^\circ$$

$$\therefore A = 30^\circ$$

$$68. \text{LHS} = \sec A (1 - \sin A) (\sec A + \tan A)$$

$$= \frac{1}{\operatorname{Cos}A} (1 - \operatorname{tin}A) \left(\frac{1}{\operatorname{Cos}A} + \frac{\operatorname{Sin}A}{\operatorname{Cos}A} \right)$$

$$= \frac{1}{\operatorname{Cos}A} (1 - \operatorname{sin}A) \left(\frac{1 + \operatorname{Sin}A}{\operatorname{Cos}A} \right)$$

$$= \frac{(1 - \operatorname{Sin}A)(1 + \operatorname{Sin}A)}{\operatorname{Cos}^2 A}$$

$$= \frac{1 - \operatorname{Sin}^2 A}{\operatorname{Cos}^2 A}$$

$$= \frac{\operatorname{Cos}^2 A}{\operatorname{Cos}^2 A}$$

$$= 1 = \text{RHS}$$

$$69. 2\sin\theta = 1 \quad \therefore \sin\theta = \frac{1}{2}$$

$$\text{Now } \cos^2 60^\circ + \sec^2 30^\circ$$

$$= \left(\frac{1}{2}\right)^2 + \left(\frac{2}{\sqrt{3}}\right)^2$$

$$= \frac{1}{4} + \frac{4}{3}$$

$$= \frac{3+16}{12}$$

$$= \frac{19}{12}$$

$$70. \text{LHS} = \tan^2\theta + \cot^2\theta$$

$$= \sec^2\theta - 1 + \text{cosec}^2\theta - 1$$

$$= \sec^2\theta + \text{cosec}^2\theta - 2 = \text{RHS}$$

$$71. 4\sin 30^\circ + \cos 60^\circ \cdot \sec 60^\circ - 3\tan 45^\circ = 4\left(\frac{1}{2}\right) + \frac{1}{2}(2) - 3(1)$$

$$= 2 + 1 - 3$$

$$= 3 - 3$$

$$= 0$$

$$72. 6\cos 60^\circ - \sin 30^\circ + \sin^2 45^\circ + \cos^2 45^\circ$$

$$= 6\left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) + \left(\frac{1}{\sqrt{2}}\right)^2$$

$$= 3$$

$$73. \frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{\sin 30^\circ + \sin 90^\circ}$$

$$= \frac{5\left(\frac{1}{2}\right)^2 + 4\left(\frac{2}{\sqrt{3}}\right)^2 - 1}{1}$$

$$= \frac{5}{4} + \frac{16}{3} - 1$$

$$= \frac{15+64-12}{12}$$

$$= \frac{67}{12}$$

$$74. \frac{\sec 60^\circ}{\cot 45^\circ} - \frac{2\sin 90^\circ}{\cos 0^\circ} + \frac{\tan 45^\circ}{\text{cosec} 30^\circ}$$

$$= \frac{1}{1} - \frac{2 \times 1}{1} + \frac{1}{2}$$

$$= 2 - 2 + \frac{1}{2}$$

$$= 2$$

$$75. 2\cot^2\theta + 2 = 2(\cot^2\theta + 1)$$

$$= 2(\operatorname{cosec}^2\theta)$$

$$= 2\left(\frac{1}{\sin^2\theta}\right)$$

$$= 2\left(\frac{1}{\left(\frac{1}{3}\right)^2}\right)$$

$$= \frac{2}{1/9}$$

$$= \frac{2 \times 9}{1}$$

$$= 18$$

$$76. 2\cos^2\theta + \frac{2}{1+\cot^2\theta} = 2\cos^2\theta + \frac{2}{\operatorname{cosec}^2\theta}$$

$$= 2\cos^2\theta + 2\sin^2\theta$$

$$= 2(\cos^2\theta + \sin^2\theta)$$

$$= 2(1)$$

$$= 2$$

$$77. \frac{5}{\cot^2\theta} - \frac{5}{\cos^2\theta} = 5\left(\frac{1}{\cot^2\theta} - \frac{1}{\cos^2\theta}\right)$$

$$= 5(\tan^2\theta - \sec^2\theta)$$

$$= 5[\tan^2\theta - (1 + \tan^2\theta)]$$

$$= 5[\tan^2\theta - 1 - \tan^2\theta]$$

$$= 5(-1)$$

$$= -5$$

$$78. \sec^2A(1+\sin A)(1-\sin A) = k$$

$$\sec^2A(1 - \sin^2A) = k$$

$$\frac{1}{\cos^2A}(\cos^2A) = k$$

$$\therefore k = 1$$

IV. Three Marks Questions :-

$$79. \text{LHS} = \frac{\sin A}{1-\cot A} + \frac{\cos A}{1-\tan A}$$

$$= \frac{\sin A}{1-\frac{\cos A}{\sin A}} + \frac{\cos A}{1-\frac{\sin A}{\cos A}}$$

$$\begin{aligned}
&= \frac{\sin A}{\frac{\sin A - \cos A}{\sin A}} + \frac{\cos A}{\frac{\cos A - \sin A}{\cos A}} \\
&= \frac{\sin^2 A}{\sin A - \cos A} + \frac{\cos^2 A}{\cos A - \sin A} \\
&= \frac{\sin^2 A}{\sin A - \cos A} - \frac{\cos^2 A}{\sin A - \cos A} \\
&= \frac{\sin^2 A - \cos^2 A}{\sin A - \cos A} \\
&= \frac{(\sin A + \cos A)(\sin A - \cos A)}{\sin A - \cos A} \\
&= \sin A + \cos A = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
80. \text{ LHS} &= \frac{1 + \cos A}{\sin A} - \frac{\sin A}{1 + \cos A} \\
&= \frac{(1 + \cos A)^2 - \sin^2 A}{\sin A(1 + \cos A)} \\
&= \frac{1 + \cos^2 A + 2\cos A - \sin^2 A}{\sin A(1 + \cos A)} \\
&= \frac{1 + \cos^2 A + 2\cos A - (1 - \cos^2 A)}{\sin A(1 + \cos A)} \\
&= \frac{1 + \cos^2 A + 2\cos A - 1 + \cos^2 A}{\sin A(1 + \cos A)} \\
&= \frac{2\cos^2 A + 2\cos A}{\sin A(1 + \cos A)} \\
&= \frac{2\cos A(\cos A + 1)}{\sin A(1 + \cos A)} \\
&= \frac{2\cos A}{\sin A} \\
&= 2\cot A = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
81. \text{ LHS} &= \frac{1 + \sin A}{\cos A} - \frac{\cos A}{1 + \sin A} \\
&= \frac{(1 + \sin A)^2 - \cos^2 A}{\cos A(1 + \sin A)} \\
&= \frac{1 + \sin^2 A + 2\sin A - \cos^2 A}{\cos A(1 + \sin A)} \\
&= \frac{1 + \sin^2 A + 2\sin A - (1 - \sin^2 A)}{\cos A(1 + \sin A)} \\
&= \frac{1 + \sin^2 A + 2\sin A - 1 + \sin^2 A}{\cos A(1 + \sin A)} \\
&= \frac{2\sin^2 A + 2\sin A}{\cos A(1 + \sin A)} \\
&= \frac{2\sin A(\sin A + 1)}{\cos A(1 + \sin A)} \\
&= \frac{2\sin A}{\cos A} \\
&= 2\tan A = \text{RHS}
\end{aligned}$$

$$82. \text{ LHS} = \frac{\cos \theta - 2\cos^3 \theta}{2\sin^3 \theta - \sin \theta}$$

$$\begin{aligned}
&= \frac{\cos\theta(1-2\cos^2\theta)}{\sin\theta(2\sin^2\theta-1)} \\
&= \frac{\cos\theta(\sin^2\theta+\cos^2\theta-2\cos^2\theta)}{\sin\theta(2\sin^2\theta-\sin^2\theta-\cos^2\theta)} \\
&= \frac{\cos\theta(\sin^2\theta-\cos^2\theta)}{\sin\theta(\sin^2\theta-\cos^2\theta)} \\
&= \frac{\cos\theta}{\sin\theta} \\
&= \cot\theta = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
83. \text{ LHS} &= \frac{\sin\theta-2\sin^3\theta}{2\cos^3\theta-\cos\theta} \\
&= \frac{\sin\theta(1-2\sin^2\theta)}{\cos\theta(2\cos^2\theta-1)} \\
&= \frac{\sin\theta(\cos^2\theta+\sin^2\theta-2\sin^2\theta)}{\cos\theta(2\cos^2\theta-\cos^2\theta-\sin^2\theta)} \\
&= \frac{\sin\theta(\cos^2\theta-\sin^2\theta)}{\cos\theta(\cos^2\theta-\sin^2\theta)} \\
&= \frac{\sin\theta}{\cos\theta} \\
&= \tan\theta = \text{RHS}
\end{aligned}$$

$$\begin{aligned}
84. \text{ LHS} &= \frac{\sin A - \cos A}{\sin A + \cos A} + \frac{\sin A + \cos A}{\sin A - \cos A} \\
&= \frac{(\sin A - \cos A)^2 + (\sin A + \cos A)^2}{(\sin A + \cos A)(\sin A - \cos A)} \\
&= \frac{\sin^2 A + \cos^2 A - 2\sin A \cos A + \sin^2 A + \cos^2 A + 2\sin A \cos A}{\sin^2 A - \cos^2 A} \\
&= \frac{1+1}{\sin^2 A - (1-\sin^2 A)} \\
&= \frac{2}{\sin^2 A - 1 + \sin^2 A} \\
&= \frac{2}{2\sin^2 A - 1} = \text{RHS}
\end{aligned}$$

$$85. x = p \tan\theta + q \sec\theta$$

$$y = p \sec\theta + q \tan\theta$$

$$x^2 = (p \tan\theta + q \sec\theta)^2 = p^2 \tan^2\theta + q^2 \sec^2\theta + 2pq \tan\theta \cdot \sec\theta \dots\dots (1)$$

$$y^2 = (p \sec\theta + q \tan\theta)^2 = p^2 \sec^2\theta + q^2 \tan^2\theta + 2pq \tan\theta \cdot \sec\theta \dots\dots (2)$$

Equation (1) – (2) gives

$$\begin{aligned}
x^2 - y^2 &= p^2 \tan^2\theta + q^2 \sec^2\theta + 2pq \tan\theta \sec\theta - p^2 \sec^2\theta - q^2 \tan^2\theta - 2pq \tan\theta \sec\theta \\
&= p^2(\tan^2\theta - \sec^2\theta) + q^2(\sec^2\theta - \tan^2\theta) \\
&= p^2(\tan^2\theta - \sec^2\theta) - q^2(\tan^2\theta - \sec^2\theta) \\
&= p^2(-1) - q^2(-1) \\
&= -p^2 + q^2
\end{aligned}$$

$$= q^2 - p^2 = \text{RHS}$$

$$\begin{aligned} 86. \text{ LHS} &= (\sec\theta - \cos\theta)\{(\operatorname{cosec}\theta - \sin\theta)(\tan\theta + \cot\theta)\} \\ &= \left\{\frac{1}{\cos\theta} - \cos\theta\right\} \left\{\frac{1}{\sin\theta} - \sin\theta\right\} \left\{\frac{\sin\theta}{\cos\theta} + \frac{\cos\theta}{\sin\theta}\right\} \\ &= \left\{\frac{1-\cos^2\theta}{\cos\theta}\right\} \left\{\frac{1-\sin^2\theta}{\sin\theta}\right\} \left\{\frac{\sin^2\theta+\cos^2\theta}{\sin\theta\cos\theta}\right\} \\ &= \left\{\frac{\sin^2\theta}{\cos\theta}\right\} \left\{\frac{\cos^2\theta}{\sin\theta}\right\} \left\{\frac{1}{\sin\theta\cos\theta}\right\} \\ &= 1 = \text{RHS} \end{aligned}$$

$$\begin{aligned} 87. \text{ LHS} &= \frac{\sec A + \tan A - 1}{\tan A - \sec A + 1} \\ &= \frac{\sec A + \tan A - (\sec^2 A - \tan^2 A)}{\tan A - \sec A + 1} \\ &= \frac{(\sec A + \tan A) - (\sec A + \tan A)(\sec A - \tan A)}{\tan A - \sec A + 1} \\ &= \frac{(\sec A + \tan A)[1 - (\sec A - \tan A)]}{\tan A - \sec A + 1} \\ &= \frac{(\sec A + \tan A)[1 - \sec A + \tan A]}{\tan A - \sec A + 1} \\ &= \sec A + \tan A \\ &= \frac{1}{\cos A} + \frac{\sin A}{\cos A} \\ &= \frac{1 + \sin A}{\cos A} = \text{RHS} \end{aligned}$$

$$\begin{aligned} 88. \text{ LHS} &= \frac{\sin\theta}{1-\cos\theta} + \frac{\tan\theta}{1+\cos\theta} \\ &= \frac{\sin\theta(1+\cos\theta) + \tan\theta(1-\cos\theta)}{(1-\cos\theta)(1+\cos\theta)} \\ &= \frac{\sin\theta + \sin\theta\cos\theta + \tan\theta - \tan\theta\cos\theta}{1-\cos^2\theta} \\ &= \frac{\sin\theta + \sin\theta\cos\theta + \tan\theta - \sin\theta}{\sin^2\theta} \\ &= \frac{\sin\theta\cos\theta + \tan\theta}{\sin^2\theta} \\ &= \frac{\sin\theta\cos\theta}{\sin^2\theta} + \frac{\tan\theta}{\sin^2\theta} \\ &= \frac{\cos\theta}{\sin\theta} + \frac{1}{\cos\theta} \cdot \frac{1}{\sin\theta} \\ &= \cot\theta + \sec\theta \cdot \operatorname{cosec}\theta = \text{RHS} \end{aligned}$$

$$\begin{aligned} 89. \text{ LHS} &= \frac{\tan A - \sin A}{\tan A + \sin A} \\ &= \frac{\frac{\sin A}{\cos A} - \sin A}{\frac{\sin A}{\cos A} + \sin A} \end{aligned}$$

$$= \frac{\sin A \left(\frac{1}{\cos A} - 1 \right)}{\sin A \left(\frac{1}{\cos A} + 1 \right)}$$

$$= \frac{\sec A - 1}{\sec A + 1} = \text{RHS}$$

$$90. \text{ LHS} = (\sin a + \operatorname{cosec} a)^2 + (\cos a + \sec a)^2$$

$$= \sin^2 a + \operatorname{cosec}^2 a + 2 \sin a \operatorname{cosec} a + \cos^2 a + \sec^2 a + 2 \cos a \sec a$$

$$= 1 + 1 + \cot^2 a + 2 \sin a \frac{1}{\sin a} + 1 + \tan^2 a + 2 \cos a \frac{1}{\cos a}$$

$$= 2 + \cot^2 a + 2 + 1 + \tan^2 a + 2$$

$$= 7 + \tan^2 a + \cot^2 a = \text{RHS}$$

$$91. \text{ LHS} = \sec \theta (1 - \sin \theta) (\sec \theta + \tan \theta)$$

$$= (\sec \theta - \sec \theta \cdot \sin \theta) (\sec \theta + \tan \theta)$$

$$= \left(\sec \theta - \frac{1}{\cos \theta} \cdot \sin \theta \right) (\sec \theta + \tan \theta)$$

$$= (\sec \theta - \tan \theta) (\sec \theta + \tan \theta)$$

$$= \sec^2 \theta - \tan^2 \theta$$

$$= 1 + \tan^2 \theta - \tan^2 \theta$$

$$= 1 = \text{RHS}$$

$$92. \text{ LHS} = \operatorname{cosec} a (1 - \cos a) (\operatorname{cosec} a + \cot a)$$

$$= (\operatorname{cosec} a - \operatorname{cosec} a \cdot \cos a) (\operatorname{cosec} a + \cot a)$$

$$= \left(\operatorname{cosec} a - \frac{1}{\sin a} \cdot \cos a \right) (\operatorname{cosec} a + \cot a)$$

$$= (\operatorname{cosec} a - \cot a) (\operatorname{cosec} a + \cot a)$$

$$= \operatorname{cosec}^2 a - \cot^2 a$$

$$= 1 + \cot^2 a - \cot^2 a$$

$$= 1 = \text{RHS}$$

$$93. (\operatorname{cosec} a - \sin a) (\sec a - \cos a)$$

$$= \left(\frac{1}{\sin a} - \sin a \right) \left(\frac{1}{\cos a} - \cos a \right)$$

$$= \left(\frac{1 - \sin^2 a}{\sin a} \right) \left(\frac{1 - \cos^2 a}{\cos a} \right)$$

$$= \sin a \cdot \cos a \dots \dots (1)$$

$$\frac{1}{\tan a + \cot a} = \frac{1}{\frac{\sin a}{\cos a} + \frac{\cos a}{\sin a}}$$

$$= \frac{1}{\frac{\sin^2 a + \cos^2 a}{\sin a \cdot \cos a}} = \left(\frac{\cos^2 a}{\sin a} \right) \left(\frac{\sin^2 a}{\cos a} \right)$$

$$= \frac{\sin a \cdot \cos a}{1}$$

$$= \sin a \cdot \cos a \dots \dots (2)$$

From (1) & (2)

$$(\operatorname{cosec} A - \sin A)(\sec A - \cos A) = \frac{1}{\tan A + \cot A}$$

$$\begin{aligned} 94. \text{ LHS} &= \sqrt{\frac{1+\cos A}{1-\cos A}} = \sqrt{\frac{1+\cos A}{1-\cos A} \times \frac{1+\cos A}{1+\cos A}} \\ &= \sqrt{\frac{(1+\cos A)^2}{1-\cos A}} = \sqrt{\frac{(1+\cos A)^2}{\sin^2 A}} \\ &= \sqrt{\left(\frac{1+\cos A}{\sin A}\right)^2} = \frac{1+\cos A}{\sin A} \\ &= \frac{1}{\sin A} + \frac{\cos A}{\sin A} = \operatorname{cosec} A + \cot A = \text{RHS} \end{aligned}$$

$$\begin{aligned} 95. \text{ LHS} &= \sqrt{\frac{1+\sin A}{1-\sin A}} = \sqrt{\frac{1+\sin A}{1-\sin A} \times \frac{1+\sin A}{1+\sin A}} \\ &= \sqrt{\frac{(1+\sin A)^2}{1-\sin A}} = \sqrt{\frac{(1+\sin A)^2}{\cos^2 A}} \\ &= \sqrt{\left(\frac{1+\sin A}{\cos A}\right)^2} = \frac{1+\sin A}{\cos A} \\ &= \frac{1}{\cos A} + \frac{\sin A}{\cos A} = \sec A + \tan A = \text{RHS} \end{aligned}$$

$$\begin{aligned} 96. \text{ LHS} &= (\sec A - \cos A)(\cot A + \tan A) \\ &= \left(\frac{1}{\cos A} - \cos A\right) \left(\frac{\cos A}{\sin A} + \frac{\sin A}{\cos A}\right) \\ &= \left(\frac{1-\cos^2 A}{\cos A}\right) \left(\frac{\sin^2 A + \cos^2 A}{\sin A \cos A}\right) \\ &= \left(\frac{\sin^2 A}{\cos A}\right) \left(\frac{1}{\sin A \cos A}\right) \\ &= \left(\frac{\sin A}{\cos A}\right) \left(\frac{1}{\cos A}\right) \\ &= \tan A \cdot \sec A \\ &= \text{RHS} \end{aligned}$$

$$\begin{aligned} 97. \text{ LHS} &= (\operatorname{cosec} A - \sin A)(\tan A + \cot A) \\ &= \left(\frac{1}{\sin A} - \sin A\right) \left(\frac{\sin A}{\cos A} + \frac{\cos A}{\sin A}\right) \\ &= \left(\frac{1-\sin^2 A}{\sin A}\right) \left(\frac{\sin^2 A + \cos^2 A}{\sin A \cos A}\right) \\ &= \left(\frac{\cos^2 A}{\sin A}\right) \left(\frac{1}{\sin A \cos A}\right) \\ &= \left(\frac{\cos A}{\sin A}\right) \left(\frac{1}{\sin A}\right) \\ &= \cot A \cdot \operatorname{cosec} A = \text{RHS} \end{aligned}$$

$$98. \tan\theta = \sqrt{3}, \quad \therefore \theta = 60^\circ$$

$$\begin{aligned} \frac{4\sin\theta - \cos\theta - 1}{4\sin\theta + \cos\theta + 1} &= \frac{4\sin 60^\circ - \cos 60^\circ - 1}{4\sin 60^\circ + \cos 60^\circ + 1} = \frac{4X\frac{\sqrt{3}}{2} - \frac{1}{2} - 1}{4X\frac{\sqrt{3}}{2} + \frac{1}{2} + 1} \\ &= \frac{2\sqrt{3} - \frac{3}{2}}{2\sqrt{3} + \frac{3}{2}} \\ &= \frac{\frac{4\sqrt{3} - 3}{2}}{\frac{4\sqrt{3} + 3}{2}} = \frac{4\sqrt{3} - 3}{4\sqrt{3} + 3} \end{aligned}$$

$$\begin{aligned} 99. \frac{2\cos(90^\circ - 30^\circ) + \tan 45^\circ - \sqrt{3}\operatorname{cosec} 60^\circ}{\sqrt{3}\sec 30^\circ + 2\cos 60^\circ + \cot 45^\circ} \\ &= \frac{2\cos(60^\circ) + \tan 45^\circ - \sqrt{3}\operatorname{cosec} 60^\circ}{\sqrt{3}\sec 30^\circ + 2\cos 60^\circ + \cot 45^\circ} \\ &= \frac{2\left(\frac{1}{2}\right) + 1 - \sqrt{3}\left(\frac{2}{\sqrt{3}}\right)}{\sqrt{3}\left(\frac{2}{\sqrt{3}}\right) + 2\left(\frac{1}{2}\right) + 1} \\ &= \frac{1 + 1 - 2}{2 + 1 + 1} \\ &= \frac{2 - 2}{4} \\ &= 0 \end{aligned}$$

$$\begin{aligned} 100. \quad \text{LHS} &= \frac{\cos^3\theta + \sin^3\theta}{\cos\theta + \sin\theta} + \frac{\cos^3\theta - \sin^3\theta}{\cos\theta - \sin\theta} \\ &= \left[\frac{\cos^3\theta + \sin^3\theta}{\cos\theta + \sin\theta} \right] + \left[\frac{\cos^3\theta - \sin^3\theta}{\cos\theta - \sin\theta} \right] \\ &= \left[\frac{(\cos\theta + \sin\theta)(\cos^2\theta + \sin^2\theta - \cos\theta\sin\theta)}{\cos\theta + \sin\theta} \right] \\ &\quad + \left[\frac{(\cos\theta - \sin\theta)(\cos^2\theta + \sin^2\theta + \cos\theta\sin\theta)}{\cos\theta - \sin\theta} \right] \\ &= \left[\frac{(\cos\theta + \sin\theta)(1 - \cos\theta\sin\theta)}{\cos\theta + \sin\theta} \right] + \left[\frac{(\cos\theta - \sin\theta)(1 + \cos\theta\sin\theta)}{\cos\theta - \sin\theta} \right] \\ &= (1 - \cos\theta\sin\theta) + (1 + \cos\theta\sin\theta) \\ &= 1 - \cos\theta\sin\theta + 1 + \cos\theta\sin\theta \\ &= 2 = \text{RHS} \end{aligned}$$

Unit : 09 SOME APPLICATIONS OF TRIGONOMETRY

I. Multiple choice questions

1. B) 30°

2. A) 60°

3. C) 60°

4. D) 45°

5. C) 2cm

II. ONE MARK QUESTIONS

6. 10m

7. Angle of elevation

8. Angle of depression

9. 12m

10. 45°

V. TWO MARK QUESTIONS

11 Angle of elevation = 30°

The distance of the tower from the point = $AB = 30\text{m}$

Height of the tower = $BC = ?$

$$\tan\theta = \frac{\text{Opposite side}}{\text{Adjacent side}} = \frac{BC}{AB}$$

$$\tan 30^\circ = \frac{BC}{30}$$

$$\frac{1}{\sqrt{3}} = \frac{BC}{30}$$

$$BC = \frac{30}{\sqrt{3}} = \frac{10 \times 3}{\sqrt{3}} = 10\sqrt{3} \text{ m}$$

$$BC = 10\sqrt{3} \text{ m}$$

12.. Let the height of the tower = AB

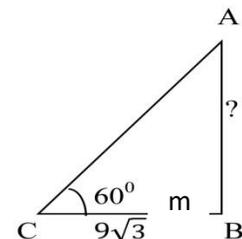
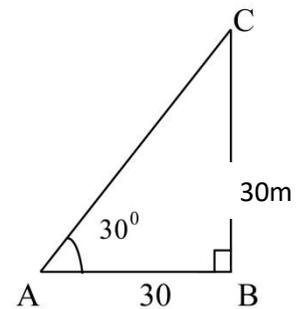
Distance from the foot of the tower to the point = $9\sqrt{3} \text{ m}$

Angle of elevation = 60°

$$\text{In } \triangle ABC \quad \tan \theta = \frac{AB}{BC}$$

$$\tan 60^\circ = \frac{AB}{9\sqrt{3}}$$

$$\sqrt{3} = \frac{AB}{9\sqrt{3}}$$



$$AB = 9\sqrt{3} \times \sqrt{3}$$

$$AB = 9 \times 3 = 27\text{m}$$

∴ **Height of the tower = AB = 27m**

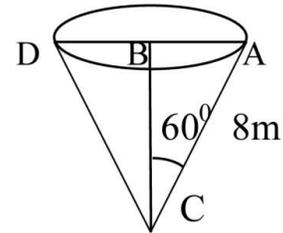
13. $\sin \theta = \frac{\text{Opposite side}}{\text{Hypotenuse}} = \frac{AB}{AC}$

$$\sin 60^\circ = \frac{AB}{8}$$

$$\frac{\sqrt{3}}{2} = \frac{AB}{8}$$

$$AB = 4\sqrt{3} \text{ m}$$

∴ **Diameter = AD = 2 \times 4\sqrt{3} \text{ m} = 8\sqrt{3} \text{ m}**



14. In $\triangle BCE$

$$\tan \theta = \frac{CE}{BC}$$

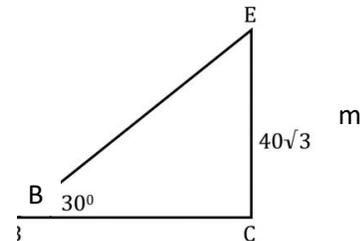
$$\tan 30^\circ = \frac{40\sqrt{3}}{BC}$$

$$\frac{1}{\sqrt{3}} = \frac{40\sqrt{3}}{BC}$$

$$BC = 40 \times \sqrt{3} \times \sqrt{3}$$

$$BC = 40 \times 3$$

$$BC = 120\text{m}$$



∴ The distance between the person and the foot of windmill = **120m**

15. Height of the building = $50\sqrt{3} \text{ m}$

Angle of depression = 60°

The distance of the object from the Foot of a building = QR = ?

$$\angle MPR = \theta = 60^\circ$$

$$\therefore \angle PRQ = \theta = 60^\circ \quad [\because PM \parallel QR, \text{ Alternate angles}]$$

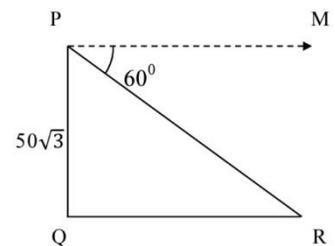
$$\tan 60^\circ = \frac{PQ}{QR}$$

$$\sqrt{3} = \frac{50\sqrt{3}}{QR}$$

$$QR = \frac{50\sqrt{3}}{\sqrt{3}}$$

$$QR = \frac{50\sqrt{3}}{\sqrt{3}}$$

∴ **The distance of the object from the Foot of a building = QR = 50m**



IV. THREE MARK QUESTIONS

16. Distance between wind mills = $AB + BC = ?$

In $\triangle ABD$

$$\tan \theta = \frac{AD}{AB}$$

$$\tan 45^\circ = \frac{50}{AB}$$

$$1 = \frac{50}{AB}$$

$$\mathbf{AB = 50m}$$

In $\triangle BCE$

$$\tan \theta = \frac{CE}{BC}$$

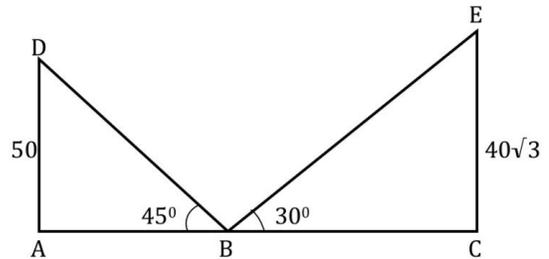
$$\tan 30^\circ = \frac{40\sqrt{3}}{BC}$$

$$\frac{1}{\sqrt{3}} = \frac{40\sqrt{3}}{BC}$$

$$BC = 40 \times \sqrt{3} \times \sqrt{3}$$

$$BC = 40 \times 3$$

$$\mathbf{BC = 120m}$$



\therefore Distance between wind mills = $AB + BC = 50 + 120 = 170 \text{ m.}$

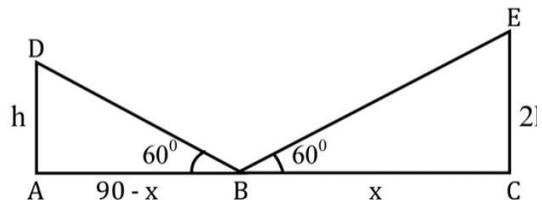
17. Width of the road = $AC = 90$ feet

Height of the short pole = $AD = h = ?$

Height of the long pole = $CE = 2h = ?$

Angle of elevation = 60°

Let $BC = x$, then $AB = 90 - x$



In $\triangle ABD$

$$\tan 60^\circ = \frac{AD}{AB}$$

$$\sqrt{3} = \frac{h}{90-x}$$

$$h = (90-x)\sqrt{3} \text{ ----- (1)}$$

In $\triangle BCE$

$$\tan 60^\circ = \frac{CE}{BC}$$

$$\sqrt{3} = \frac{2h}{x}$$

$$2h = x\sqrt{3}$$

$$h = x \cdot \frac{\sqrt{3}}{2} \text{ ----- (2)}$$

From Eqn(1) and Eqn(2),

$$\begin{aligned}(90-x)\sqrt{3} &= x \cdot \frac{\sqrt{3}}{2} \\ 2(90-x)\sqrt{3} &= x \cdot \sqrt{3} \\ 180 - 2x &= x \\ 3x &= 180 \\ \mathbf{x} &= \mathbf{60}\end{aligned}$$

Substitute $x = 60$ in Eqn (1) then

$$h = (90-x)\sqrt{3} = (90-60)\sqrt{3} = 30\sqrt{3} \text{ m}$$

Height of the short pole = AD = h = $30\sqrt{3}$ feet

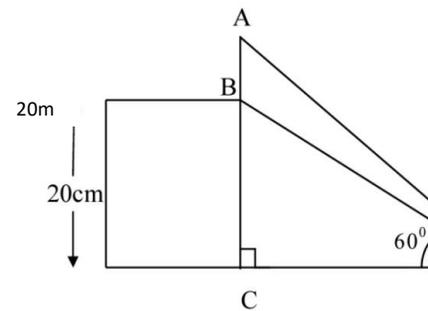
Height of the long pole = CE = 2h = $60\sqrt{3}$ feet

18. Height of the building = BC = 20m
 Angle of Elevation = $\theta = 60^\circ$ and 45°
 Height of the transmission tower = AB = ?

$$\begin{aligned}\text{In } \triangle BCD \quad \tan \theta &= \frac{BC}{CD} \\ \tan 45^\circ &= \frac{20}{CD} \\ 1 &= \frac{20}{CD} \\ \therefore CD &= 20\text{m}\end{aligned}$$

$$\begin{aligned}\text{In } \triangle ACD \quad \tan \theta &= \frac{AC}{CD} \\ \tan 60^\circ &= \frac{AB+BC}{20} \\ \sqrt{3} &= \frac{AB+20}{20} \\ \sqrt{3} \times 20 &= AB + 20 \\ AB &= 20(\sqrt{3} - 1) \text{ m}\end{aligned}$$

\therefore Height of the transmission tower = AB = $20(\sqrt{3} - 1)$ m



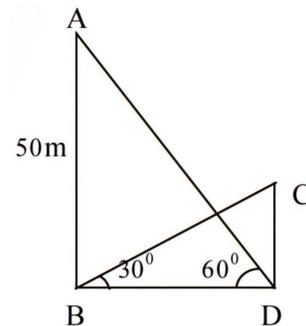
19. In $\triangle ABD$ $\tan 60^\circ = \frac{AB}{BD}$
 $\sqrt{3} = \frac{50}{BD}$
 $BD = \frac{50}{\sqrt{3}}$ -----(1)

In $\triangle BDC$ $\tan 30^\circ = \frac{DC}{BD}$
 $\frac{1}{\sqrt{3}} = \frac{DC}{BD}$
 $BD = \sqrt{3} \cdot DC$ ----- (2)

From equation (1) and (2)

$$\begin{aligned}\sqrt{3} \cdot DC &= \frac{50}{\sqrt{3}} \\ DC &= \frac{50}{\sqrt{3} \times \sqrt{3}}\end{aligned}$$

\therefore Height of the building = DC = $\frac{50}{3} \text{ m} = 16.67\text{m}$



20. Height of the building is 7 m.
 Height of the tower = CD = CE + DE = ?
 $\therefore AB \parallel CD$, $AB = DE = 7$ m and $AE = BD$.

$$AE \parallel BD \therefore \angle BDA = 45^\circ$$

$$\text{In } \triangle ABD \quad \tan 45^\circ = \frac{AB}{BD}$$

$$1 = \frac{AB}{BD}$$

$$BD = AB$$

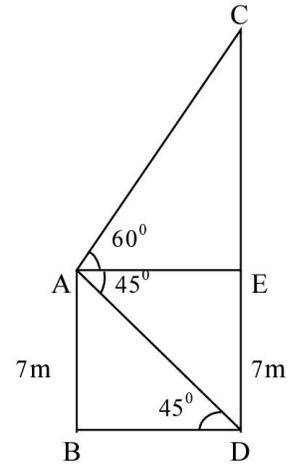
$$BD = 7\text{m}$$

$$\text{In } \triangle ACE \quad \tan 60^\circ = \frac{CE}{AE}$$

$$\sqrt{3} = \frac{CE}{7}$$

$$CE = 7\sqrt{3}$$

$$\therefore \text{Height of the tower} = CE + DE = 7\sqrt{3} + 7 = 7(\sqrt{3} + 1) \text{ m}$$



V. FOUR MARK QUESTIONS

- 21 Height of the tower = 60m.
 Height of the pole = CD = h m. and BE = CD = h m.

$$\text{Let } BD = EC = x$$

$$\therefore AE = (60 - h) \text{ m.}$$

$$\angle ACE = 30^\circ$$

$$\angle ADB = 60^\circ$$

In $\triangle AEC$

$$\tan 30^\circ = \frac{AE}{EC}$$

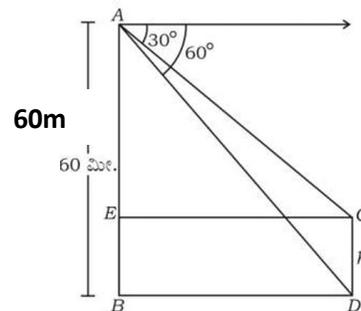
$$\frac{1}{\sqrt{3}} = \frac{60-h}{x}$$

$$x = \sqrt{3}(60 - h) \text{ -----(1)}$$

In $\triangle ABD$ $\tan 60^\circ = \frac{AB}{BD}$

$$\sqrt{3} = \frac{60}{x}$$

$$x = \frac{60}{\sqrt{3}} \text{ -----(2)}$$



From Eqn(1) and Eqn(2)

$$\sqrt{3}(60 - h) = \frac{60}{\sqrt{3}}$$

$$(60 - h) = \frac{60}{\sqrt{3} \times \sqrt{3}}$$

$$(60 - h) = \frac{60}{3}$$

$$(60 - h) = 20$$

$$h = 60 - 20$$

$$h = 40 \text{ m}$$

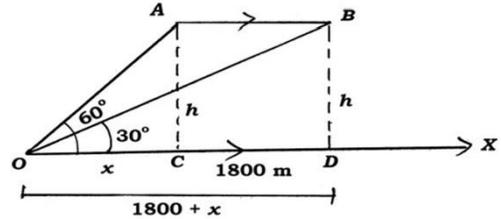
Height of the pole = CD = h = 40m

22. Velocity = $648 \text{ km/h} = \frac{648 \times 1000}{3600}$
 $= 180 \text{ m/sec.}$

After 10 seconds distance travelled by aircraft = $180 \times 10 = 1800 \text{ m}$

In the diagram $OC = x$ $CD = 1800 \text{ m}$ $OD = 1800 + x$

In $\triangle OAC$ $\angle C = 90^\circ$ $\tan \theta = \frac{AC}{OC}$
 $\tan 60^\circ = \frac{h}{x}$
 $\sqrt{3} = \frac{h}{x}$
 $h = \sqrt{3} x$ ----- (i)



In $\triangle ODB$ $\angle D = 90^\circ$, $\tan \theta = \frac{BD}{OD}$
 $\tan 30^\circ = \frac{h}{1800+x}$
 $\frac{1}{\sqrt{3}} = \frac{h}{1800+x}$
 $\sqrt{3} h = 1800 + x$ ----- (ii)

Substitute Eqn (i) in Eqn (ii)

$x\sqrt{3} \cdot \sqrt{3} = 1800 + x$
 $3x = 1800 + x$
 $3x - x = 1800$
 $2x = 1800$
 $x = \frac{1800}{2} = 900$

$\therefore h = \sqrt{3} x = 900 \cdot \sqrt{3} = 900 \times 1.73$

$\therefore h = 1557 \text{ m}$

23. Height of the tower = AC = ?

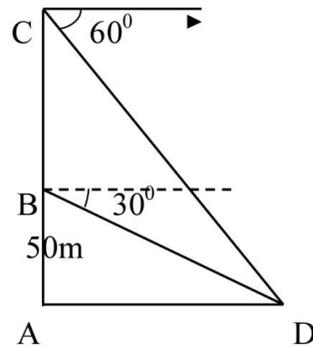
Height of the tower from the foot to point B = AB = 50m.

Angle of depression = 60° and 30°

$\therefore \angle ADB = 30^\circ$
 $\angle ADC = 60^\circ$

In $\triangle ABD$, $\tan \theta = \frac{AB}{AD}$

$\tan 30^\circ = \frac{50}{AD}$
 $\frac{1}{\sqrt{3}} = \frac{50}{AD}$



$$AD = 50\sqrt{3} \text{ m} \text{ -----(1)}$$

In ΔADC , $\tan 60^\circ = \frac{AC}{AD}$

$$\sqrt{3} = \frac{AC}{50\sqrt{3}}$$

$$AC = 50\sqrt{3} \times \sqrt{3}$$

$$AC = 50 \times 3 = 150 \text{ m}$$

\therefore Height of the tower = AC = 150m

24. Height of the cylinder = CD = 10 ft

Height of the conical shaped tomb = AE = ?

Angle of Elevations $\theta = 30^\circ$ and 45°

In ΔPCD , $\tan \theta = \frac{CD}{PD}$

$$\tan 30^\circ = \frac{10}{PD}$$

$$\frac{1}{\sqrt{3}} = \frac{10}{PD}$$

$$PD = 10\sqrt{3} = 10 \times 1.73 = 17.3 \text{ ft}$$

Diameter of the cylinder = 9.4 ft

Radius = BD = 4.7 ft

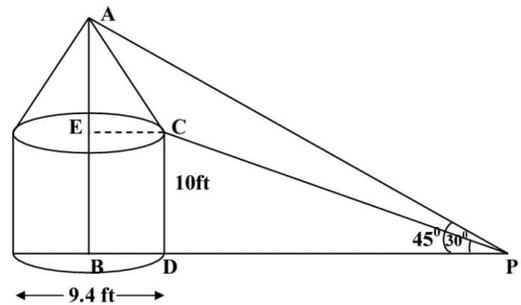
So, BP = BD + PD = 4.7 + 17.3 = 22 ft

In ΔABP , $\tan 45^\circ = \frac{AB}{BP}$

$$1 = \frac{AB}{22}$$

$$AB = 22 \text{ ft}$$

Height of the conical shaped tomb = AE = AB - EB = 22 - 10 = 12 ft

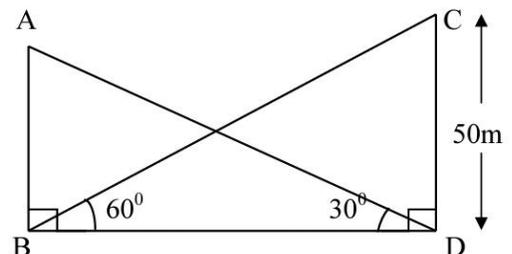


25. In ΔABC , $\tan 60^\circ = \frac{CD}{BD}$

$$\sqrt{3} = \frac{50}{BD}$$

$$BD = \frac{50}{\sqrt{3}} \text{ -----(1)}$$

In ΔABD , $\tan 30^\circ = \frac{AB}{BD}$



$$\frac{1}{\sqrt{3}} = \frac{AB}{BD}$$

$$BD = \sqrt{3} \cdot AB \text{ ----- (2)}$$

From (1) and (2)

$$\sqrt{3} \cdot AB = \frac{50}{\sqrt{3}}$$

$$\therefore \text{Height of the building} = AB = \frac{50}{3} \text{ m}$$

26. Distance between two ships is PQ

$$\text{In } \triangle ABP, \tan 45^\circ = \frac{AB}{BP}$$

$$1 = \frac{75}{BP}$$

$$BP = 75$$

$$\text{In } \triangle ABQ, \tan 30^\circ = \frac{AB}{BQ}$$

$$\frac{1}{\sqrt{3}} = \frac{75}{BP+PQ}$$

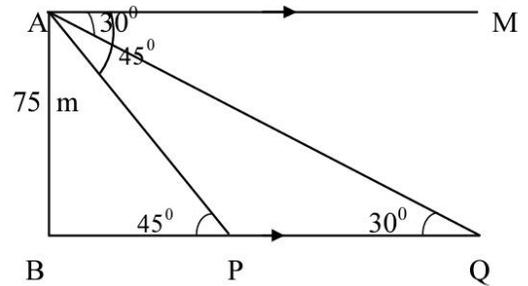
$$\frac{1}{\sqrt{3}} = \frac{75}{75+PQ}$$

$$75 + PQ = 75\sqrt{3}$$

$$PQ = 75\sqrt{3} - 75$$

$$PQ = 75(\sqrt{3} - 1) \text{ m}$$

$$\therefore \text{Distance between two ships} = PQ = 75(\sqrt{3} - 1) \text{ m}$$



27. Height of the building = AB

Angle of depression = 60° and angle of elevation = 30° ,

We have to prove that $CP = 2BC$.

$$\therefore \angle ACB = 60^\circ$$

$$\text{In } \triangle ABC, \tan \theta = \frac{AB}{BC}$$

$$\tan 60^\circ = \frac{AB}{BC}$$

$$\sqrt{3} = \frac{AB}{BC}$$

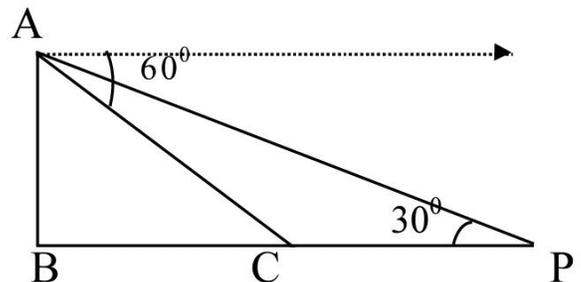
$$AB = \sqrt{3} BC \text{ -----(1)}$$

$$\text{In } \triangle ABP, \tan 30^\circ = \frac{AB}{BP}$$

$$\frac{1}{\sqrt{3}} = \frac{AB}{BP}$$

$$AB = \frac{BP}{\sqrt{3}} \text{ -----(2)}$$

From equation (1) and (2)



$$\begin{aligned}\sqrt{3} BC &= \frac{BP}{\sqrt{3}} \\ 3BC &= BP \\ 3BC &= BC + CP \\ 3BC - BC &= CP \\ 2BC &= CP \\ \therefore CP &= 2BC\end{aligned}$$

28.

The distance of the point from the foot of the tower = $BC = 30\sqrt{3}$ m

Height of the building = $DE = 10$ m

The distance between the foot of the tower and building = $BE = ?$

The distance between their tops = $AD = ?$

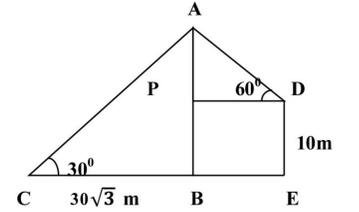
In ΔABC , $\tan \theta = \frac{AB}{BC}$

$$\begin{aligned}\tan 30^\circ &= \frac{AB}{30\sqrt{3}} \\ \frac{1}{\sqrt{3}} &= \frac{AB}{30\sqrt{3}} \\ AB &= 30 \text{ m}\end{aligned}$$

$$AP = AB - PB = 30 - 10 = 20 \text{ m}$$

In ΔAPD , $\tan \theta = \frac{AP}{PD}$

$$\begin{aligned}\tan 60^\circ &= \frac{20}{PD} \\ \sqrt{3} &= \frac{20}{PD} \\ PD &= \frac{20}{\sqrt{3}}\end{aligned}$$



\therefore The distance between the foot of the tower and building = $BE = PD = \frac{20}{\sqrt{3}}$ m

$$\begin{aligned}\Delta APD \text{ ಯಲ್ಲಿ, } \sin \theta &= \frac{AP}{AD} \\ \sin 60^\circ &= \frac{20}{AD} \\ \frac{\sqrt{3}}{2} &= \frac{20}{AD} \\ AD &= \frac{40}{\sqrt{3}} \text{ m}\end{aligned}$$

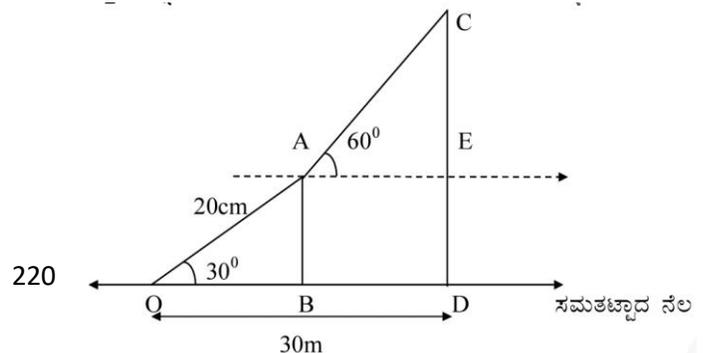
\therefore The distance between their tops = $AD = \frac{40}{\sqrt{3}}$ m

29. In ΔABO , $\sin \theta = \frac{AB}{AO}$

$$\begin{aligned}\sin 30^\circ &= \frac{AB}{20} \\ \frac{1}{2} &= \frac{AB}{20}\end{aligned}$$

$$AB = 10 \text{ cm}$$

$$DE = AB = 10 \text{ cm}$$



$$\cos \theta = \frac{OB}{AO}$$

$$\cos 30^\circ = \frac{OB}{20}$$

$$\frac{\sqrt{3}}{2} = \frac{OB}{20}$$

$$OB = 10\sqrt{3} = 10 \times 1.73 = 17.3 \text{ cm}$$

$$BD = OD - OB = 30 - 17.3 = 12.7 \text{ cm}$$

$$AE = BD = 12.7 \text{ cm}$$

In $\triangle ACE$, $\tan 60^\circ = \frac{CE}{AE}$

$$\sqrt{3} = \frac{CE}{12.7}$$

$$CE = 1.73 \times 12.7 = 21.97 \text{ cm}$$

$$\begin{aligned} \text{Height of the pole} &= CD = CE + DE \\ &= 21.97 + 10 \end{aligned}$$

$$\text{Height of the pole} = 31.97 \text{ cm}$$

30. Height of the balloon from ground = $AB = CD = 88.2 - 1.2 = 87 \text{ m}$

In $\triangle AEB$, $\tan \theta = \frac{AB}{BE}$

$$\tan 30^\circ = \frac{87}{BE}$$

$$\frac{1}{\sqrt{3}} = \frac{87}{BE}$$

$$\mathbf{BE = 87\sqrt{3} \text{ m}}$$

In $\triangle CED$, $\tan \theta = \frac{CD}{DE}$

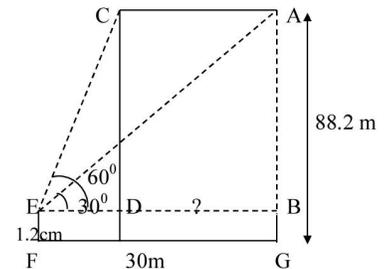
$$\tan 60^\circ = \frac{87}{DE}$$

$$\sqrt{3} = \frac{87}{DE}$$

$$DE = \frac{87}{\sqrt{3}}$$

$$DE = \frac{29 \times 3}{\sqrt{3}}$$

$$\mathbf{DE = 29\sqrt{3} \text{ m}}$$

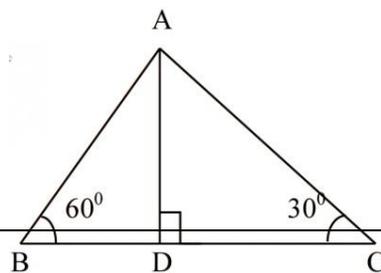


Distance travelled by the balloon = $AC = DB$

$$\begin{aligned} &= BE - DE \\ &= 87\sqrt{3} - 29\sqrt{3} \\ &= 58\sqrt{3} \text{ m} \end{aligned}$$

31. $\angle ABC = 60^\circ$, $\angle ACB = 30^\circ$ then $\angle CAB = 90^\circ$
In right triangle ABC, $\angle CAB = 90^\circ$

$$\sin \theta = \frac{AB}{BC}$$



$$\begin{aligned}\sin 30^\circ &= \frac{AB}{36} \\ \frac{1}{2} &= \frac{AB}{36} \\ AB &= \frac{36}{2} \\ \mathbf{AB} &= \mathbf{18 \text{ cm}}\end{aligned}$$

$$\begin{aligned}\cos \theta &= \frac{AC}{BC} \\ \cos 30^\circ &= \frac{AC}{36} \\ \frac{\sqrt{3}}{2} &= \frac{AC}{36} \\ \mathbf{AC} &= \mathbf{18\sqrt{3} \text{ cm}}\end{aligned}$$

In right triangle ADB, $\angle ADB = 90^\circ$

$$\begin{aligned}\sin \theta &= \frac{AD}{AB} \\ \sin 60^\circ &= \frac{AD}{18} \\ \frac{\sqrt{3}}{2} &= \frac{AD}{18}\end{aligned}$$

$$\mathbf{AD = 9\sqrt{3} \text{ cm}}$$

32. In ΔCPD ,

Let angle CPD be θ

$$\text{Then } \tan \theta = \frac{CD}{PD} = \frac{20\sqrt{3}}{20} = \sqrt{3}$$

$$\therefore \theta = 60^\circ$$

$$\angle APB = 90^\circ - 60^\circ = 30^\circ$$

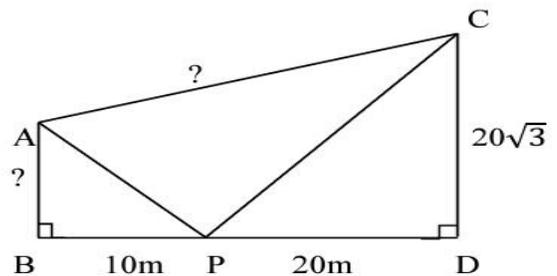
In ΔABP ,

$$\begin{aligned}\tan \theta &= \frac{AB}{BP} \\ \tan 30^\circ &= \frac{AB}{10} \\ \frac{1}{\sqrt{3}} &= \frac{AB}{10} \\ AB &= \frac{10}{\sqrt{3}} \text{ m}\end{aligned}$$

$$\therefore \text{Length of the pole } \mathbf{AB} = \frac{10}{\sqrt{3}} \text{ m}$$

In right ΔPDC , $PC^2 = PD^2 + DC^2$

$$\begin{aligned}&= 20^2 + (20\sqrt{3})^2 \\ &= 400 + (400 \times 3) \\ &= 400 + 1200 \\ PC^2 &= 1600 \dots\dots\dots (1)\end{aligned}$$



$$\begin{aligned} \text{In right } \triangle ABP, AP^2 &= AB^2 + BP^2 \\ &= \left(\frac{10}{\sqrt{3}}\right)^2 + 10^2 \\ &= \frac{100}{3} + 100 \\ &= \frac{100+300}{3} \end{aligned}$$

$$AP^2 = \frac{400}{3} \dots\dots\dots (2)$$

$$\begin{aligned} \text{In right } \triangle APC, AC^2 &= AP^2 + PC^2 \\ &= \frac{400}{3} + 1600 \end{aligned}$$

$$= \frac{400+4800}{3}$$

$$= \frac{5200}{3}$$

$$AC = \sqrt{\frac{400 \times 13}{3}}$$

$$AC = \frac{20\sqrt{13}}{\sqrt{3}} = \frac{20}{3} \times \sqrt{39} \text{ m}$$

\therefore Distance AC between the tops of the poles $AC = \frac{20\sqrt{39}}{3} \text{ m}$

33. Angle of elevation $\theta = 60^\circ$ and 30°

$$\begin{aligned} \text{In } \triangle PMA, \tan 60^\circ &= \frac{AM}{PM} \\ \sqrt{3} &= \frac{300}{PM} \\ PM &= \frac{300}{\sqrt{3}} \end{aligned}$$

$$\text{In } \triangle PMB, \tan 30^\circ = \frac{BM}{PM}$$

$$\begin{aligned} \frac{1}{\sqrt{3}} &= \frac{BM}{\frac{300}{\sqrt{3}}} \\ \sqrt{3} \cdot \sqrt{3} \cdot BM &= 300 \end{aligned}$$

$$3 \cdot BM = 300$$

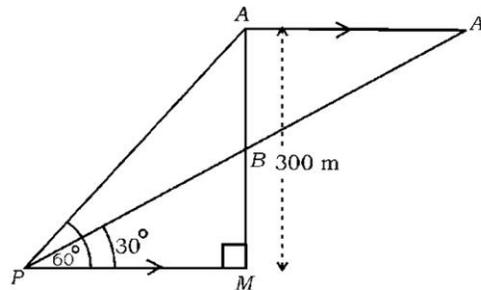
$$BM = \frac{300}{3}$$

$$BM = 100 \text{ m}$$

$$AB = AM - BM = 300 - 100 = 200 \text{ m}$$

In $\triangle ABA^1$, $\angle AA^1B = \angle BPM = 30^\circ$ ($AA^1 \parallel PM$, corresponding angles)

$$\sin 30^\circ = \frac{AB}{A^1B}$$



$$\frac{1}{2} = \frac{200}{A^1B}$$

$$A^1B = 200 \times 2 = 400 \text{ m}$$

The distance between the kites (A^1B) = 400 m

34. Height of the taller tower = $DC = 500 \text{ m}$,
 Distance between the foot of the two towers = $BD = 300 \text{ m}$
 Height of the shorter tower = $AB = ?$

Join AN , MC and NE

Angle of depression $\theta = 60^\circ$ and 30°

$$\angle AHP = \angle HAN = 60^\circ \quad (\text{alternate angles})$$

$$\angle CHQ = \angle HCM = 30^\circ \quad (\text{alternate angles})$$

In $\triangle AHN$, $\tan 60^\circ = \frac{HN}{AN}$

$$\sqrt{3} = \frac{HN}{100\sqrt{3}} \quad (\text{AN} = \text{BG})$$

$$HN = 100\sqrt{3} \times \sqrt{3}$$

$$= 100 \times 3$$

$$\mathbf{HN = 300 \text{ m}}$$

But $GD = 300 - 100\sqrt{3}$

$$= 100 \times 3 - 100\sqrt{3}$$

$$= 100\sqrt{3}(\sqrt{3} - 1)$$

In $\triangle HMC$, $\tan 30^\circ = \frac{HM}{MC}$

$$\frac{1}{\sqrt{3}} = \frac{HM}{100\sqrt{3}(\sqrt{3}-1)}$$

$$HM = 100(\sqrt{3} - 1)$$

$$= 100(1.73 - 1)$$

$$= 100 \times 0.73$$

$$\mathbf{HM = 73 \text{ m}}$$

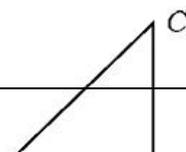
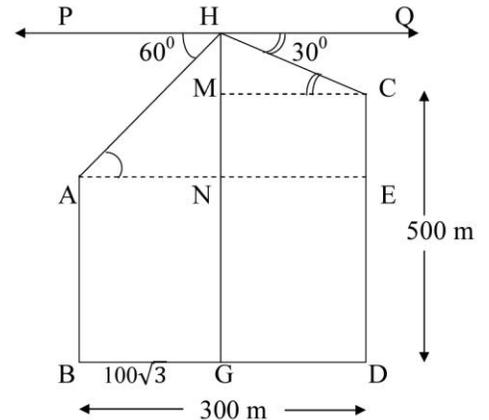
$$MN = HN - HM = 300 - 73$$

$$\mathbf{MN = 227 \text{ m}}$$

\therefore **Height of the short tower = $AB = DE = DC - CE = 500 - 227 = 273 \text{ m}$**

VI. FIVE MARKS QUESTIONS

35. In $\triangle ABD$, $\tan 30^\circ = \frac{AB}{BD}$



$$\frac{1}{\sqrt{3}} = \frac{6}{BD}$$

$$BD = 6\sqrt{3} \text{ m}$$

$$BD = AE = 6\sqrt{3} \text{ m}$$

In $\triangle AEC$, $\tan 60^\circ = \frac{CE}{AE}$

$$\sqrt{3} = \frac{CE}{6\sqrt{3}}$$

$$CE = 6\sqrt{3} \times \sqrt{3} \text{ m}$$

$$CE = 18 \text{ m}$$

In $\triangle AEC$, $\sin 60^\circ = \frac{CE}{AC}$

$$\frac{\sqrt{3}}{2} = \frac{18}{AC}$$

$$AC = \frac{18 \times 2}{\sqrt{3}}$$

$$AC = \frac{36\sqrt{3}}{3}$$

$$AC = 12\sqrt{3} \text{ m}$$

$$CD = CE + DE$$

$$CD = 18 + 6$$

$$CD = 24 \text{ m}$$

36.

The height of light house = $10\sqrt{3} \text{ m}$

The distance between foot of the light house to foot of the tower = $BC = 30 \text{ m}$

The distance between foot of the light house to ship = $BF = 10 \text{ m}$

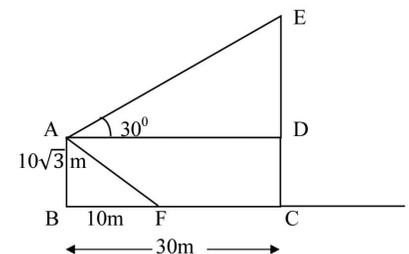
Height of the tower = $CE = ?$

Distance between the top of the light house to the top of the tower = $AE = ?$

Angle of depression = $\theta = ?$

In $\triangle ADE$, $\tan \theta = \frac{DE}{AD}$

$$\tan 30^\circ = \frac{DE}{30}$$



$$\frac{1}{\sqrt{3}} = \frac{DE}{30}$$

$$DE = \frac{30}{\sqrt{3}} \text{ m}$$

∴ Height of the tower = CE = DE + CD

$$= \frac{30}{\sqrt{3}} + 10\sqrt{3}$$

$$= \left(\frac{30+10 \times 3}{\sqrt{3}}\right)$$

$$= \frac{60}{\sqrt{3}}$$

$$= 20\sqrt{3} \text{ m}$$

In $\triangle ADE$, $\cos \theta = \frac{AD}{AE}$

$$\cos 30^\circ = \frac{30}{AE}$$

$$\frac{\sqrt{3}}{2} = \frac{30}{AE}$$

$$AE = \frac{60}{\sqrt{3}} = 20\sqrt{3} \text{ m}$$

Distance between the top of the lighthouse to the top of the tower = AE = $20\sqrt{3} \text{ m}$

Angle of depression = $\angle DAF = \angle AFB = \theta$

In $\triangle ABF$, $\tan \theta = \frac{AB}{BF}$

$$\tan \theta = \frac{10\sqrt{3}}{10}$$

$$\tan \theta = \sqrt{3}$$

$$\tan \theta = \tan 60^\circ$$

∴ Angle of depression = $\theta = 60^\circ$

CHAPTER 10: CIRCLES

I. Multiple choice Questions :

- 1) D) MN
- 2) D) AB
- 3) A) P
- 4) C) 8cm
- 5) C) 90°
- 6) A) 7cm
- 7) B)) Secant
- 8) A) tangent
- 9) B) 100°
- 10) D) 4cm

- 11) B) 50°
- 12) B) 3cm
- 13) A) 25°
- 14) D) 65°
- 15) D) 40°
- 16) B) 5cm
- 17) B) 13cm
- 18) A) 7cm
- 19) B) 70°

II. ONE MARK QUESTIONS:

- 20) The line that intersects circle at only one point is a Tangent.
- 21) A line intersecting a circle in 2 points is a secant.
- 22) 90°
- 23) 2
- 24) One
- 25) $\angle BOC + \angle BAC = 180^{\circ}$

$$130^{\circ} + \angle BAC = 180^{\circ}$$

$$\angle BAC = 180^{\circ} - 130^{\circ}$$

$$\angle BAC = 50^{\circ}$$

- 26) In $\triangle OAP$

$$\angle OPA + \angle OAP + \angle AOP = 180^{\circ}$$

$$40^{\circ} + 90^{\circ} + \angle AOP = 180^{\circ}$$

$$130^{\circ} + \angle AOP = 180^{\circ}$$

$$\angle AOP = 180^{\circ} - 130^{\circ}$$

$$\angle AOP = 50^{\circ}$$

III. TWO MARKS QUESTIONS:

- 27) In $\triangle OAP$, $\angle AOP = 90^{\circ}$ [$\because OA \perp AP$]
 $\angle AOP = 180^{\circ} - (90^{\circ} + 40)$

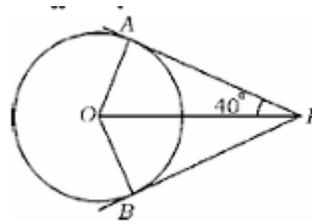
$$= 180^\circ - 130^\circ$$

$$\angle AOP = 50^\circ$$

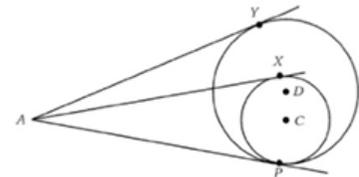
$$\angle AOP = \angle BOP = 50^\circ$$

$$\angle AOB = 50^\circ + 50^\circ = 100^\circ$$

$$AP = PB \text{ (by theorem) } \therefore PB = 4\text{cm}$$



- 28) In a circle with center 'D' $AY = AP$ -----(1)
 (\because Tangents drawn from an external point to a circle are equal)
 In a circle with center 'C' $AX = AP$ -----(2)
 From (1) and (2)
 $AY = AX$

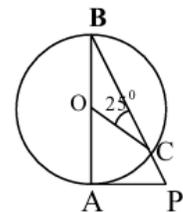


- 29) According to Pythagoras theorem, $OA^2 = AB^2 + OB^2$
 $5^2 = AB^2 + 3^2$
 $OA^2 = AB^2 + 9^2$
 $AB^2 = 25 - 9$
 $AB^2 = 16$
 $AB = 4\text{cm}$



\therefore Length of the chord $= AC = 8\text{cm}$

- 30) $\angle OCD = 25^\circ$
 $OB = OC$ (\because Radii of same circle)
 $\angle OBC = \angle OCD = 25^\circ$ (\because $\triangle OBC$ is an Isosceles triangle)
 $\angle PAB = 90^\circ$ (\because Tangents at any point of a circle is perpendicular to the radius through the point of contact)
 In $\triangle PAB$, $\angle APB + \angle ABP + \angle PAB = 180^\circ$
 $\angle APB + 25^\circ + 90^\circ = 180^\circ$
 $\angle APB = 180^\circ - 115^\circ$
 $\angle APB = 65^\circ$



IV. THREE MARKS QUESTIONS:

- 31) Data : A circle with center O and tangent XY at a point P.
 To Prove : $OP \perp XY$

Construction : Take any point Q other than P on the tangent XY, and join OQ

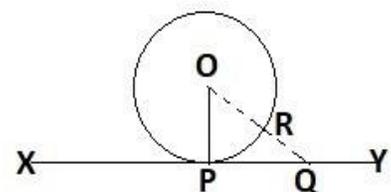
Proof : Hence Q is a point on the tangent XY, other than the point of contact P. So Q lies outside the circle.

Let OQ intersect the circle at R

$$\therefore OP = OR \text{ [Radii of same circle]}$$

$$\text{Now } OQ = OR + RQ$$

$$\Rightarrow OQ > OR$$



$$\Rightarrow OQ > OP \text{ [}\because OP = OR\text{]}$$

Therefore OP is the shortest distance to the tangent from the center O, \therefore
 $OP \perp XY$ [\because Perpendicular distance is always the shortest distance]

- 32)** Given : PQ and PR are the two tangents drawn from the external point P to a circle of center O.
 To Prove : $PQ = PR$

Construction : Join OP, OQ, OR

Proof : In $\triangle OQP$ and $\triangle ORP$

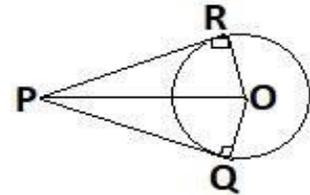
$$OQ = OR \quad (\because \text{Radii of same circles})$$

$$OP = OP \quad (\because \text{Common side})$$

$$\angle OQP = \angle ORP = 90^\circ$$

$$\therefore \triangle OQP \cong \triangle ORP$$

$$\therefore PQ = PR$$



- 33)** Join OT, let it intersect PQ at the point R.

Then $\triangle TPQ$ is isosceles and TO is the angle bisector of $\angle PTQ$

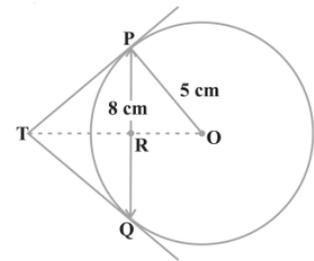
Therefore $OT \perp PQ$ and OT bisects PQ

$$\Rightarrow PR = RQ = 4\text{cm}$$

$$RO = \sqrt{5^2 - 4^2}$$

$$RO = \sqrt{25 - 16}$$

$$RO = \sqrt{9} = RO = 3\text{cm}$$



$$\angle OPR + \angle TPR = 90^\circ \text{ ----- (1)}$$

$$\angle PTR + \angle TPR = 90^\circ \text{ ----- (2)}$$

From (1) and (2)

$$\angle OPR = \angle PTR \text{ -----(3)}$$

$\triangle PRO$ and $\triangle PTR$ right angled triangles are similar [AA similarity criteria]

$$\Rightarrow \frac{PT}{OP} = \frac{PR}{OR} = \frac{PT}{5} = \frac{4}{3}$$

$$PT = \frac{4 \times 5}{3} = \frac{20}{3}$$

- 34)** Data : TP and TQ are two tangents drawn from an external point T to the circle with center O.

To Prove : $\angle PTQ = 2 \angle OPQ$

$$\text{Let } \angle PTQ = \theta \text{ -----(1)}$$

$$TP = TQ$$

Therefore TPQ is an Isosceles triangle.

$$\angle TPQ = \angle TQP = \frac{1}{2} [180 - \theta]$$

$$\Rightarrow \angle TPQ = \angle TQP = 90^\circ - \frac{1}{2} \theta \text{ -----(2)}$$

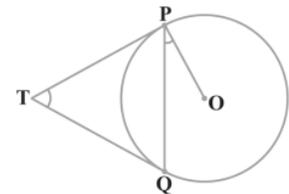
$$\angle OPT = 90^\circ \text{ -----(3)}$$

$$\angle OPT = \angle OPT - \angle TPQ$$

$$\Rightarrow \angle OPQ = 90^\circ - (90^\circ - \frac{1}{2} \theta)$$

$$\Rightarrow \angle OPQ = \frac{1}{2} \theta$$

$$\Rightarrow \angle PTQ = 2 \angle OPQ \text{ [} \because \text{ (2) and (3)]}$$



35) Proof : Let the tangent AB touch the circle at C, join OC

In $\triangle OXA$ and $\triangle OCA$

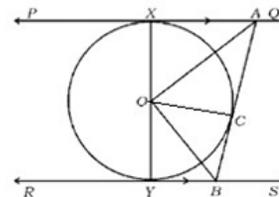
$AX = AC$ (\because Tangents)

$OX = OC$ (\because Radii)

$OA = OA$ (\because common sides)

$\therefore \triangle OXA \cong \triangle OCA$ (\because SSS Postulate)

$$\angle XOA = \angle COA \text{ -----(1)}$$



Similarly, $\triangle OCB \cong \triangle OYB$ (\because SSS Postulate)

$\angle COB = \angle YOYB$ -----(2)

$\angle XOA + \angle COA + \angle COB + \angle YOYB = 180^0$ -----(3) (\because XY is a straight line)

From (1) and (2) ,

$$2 \angle AOC + 2 \angle COB = 180^0$$

$$\angle AOC + \angle COB = 90^0$$

$$\angle AOB = 90^0$$

Unit : 11 Area Related to Circles

I. Multiple Choice Questions :

1. A) 7π units
2. A) $2\pi r^2$
3. C) $\frac{\theta}{180} \times \pi r$
4. C) $\frac{\pi r^2}{4} \text{cm}^2$
5. C) $\frac{3\pi r^2}{4} \text{cm}^2$
6. D) 88cm
7. B) 80^0
8. C) Area of Sector – Area of $\triangle AOB$
9. C) 66cm
10. C) 44 cm^2
11. A) $\frac{(360-30)\pi r^2}{360} \text{cm}^2$
12. C) $\frac{\pi r}{2} \text{ cm}$

II. One Marks Questions : -

13. $\frac{\theta}{360} \times \pi r^2$
14. $\frac{\theta}{360} \times 2\pi r$
15. 45^0
16. 11cm
17. 11cm
18. 7cm
19. 3.5cm
20. Radius $r = 2$ units

III. Two Marks Questions :-

$$\begin{aligned} 21. \text{ Length of the Arc} &= \frac{\theta}{360} \times 2\pi r \\ &= \frac{60}{360} \times 2 \times \frac{22}{7} \times 21 \\ &= \frac{1}{3} \times \frac{22}{7} \times 21 \\ \text{Length of the Arc} &= 22\text{cm} \end{aligned}$$

$$\begin{aligned} 22. \text{ Area of Sector} &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{45}{360} \times \frac{22}{7} \times 4^2 \\ &= \frac{1}{8} \times \frac{22}{7} \times 16 \\ \text{Area of Sector} &= 6.28 \text{ cm}^2. \end{aligned}$$

$$\begin{aligned} 23. \text{ Area of big Circle} &= (92 + 62) \text{ Sq.cm} \\ \pi r^2 &= 154 \\ r^2 &= 154 \times \frac{7}{22} = 49 \\ r^2 &= 49 \\ \text{Radius } r &= 7\text{cm}. \end{aligned}$$

$$\begin{aligned} 24. \text{ Area swept by the minute hand of the clock} &= \text{Area of sector} \\ &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{60}{360} \times \frac{22}{7} \times 14^2 \\ &= \frac{1}{8} \times \frac{22}{7} \times 16 \\ &= \frac{22 \times 14}{3} = \frac{308}{3} \text{ cm}^2. \end{aligned}$$

$$\begin{aligned} 25. \text{ Area of Quadrant of Circle} &= \frac{\pi r^2}{4} = \frac{3.14 \times 20 \times 20}{4} = 3.14 \times 5 \times 20 = 3.14 \times 100 = 314 \text{ cm}^2. \\ \text{Perimeter of Quadrant of Circle} &= \frac{\pi r}{2} + 2r = \frac{3.14 \times 20}{2} + 2 \times 20 = 31.4 + 40 = 71.4\text{cm} \end{aligned}$$

IV. Three Marks Questions :-

$$\begin{aligned} 26. \text{ Area of Cloth required to make hand fan} &= \text{Area of Sector} \\ &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{120}{360} \times \frac{22}{7} \times 21 \times 21 \\ &= 22 \times 21 \\ \text{Area of Cloth required to make hand fan} &= 462\text{cm}^2. \\ \text{Total length of the wire} &= \text{Length of Arc} + 2 \text{ Radius} \\ &= \frac{\theta}{360} \times 2\pi r + 2r \\ &= \frac{120}{360} \times 2 \times \frac{22}{7} \times 21 + 2 \times 21 \\ &= 44 + 42 \\ \text{Total length of the wire} &= 86\text{cm} \end{aligned}$$

$$\begin{aligned}
 27. \text{ i) Length of Arc} &= \frac{\theta}{360} \times 2\pi r \\
 &= \frac{60}{360} \times 2 \times \frac{22}{7} \times 21 \\
 &= \frac{1}{6} \times 2 \times 22 \times 3 \\
 &= 22 \text{ cm}
 \end{aligned}$$

$$\begin{aligned}
 \text{ii) Area of Sector} &= \frac{\theta}{360} \times \pi r^2 \\
 &= \frac{60}{360} \times \frac{22}{7} \times 21 \times 21 \\
 &= \frac{1}{6} \times 22 \times 3 \times 21 \\
 &= 231 \text{ cm}^2.
 \end{aligned}$$

28. Area of Segment = Area of Sector – Area of Equilateral Triangle

$$\begin{aligned}
 &= \frac{\theta}{360} \times \pi r^2 - \frac{\sqrt{3}}{4} a^2 \\
 &= \frac{60}{360} \times \frac{22}{7} \times 21 \times 21 - \frac{1.73}{4} \times 21 \times 21 \\
 &= \frac{1}{6} \times 22 \times 3 \times 21 - \frac{762.93}{4} \\
 &= 231 - 190.7325 \\
 &= 40.2675 \text{ cm}^2.
 \end{aligned}$$

29. Area of remaining part of Circle = Area of Semicircle – Area of Triangle

$$\begin{aligned}
 &= \frac{\pi r^2}{2} - \frac{1}{2} \times \text{base} \times \text{height} \quad \text{Height} = \sqrt{100 - 36} = \sqrt{64} = 8 \text{ cm} \\
 &= \frac{22 \times 5 \times 5}{2 \times 7} - \frac{1}{2} \times 6 \times 8 \\
 &= \frac{11 \times 25}{7} - 24 \\
 &= 39.28 - 24
 \end{aligned}$$

Area of remaining part of Circle = 15.28 cm².

30. Area of Sector : Area of Circle = 1:5

$$\begin{aligned}
 (\theta/360^\circ) \pi r^2 / \pi r^2 &= 1/5 \\
 \theta &= 360^\circ / 5 \\
 \theta &= 72^\circ
 \end{aligned}$$

$$\begin{aligned}
 \text{Length of Arc} &= (\theta/360^\circ) 2\pi r \\
 &= (72^\circ / 360^\circ) \times 2 \times 22/7 \times 7 \\
 &= (1/5) \times 44 \\
 &= 44/5 \text{ cm}
 \end{aligned}$$

31. Area of Sector = 231

$$\begin{aligned}
 (\theta/360^\circ) \pi r^2 &= 231 \\
 (\theta/360^\circ) &= 231/\pi r^2 \dots\dots(1)
 \end{aligned}$$

Length of Arc = 22

$$(\theta/360^\circ) 2\pi r = 22$$

$$(\theta/360^\circ) = 22/2\pi r \dots\dots(2)$$

From (1) & (2)

$$231/\pi r^2 = 22/2\pi r$$

$$231/22 = \pi r^2 / 2\pi r$$

$$r = 21 \text{ cm}$$

$$(\theta/360^\circ) 2\pi r = 22$$

$$(\theta/360^\circ) = 22/2\pi r$$

$$\theta = 22 \times 360^\circ / 2 \times 22/7 \times 21$$

$$\theta = 60^\circ$$

32. Length of Arc = 22cm

$$(\theta/360^\circ) 2\pi r = 22$$

$$(60^\circ/360^\circ) \times 2 \times 22/7 \times r = 22$$

$$(1/6) \times 2 \times 22/7 \times r = 22$$

$$r = 22 \times 7 \times 6 / 2 \times 22$$

$$r = 21 \text{ cm}$$

$$\text{Area of Sector} = (\theta/360^\circ) \pi r^2$$

$$= (60^\circ/360^\circ) \times 22/7 \times 21 \times 21$$

$$= 11 \times 21$$

$$= 231 \text{ cm}^2$$

33. Area of Sector = Length of Arc

$$(\theta/360^\circ) \pi r^2 = (\theta/360^\circ) 2\pi r$$

$$\pi r^2 = 2\pi r$$

$$r = 2$$

Length of Arc = 44/21

$$(\theta/360^\circ) 2\pi r = 44/21$$

$$(\theta/360^\circ) \times 2 \times 22/7 \times 2 = 44/21$$

$$\theta = 44 \times 360 \times 7 / 21 \times 22 \times 2 \times 2$$

$$\theta = 60^\circ$$

34. Area of Sector = 462 cm²

$$(\theta/360^\circ) \pi r^2 = 462$$

$$(120^\circ/360^\circ) \times \pi r^2 = 462$$

$$(1/3) \times 22/7 \times r^2 = 462$$

$$r^2 = 462 \times 3 \times 7 / 22$$

$$r^2 = 21 \times 21$$

$$r = 21 \text{ cm}$$

$$\text{Length of Arc} = (\theta/360^\circ) 2\pi r$$

$$= (120^\circ/360^\circ) \times 2 \times 22/7 \times 21$$

$$= 44 \text{ cm}$$

35. Length of Arc = 11 cm

$$11 = \frac{\theta}{360} \times 2\pi r$$

$$11 = \frac{30}{360} \times 2 \times \frac{22}{7} \times r$$

$$11 \times 12 \times 7 = 2 \times 22 \times r$$

$$r = \frac{11 \times 12}{2 \times 22}$$

$$r = 21 \text{ cm}$$

$$\begin{aligned} \text{Area of Sector OAXB} = A1 &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{30}{360} \times \frac{22}{7} \times 21 \times 21 \end{aligned}$$

$$A1 = \frac{231}{2} \text{ cm}^2.$$

$$\begin{aligned} \text{Area of Sector OCYD} = A2 &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{30}{360} \times \frac{22}{7} \times 7 \times 7 \end{aligned}$$

$$A2 = \frac{77}{6} \text{ cm}^2.$$

$$\begin{aligned} \text{Area of Shaded region} &= A1 - A2 \\ &= \frac{231}{2} - \frac{77}{6} \\ &= \frac{693 - 77}{6} \\ &= \frac{606}{6} \\ &= \frac{308}{3} \\ &= 102.66 \text{ cm}^2. \end{aligned}$$

36. ABC is an equilateral Triangle, therefore $\theta = 60^\circ$ $r = 3.5 \text{ cm}$

$$\text{Length of Arc PQ} = \frac{\theta}{360} \times 2\pi r = \frac{60}{360} \times 2 \times \frac{22}{7} \times \frac{7}{2} = \frac{11}{3} \text{ cm}$$

$$\text{PQ} = \text{RS} = \text{UT}$$

$$\therefore \text{Length of Arc RS} = \frac{11}{3} \text{ cm}$$

$$\begin{aligned} \text{Area of Equilateral Triangle} &= \frac{\sqrt{3}a^2}{4} \\ &= \frac{\sqrt{3}a^2}{4} = 49\sqrt{3} \\ a^2 &= 49 \times 4 \end{aligned}$$

$$\therefore a = 14 \text{ cm}$$

$$\text{AB} = \text{AC} = \text{BC} = 14 \text{ cm}$$

$$\begin{aligned} \text{Length of QR} &= \text{AC} - \text{AQ} - \text{CR} \\ &= 14 - 3.5 - 3.5 \\ &= 7 \text{ cm} \end{aligned}$$

$$\text{QR} = \text{TS} = \text{PU} = 7 \text{ cm}$$

$$\begin{aligned} \text{Perimeter of PQRSTUP} &= \text{PQ} + \text{RS} + \text{UT} + \text{QR} + \text{TS} + \text{PU} \\ &= \frac{11}{3} + \frac{11}{3} + \frac{11}{3} + 7 + 7 + 7 \\ &= \frac{33}{3} + 21 \\ &= 11 + 21 \end{aligned}$$

$$\text{Perimeter of PQRSTUP} = 32 \text{ cm}$$

$$37. \text{ Length of Arc} = \frac{\theta}{360} \times 2\pi r$$

$$\frac{22}{3} = \frac{\theta}{360} \times 2 \times \frac{22}{7} \times 7$$

$$\frac{1}{3} = \frac{\theta}{360} \times 2$$

$$\theta = \frac{180}{3}$$

$$\theta = 60^\circ$$

$$\text{Area of Circle} = A_1 = \pi r^2 = \frac{22}{7} \times 7 \times 7 = 22 \times 7 = 154 \text{ cm}^2.$$

$$\text{Area of Sector} = A_2 = \frac{\theta}{360} \times \pi r^2 = \frac{60}{360} \times \frac{22}{7} \times 7 \times 7 = \frac{1}{6} \times 22 \times 7 = 25.66 \text{ cm}^2.$$

$$\begin{aligned} \text{Required Area} &= A_1 - A_2 \\ &= 154 - 25.66 \\ &= 128.34 \text{ cm}^2. \end{aligned}$$

$$38. \text{ Area of semicircle } \pi r = 44$$

$$r = 44 \times \frac{7}{22} = 14 \text{ cm}$$

$$\angle OPQ = 180 - 90 = 90^\circ$$

$$\text{Area of Sector OPRQ} = \frac{\theta}{360} \times \pi r^2 = \frac{90}{360} \times \frac{22}{7} \times 14 \times 14 = \frac{1}{4} \times \frac{22}{7} \times 196$$

$$= \frac{1}{4} \times 22 \times 28$$

$$= 22 \times 7$$

$$= 154 \text{ cm}^2.$$

$$\text{Area of } \triangle OPQ = \frac{1}{2} \times \text{base} \times \text{height} = \frac{1}{2} \times 14 \times 14 = \frac{1}{2} \times 196 = 98 \text{ cm}^2.$$

$$\text{Area of Sector} = \text{Area of OPRQ} - \text{Area of } \triangle OPQ$$

$$= 154 - 98$$

$$= 56 \text{ cm}^2.$$

Unit : 12 SURFACE AREA & VOLUME

I. Multiple choice questions

1. B) $6a^2$
2. D) $4a^2$
3. C) a^3
4. A) $2(lb+bh+hl)^2$
5. B) $2h(1+b)$
6. B) $l \times b \times h$
7. D) $2\pi rh$
8. A) $2\pi(r+h)$
9. C) $\pi r^2 h$
10. A) πrl
11. B) $\pi r(r+1)$
12. C) $\frac{1}{3} \pi r^2 h$
13. D) $4\pi r^2$
14. D) $\frac{4}{3} \pi r^3$
15. C) 3 : 1

16. D) 20cm^3
17. B) 6cm
18. C) 216cm^3
19. D) 30cm^3
20. B) 10cm
21. D) $60,000 \text{ ltr}$
22. C) 220cm^3
23. A) 120 cm^3
24. C) 616 cm^3
25. D) 125 cm^3

II. One-mark questions

26. $A = 3\pi r^2$

27. $A = 2\pi r^2$

28. $V = \frac{2}{3}\pi r^3$

29. $V = \frac{4}{3}\pi r^3$

30. 2:1

31. 4:1

32. $30\text{cm}^3 \times 3 = 90\text{cm}^3$

33. $A = 2\pi rh = 25 \times 10 = 250 \text{ cm}^2$

34. $\text{TSA} = \pi rl + 2\pi r^2$

35. $V = \pi r^2 h - \frac{4}{3}\pi r^3$

36. $V = \pi r^2 h$

$$500 = \frac{22}{7} \times r^2 \times 10$$

$$r^2 = \frac{500 \times 7}{22 \times 10}$$

$$\frac{350}{22} = r^2$$

$$r = 3.9\text{cm}$$

37.

$$\frac{v_1}{v_2} = \frac{\pi r_1^2 h_1}{\pi r_1^2 h_2}$$

$$\frac{v_1}{v_2} = \frac{9^2}{1^2} = \frac{1}{9}$$

$$\frac{v_1}{v_2} = \frac{81}{9}$$

$$\frac{v_1}{v_2} = \frac{9}{1}$$

$$v_1 : v_2 = 9 : 1$$

38. 616cm^2

III. Two-mark questions

39. $h=20\text{cm}$ $r=6\text{cm}$

CSA of cylinder = $2\pi rh$

$$A = 2 \times \frac{22}{7} \times 6 \times 20$$

$$A = \frac{5280}{7}$$

$$A = 754.2857\text{cm}^2$$

40. length of the edge of a cube is = 3cm

Length of a cuboid = $3+3 = 6\text{cm}$

$l=6\text{cm}$, $b=3\text{cm}$, $h=3\text{cm}$

$$\begin{aligned} \text{TSA} &= 2[lb+bh+hl] \\ &= 2[6 \times 3 + 3 \times 3 + 3 \times 6] \\ &= 2 \times 45 \end{aligned}$$

$$\text{TSA} = 90\text{ cm}^2$$

41. Volume of toy = Volume of Hemisphere + Volume of cone

$$V = \frac{2}{3} \pi r^3 + \frac{1}{3} \pi r^2 h$$

$$V = \frac{1}{3} \times \frac{22}{7} \times 7 \times 7 [2 \times 7 + 4]$$

$$V = \frac{2772}{3}$$

$$V = 924\text{cm}^3$$

42. TS of a toy = CSA of cylinder + TSA of sphere

$$A = 2\pi rh + 4\pi r^2$$

$$A = 2\pi r(h + 2r)$$

$$A = 2 \times \frac{22}{7} \times 7(10 + 2 \times 7)$$

$$A = 44 \times 24$$

$$A = 1056 \text{ cm}^2$$

43. $a^3 = 125$ $a = 5 \text{ cm}$

CSA of the cube = $4a^2$

$$A = 4 \times 5^2$$

$$A = 4 \times 25$$

$$A = 100 \text{ cm}^2$$

44.

$$V = \frac{4}{3}\pi r^3$$

$$38808 = \frac{4}{3} \left(\frac{22}{7}\right) r^3$$

$$r^3 = \frac{814968}{88}$$

$$r = 21$$

$$A = 4\pi r^2$$

$$A = 4 \left(\frac{22}{7}\right) 21^2$$

$$A = 5544 \text{ cm}^2$$

IV. Three Marks Questions

45. Height of the cone $h = 14 - 6 = 8 \text{ cm}$

$$r = 6 \text{ cm}$$

$$\text{Slope of the cone } l^2 = r^2 + h^2$$

$$l^2 = 6^2 + 8^2$$

$$l^2 = 10^2$$

$$l = 10 \text{ cm}$$

Surface area of the toy = CSA of cone + CSA of hemisphere

$$A = \pi r l + 2\pi r^2$$

$$A = \pi r (l + 2r)$$

$$A = \frac{22}{7} (6) (10 + 2 \times 6)$$

$$A = \frac{22}{7} (6) (22)$$

$$A = 13684 / 7$$

$$A = 1954.85 \text{ cm}^2$$

46. Surface area of toy = CSA Of cylinder + CSA of hemisphere + area of circle

$$A = 2\pi rh + 2\pi r^2 + \pi r^2$$

$$A = 2\pi r (h + 2r + r)$$

$$A = 2 \left(\frac{22}{7}\right) (3.5)(10 + 3 \times 3.5)$$

$$A = 3157 / 7$$

$$A = 451 \text{ cm}^2$$

47. $d = 6 \text{ cm}$ $r = 3 \text{ cm}$ $h = 12 \text{ cm}$

Real capacity of the glass = volume of cylinder – volume of hemisphere

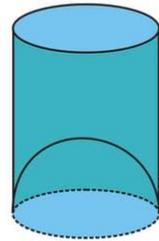
$$V = \pi r^2 h - \frac{2}{3} \pi r^3$$

$$V = \pi r^2 \left(h - \frac{2}{3} r\right)$$

$$V = \frac{22}{7} \times 3 \times 3 \left(12 - \frac{2}{3} \times 3\right)$$

$$V = \frac{1980}{7}$$

$$V = 282.857 \text{ cm}^3$$



48. $d = 126 \text{ m}$ $r = 63 \text{ m}$ $h = 5 \text{ m}$

height of the cone $h = 21 - 5 = 16 \text{ m}$

$$l^2 = r^2 + h^2$$

$$l^2 = 63^2 + 16^2$$

$$l^2 = 65^2$$

$$l = 65 \text{ m}$$

Area of the canvas cloth = CSA of cylinder + CSA of cone

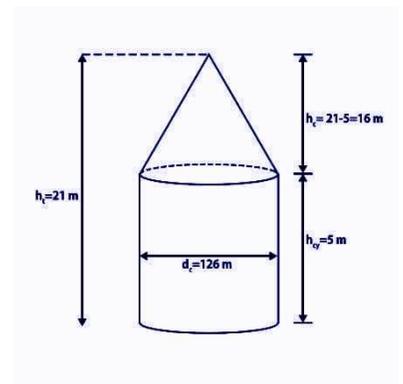
$$A = 2\pi rh + \pi rl$$

$$A = 2\pi r(2h + l)$$

$$A = \frac{22}{7} \times 63(2 \times 5 + 65)$$

$$A = 14850 \text{ m}^2$$

Area of the canvas cloth = 14850 m^2



V. Four Marks Questions

49. Transforming the petrol per minute = 742.5 lit

In one hour = 742.5 x 60 = 44550 lit

Capacity of the tank = 44550 lit

Volume of tank = volume of cylinder + volume of 2 hemisphere

$$V = \pi r^2 h + 2x \frac{2}{3} \pi r^3$$

$$V = \pi r^2 \left(h + \frac{4}{3} x \frac{3}{2} \right)$$

$$44550 = \frac{22}{7} x \frac{3}{2} x \frac{3}{2} \left(h + \frac{4}{3} x \frac{3}{2} \right)$$

$$6.3 = h + 2$$

$$h = 6.3 - 2 = 4.3 \text{ m}$$

Length of the tank = 4.3 m

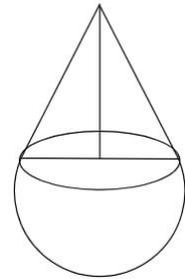
50. VOLUME = $\frac{2}{3}\pi r^3$

$$539/6 = \frac{2}{3} \left(\frac{22}{7} \right) r^3$$

$$r^3 = 1/8$$

$$r = 1/2 \text{ cm}$$

$$\begin{aligned} \text{SURFACE AREA OF THE TOY} &= 2\pi r^2 + \pi r l \\ &= \pi r(2r + l) \\ &= \frac{22}{7} \times \frac{1}{2} (2 \times \frac{1}{2} + 12.5) \\ \mathbf{A} &= \mathbf{21.21 \text{ cm}^2} \end{aligned}$$



51. $r_s = \frac{8.5}{2} = 4.25 \text{ cm}$

$r_c = 1 \text{ cm}$

Volume of water = volume of cylinder + Volume of sphere

$$V = \pi r_c^2 h + \frac{4}{3} \pi r_s^3$$

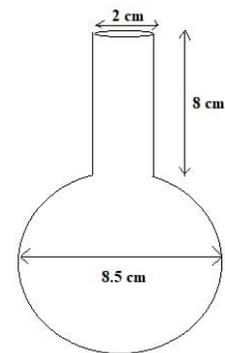
$$V = \pi \left(r_c^2 h + \frac{4}{3} r_s^3 \right)$$

$$V = 3.14 \left(1^2 \times 8 + \frac{4}{3} (4.25)^3 \right)$$

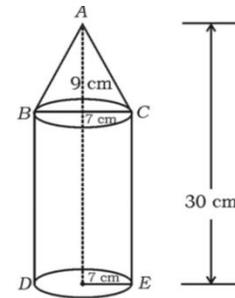
$$V = 3.14 \left(\frac{24 + 307.08}{3} \right)$$

$$V = \frac{1039.59}{3}$$

$$V = 346.53 \text{ cm}^3$$



52. $r = 7\text{cm}$ $h_1 = 21\text{ cm for cylinder}$
 $h_2 = 9\text{cm for cone}$
 volume of solid = volume of cylinder + volume of cone
 $= \pi r^2 h_1 + \frac{1}{3} \pi r^2 h_2$
 $= \pi r^2 (h_1 + \frac{1}{3} h_2)$
 $= \frac{22}{7} \times 7 \times 7 (21 + \frac{1}{3} \times 9)$
 $= 22 \times 7 \times 24$
 $V = 3696 \text{ c.c.}$

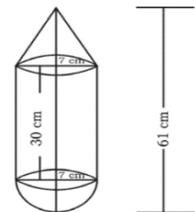


53. Height of the cone = $61 - (30+7)$
 $= 61 - 37 = 24 \text{ cm}$

But 7,24,25 are pythagorian triplets

Slant height of the cone = $l = 25 \text{ cm}$

TSA of the solid = LSA of the cone + LSA of the cylinder + LSA of the hemisphere
 $= \pi r l + 2\pi r h + 2\pi r^2$
 $= \pi r (l + 2h + 2r)$
 $= \frac{22}{7} \times 7 (25 + 2 \times 30 + 2 \times 7)$
 $= 22 \times 99$
 $= 2178 \text{ cm}^2$



Cost of painting at the rate of Rs. 10 per 100 cm^2 is = $\frac{2178 \times 10}{100} = 217.8 \text{ rupees}$

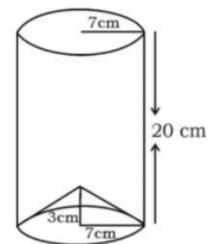
54. Volume of the vessel equal to volume of the cylinder – volume of cone

Volume of the cylinder = $\pi r^2 h$
 $= \frac{22}{7} \times 7 \times 7 \times 20$
 $V_1 = 3080 \text{ cm}^3$

Volume of the cone = $\frac{1}{3} \pi r^2 h$
 $= \frac{1}{3} \times \frac{22}{7} \times 7 \times 7 \times 3$
 $V_2 = 154 \text{ cm}^3$

Volume of vessel = $V_1 - V_2 = 3080 - 154 = 2926 \text{ cm}^3$

$\frac{2926}{1000} = 2.926 \text{ lit}$



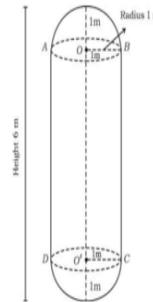
OR

Cost of the milk to fill this vessel at the rate of Rs. 20 per lit.

$= 2.926 \times 20 = \text{Rs. } 58.20$

55. Radius of hemisphere $r = 1\text{m}$
 Radius of cylinder $r = 1\text{m}$
 Height of cylinder $h = 4\text{m}$
 Volume of solid = Volume of cylinder + 2 (volume of hemisphere)

$$\begin{aligned}
 &= \pi r^2 h + 2 \left(\frac{2}{3} \pi r^3 \right) \\
 &= \pi r^2 \left(h + \frac{4}{3} r \right) \\
 &= \frac{22}{7} \times 1 \times 1 \left(4 + \frac{4}{3} \times 1 \right) \\
 &= \frac{22}{7} \times \frac{16}{3} \text{m}^3 \\
 &= \frac{352}{21} \times (100)^3 \text{cm}^3 \\
 &= \frac{352000}{21}
 \end{aligned}$$



Capacity of milk tank = 16761.9 litres.

56. Diameter of hemisphere = 5mm

Radius = 2.5 mm
 Length of entire capsule = 14 mm
 Height of cylinder $h = 14 - 5 = 9\text{mm}$

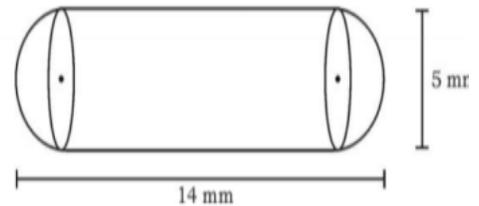
Surface area of capsule = $2\pi rh + 4r^2$

$$= 2\pi r (h + 2r)$$

$$= 2 \times \frac{22}{7} \times 2.5 (9 + 2 \times 2.5)$$

$$= 88 \times 2.5$$

$$\text{Surface area of capsule} = 220 \text{mm}^2$$



57. Height of cone $h_c = 23 - 11 = 12 \text{cm}$

Radius of cone $r = 5\text{cm}$

Slant height of cone $l^2 = r^2 + h^2$
 $l^2 = 5^2 + 12^2$
 $l^2 = 169$
 $l = 13 \text{cm}$

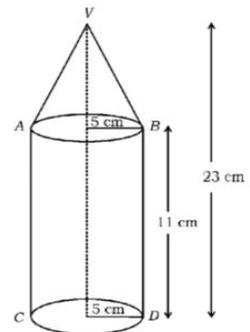
CAS of given solid = CSA of cone + CSA of cylinder

$$= \pi r l + 2\pi r h$$

$$= \pi r (l + 2h)$$

$$= \frac{22}{7} \times 5 (13 + 2 \times 11)$$

$$= 550 \text{cm}^2$$



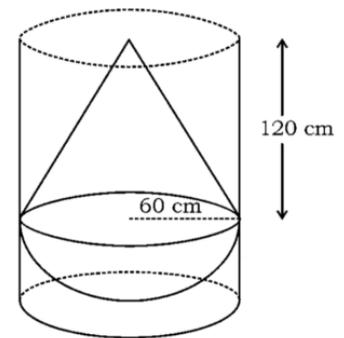
Volume of given = volume of cone + volume of cylinder

$$\begin{aligned}
 &= \frac{1}{3} \pi r^2 h_c + \pi r^2 h_{cy} \\
 &= \pi r^2 \left(\frac{1}{3} x h_c + h_{cy} \right) \\
 &= \frac{22}{7} \times 5 \times 5 \left(\frac{1}{3} \times 12 + 11 \right) \\
 &= \frac{8250}{7} \\
 &= 1178.57 \text{ cm}^3
 \end{aligned}$$

58. Volume of cylinder = $\pi r^2 h$
 $= (60 \times 60) \times 180$
 $= 648000 \pi \text{ cm}^3$

Volume of solid = Volume of cone + Volume of hemisphere

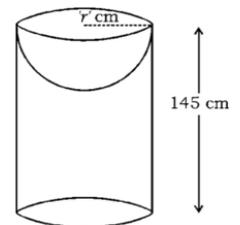
$$\begin{aligned}
 &= \frac{1}{3} \pi r^2 h + \frac{2}{3} \pi r^3 \\
 &= \frac{1}{3} \pi r^2 (h + 2r) \\
 &= \frac{1}{3} \times \pi \times 60 + 60 [120 + 6(60)] \\
 &V = 288000 \pi \text{ cm}^3
 \end{aligned}$$



Volume of water left in the cylinder = Volume of cylinder – Volume of solid
 $= 64800 \pi - 28800 \pi$
 $= 360000 \pi \text{ cm}^3$

59. Volume of the hemisphere = $\frac{2}{3} \pi r^3$
 $18000 \pi = \frac{2}{3} \times \pi \times r^3$
 $r^3 = \frac{18000 \times 3}{2}$
 $r^3 = 27000$
 $r = 30 \text{ cm}$

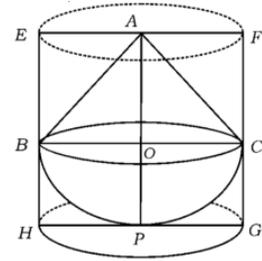
TSA of solid = CSA of Hemisphere + CSA of cylinder + Area of circular base
 $= 2 \pi r^2 + 2 \pi r h + \pi r^2$
 $= \pi r (2r + 2h + r)$
 $= \frac{3}{2} \times 30 (2 \times 30 + 2 \times 145 + 30)$
 $= \frac{250800}{7} \text{ cm}^2$
 $= 35828.5 \text{ cm}^2$



60. Base radius of cone = $BO = \frac{1}{2} \times 4 = 2 \text{ cm}$
 Radius of hemisphere = $BO = r = 2 \text{ cm}$

Volume of the toy = Volume of hemisphere + Volume of cone

$$\begin{aligned}
 &= \frac{2}{3} \pi r^3 + \frac{1}{3} \pi r^2 h \\
 &= \frac{2}{3} \times 3.14 \times 2^3 + \frac{1}{3} \times 3.14 \times 2^2 \times 2 \\
 &= 25.12 \text{ cm}^3
 \end{aligned}$$



EFGH is right circular cylinder

Radius of EFGH = HP = BO = r = 2m

Height of EFGH = EH = h

$$EH = 4\text{m}$$

Volume required = Volume of right circular cylinder – volume of the toy

$$\begin{aligned}
 &= \pi r^2 h - 25.12 \\
 &= 3.14 \times 2^2 \times 4 - 25.12 \\
 &= 25.12 \text{ cm}^3
 \end{aligned}$$

61. Height of cylinder = h = Height of cone = 2.4 m

Diameter of cylinder = d = 1.4 m

Radius of cylinder = $\frac{1.4}{2} = 0.7$ m

Slant height of cone

$$\begin{aligned}
 l^2 &= h^2 + r^2 \\
 l^2 &= 2.4^2 + 0.7^2 \\
 l &= 2.5 \text{ m}
 \end{aligned}$$

Radius of cone = r = 0.7 m

TSA of the remaining solid

$$\begin{aligned}
 &= \text{CSA of cylinder} + \text{CSA of cone} + \text{base area of cylinder} \\
 &= 2\pi r h + \pi r l + \pi r^2 \\
 &= \pi r (2h + l + r) \\
 &= \frac{22}{7} \times 0.7 (2 \times 2.4 + 2.5 + 0.7) \\
 &= 2.2 \times 8 \\
 &= 17.6 \text{ m}^2
 \end{aligned}$$

VI. Five Marks Questions

62. Surface area of the toy = CSA of toy + CSA of hemisphere + CSA of cone

$$A = 2\pi r h + 2\pi r^2 + \pi r l$$

$$A = \pi r (2h + 2r + l)$$

$$A = \frac{22}{7} \times 5 (2 \times 20 + 2 \times 5 + 13)$$

$$A = \frac{110}{7} \times 63$$

$$A = 990 \text{ cm}^2$$

$$\begin{aligned}
 l^2 &= h^2 + r^2 \\
 13^2 &= h^2 + 5^2 \\
 h^2 &= 144 \\
 h &= 12
 \end{aligned}$$

Volume of the toy V = Volume of cylinder + Volume of hemisphere + Volume of cone

$$A = \pi r^2 h + \frac{22}{7} \pi r^3 + \frac{1}{3} \pi r^3 h$$

$$A = \pi r^2 \left(h + \frac{2}{3} r + \frac{1}{3} h \right)$$

$$A = \frac{22}{7} \times 5 \times 5 \left(20 + \frac{2}{3} \times 5 + \frac{1}{3} \times 12 \right)$$

$$A = \frac{15015}{7} \times 27.3$$

$$A = 2145 \text{ cm}^3$$

63. $d=4.2\text{cm}$ $r=2.1\text{cm}$

height of cylinder = height of cone = 2.8cm

slope of the cone $l^2 = h^2 + r^2$

$$l^2 = (2.8)^2 + (2.1)^2$$

$$l^2 = 12.25 \text{ cm}$$

$$l = (3.5)^2$$

$$l = 3.5 \text{ cm}$$

Surface area of the rest part of the Solid.

1. $A = \text{CSA of cylinder} + \text{CSA of cone} + \text{Area of circle}$

$$A = 2\pi rh + \pi rl + \pi r^2$$

$$A = 2 \times \frac{22}{7} \times 2.1 \times 2.8 + \frac{22}{7} \times 2.1 \times 3.5 + \frac{22}{7} \times 2.1 \times 2.1$$

$$A = 36.96 + 23.1 + 13.86$$

$$A = 73.92 \text{ cm}^2$$

64. height of cylinder = 27cm

$r=6\text{cm}$

height of cone = 8cm

slope of cone $l^2 = h^2 + r^2$

$$l^2 = 8^2 + 6^2$$

$$l^2 = 10^2$$

$$l = 10 \text{ cm}$$

Surface area of Solid = CSA of the cylinder + CSA of hemisphere + CSA of cone

$$A = 2\pi rh + 2\pi r^2 + \pi rl$$

$$A = \pi r[2h + 2r + l]$$

$$A = \pi \times 6[2 \times 27 + 2 \times 6 + 10]$$

$$A = 6\pi[54 + 12 + 10]$$

$$A = 456\pi \text{ cm}^2$$

$$A = 456 \times \frac{22}{7}$$

$$A = 1433.142 \text{ cm}^2$$

V = Volume of the cylinder – volume of hemisphere – volume of cone

$$V = \pi r^2 h - \frac{2}{3} \pi r^3 - \frac{1}{3} \pi r^2 h$$

$$V = \pi \left(6 \times 6 \times 27 - \frac{2}{3} 6 \times 6 \times 6 - \frac{1}{3} 6 \times 6 \times 8 \right)$$

$$V = \pi(972 - 144 - 96)$$

$$V = 732\pi \text{ cm}^3$$

$$V = 732 \times \frac{22}{7}$$

$$V = 2300.57 \text{ cm}^3$$

65. Height of the cone $h^2 = l^2 - r^2$
 $h^2 = 25^2 - 7^2$
 $h^2 = 625 - 49$
 $h^2 = 576$
 $h = 24 \text{ cm}$

Volume of cone = $\frac{1}{3} \pi r^2 h$
 $= \frac{1}{3} \times \frac{22}{7} \times 7 \times 7 \times 24$
 $= 1232 \text{ cc}$

Volume of cylinder = 5 x volume of cone
 $= 5 \times 1232$
 $= 6160 \text{ cc}$

Radius of cylinder = 14 cm

Volume of cylinder = $\pi r^2 h$
 $= \frac{22}{7} \times 14 \times 14 \times h$
 $h = \frac{6160}{616} = 10 \text{ cm}$

Curved surface area of a cone = $2\pi rh$
 $= 2 \times \frac{22}{7} \times 14 \times 10$
 $= 880 \text{ cm}^2$

Unit : 13 STATISTICS

I. Multiple Choice Questions

1. B) Mode
2. C) $\frac{\text{upper limit} + \text{lower Limit}}{2}$
3. C) 30
4. A) 35
5. B) Median
6. A) $3 \text{ Median} = 2 \text{ Mean} + \text{Mode}$
7. C) size of the class Interval
8. C) 7
9. B) The height of 50% girls is more than 149.03 cm and height of n50% of the girls is less than 149.03 cm
10. A) $x = a + \frac{\sum f_i u_i}{\sum f_i} \times h$

II. One Mark Questions :

11. 17
12. 20-30
13. 3-5
14. $\bar{X} = \frac{\sum f_i x_i}{\sum f_i}$
15. 40
16. Median = Mean + 3
Mode = 3 Median – 2 Mean
= 3 (Mean + 3) – 2 Mean
Mode = Mean + 9
∴ Mode is 9 more than the mean
17. Median = $L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h$
18. Mode = $L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$
19. $3 \text{ Median} = \text{Mode} + 2 \text{ Mean}$
= 12.4 + 2 x 10.5
= 33.4
20. $3 \text{ Median} = \text{Mode} + 2 \text{ Mean}$
3(33) = Mode + 2 (27)
Mode = 99 – 54 = 45

$$\begin{aligned}
21. \quad 3 \text{ Median} &= \text{Mode} + 2 \text{ Mean} \\
&= 7 + 2 \times 8 \\
&= 7 + 16 \\
\text{Median} &= 23/3 \\
&= 7.66
\end{aligned}$$

III. Two Mark questions

$$\begin{aligned}
22. \quad 3 \text{ Median} &= \text{Mode} + 2 \text{ Mean} \\
3 \times 45.5 &= 50.5 + 2 \text{ Mean} \\
2 \text{ Mean} &= 136.5 - 50.5.
\end{aligned}$$

$$\begin{aligned}
\text{Mean} &= \frac{86}{2} \\
\text{Mean} &= 43
\end{aligned}$$

23.

C - I	f	x	$f_i x_i$
1-5	2	3	6
6-10	3	8	24
11-15	4	13	52
16-20	2	18	36
	$\Sigma f_i = 10$		$\Sigma f_i x_i = 118$

$$\begin{aligned}
\bar{X} &= \frac{\Sigma f_i x_i}{\Sigma f_i} \\
&= \frac{118}{10} \\
&= 11.8
\end{aligned}$$

24.

C - I	f	x	d_i
10-25	2	17.5	-45
25-40	3	32.5	-30
40-55	7	47.5	-15
55-70	6	62.5	0
70-85	6	77.5	15
85 -100	6	92.5	30

IV. THREE MARKS QUESTIONS :

25.

C - I	f	x_i	$f_i x_i$
45 - 55	3	50	150
55 - 65	10	60	600
65 - 75	11	70	770
75 - 85	8	80	640
85 - 95	3	90	270
	$\Sigma, f . = 35$		$\Sigma f_i x_i = 2430$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{2400}{35} = 69.42$$

26.

C - I	f	x_i	$f_i x_i$
1 - 3	2	2	4
3 - 5	5	4	20
5 - 7	8	6	48
7 - 9	3	8	24
9 - 11	2	10	20
	$\Sigma, f . i . = 20$		$\Sigma f_i x_i = 116$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{116}{20} = 5.8$$

27.

C - I	f	x_i	$f_i x_i$
10-14	2	12	24
15-19	3	17	51
20-24	5	22	110
25-29	3	27	81
30-34	2	32	64
	$\Sigma, f_i . = 15$		$\Sigma f_i x_i = 330$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{330}{15} = 22$$

28.

C - I	f	x_i	$f_i x_i$
0 - 10	4	5	20
10 - 20	9	15	135
20 - 30	15	25	375
30 - 40	14	35	490
40 - 50	8	45	360
	$\Sigma f_i = 50$		$\Sigma f_i x_i = 1380$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{1380}{50} = 27.6$$

29.

C - I	f	x_i	$f_i x_i$
11 - 13	7	12	84
13 - 15	6	14	84
15 - 17	9	16	144
17 - 19	13	18	234
19 - 21	x	20	20x
21 - 23	5	22	110
23 - 25	4	24	96
	$\Sigma f_i = 44+x$		$\Sigma f_i x_i = 752+20x$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i}$$

$$18 = \frac{752+20x}{44+x}$$

$$792 + 18x = 752 + 20x$$

$$40 = 2x$$

$$x = \frac{40}{2} = 20$$

30.

C - I	f	x_i	$f_i x_i$
15-25	8	20	160
25-35	12	30	360
35-45	15	40	600
45-55	9	50	450
55-65	6	60	360
	$\Sigma f_i = 50$		$\Sigma f_i x_i = 1930$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{1930}{50} = 38.6$$

31.

C - I	f	x_i	$f_i x_i$
0-10	7	5	35
10-20	8	15	120
20-30	12	25	300
30-40	13	35	455
40-50	10	45	450
	$\Sigma f_i = 50$		$\Sigma f_i x_i = 1360$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{1360}{50} = 27.2$$

32.

C - I	f	x_i	$f_i x_i$
20-40	7	30	210
40-60	15	50	750
60-80	20	70	1400
80-100	8	90	720
100-120	5	110	550
	$\Sigma f_i = 55$		$\Sigma f_i x_i = 3630$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{3630}{55} = 66$$

33.

C - I	f	x_i	$f_i x_i$
10-20	2	15	30
20-30	3	25	75
30-40	5	35	175
40-50	7	45	315
50-60	3	55	165
	$\Sigma f_i = 20$		$\Sigma f_i x_i = 760$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{760}{20} = 38$$

34.

C - I	f	x_i	$f_i x_i$
10-20	2	15	30
20-30	3	25	75
30-40	6	35	210
40-50	5	45	225
50-60	4	55	220
	$\Sigma f_i = 20$		$\Sigma f_i x_i = 760$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{760}{20} = 38$$

35.

C - I	f	x_i	$f_i x_i$
10-20	2	15	30
20-30	5	25	125
30-40	6	35	210
40-50	5	45	225
50-60	2	55	110
	$\Sigma f_i = 20$		$\Sigma f_i x_i = 700$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{700}{20} = 35$$

36.

C - I	f	x_i	$f_i x_i$
10-20	4	15	60
20-30	6	25	150
30-40	5	35	175
40-50	4	45	180
50-60	1	55	55
	$\Sigma f_i = 20$		$\Sigma f_i x_i = 620$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{620}{20} = 31$$

37.

C - I	f	x_i	$f_i x_i$
5-15	1	10	10
15-25	3	20	60
25-35	5	30	150
35-45	4	40	160
45-55	2	50	100
	$\Sigma f_i = 15$		$\Sigma f_i x_i = 480$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{480}{15} = 32$$

38.

C - I	f	x_i	$f_i x_i$
5 - 15	4	10	40
15 - 25	6	20	120
25 - 35	5	30	150
35 - 45	6	40	240
45 - 55	4	50	200
	$\Sigma f_i = 25$		$\Sigma f_i x_i = 750$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{750}{25} = 30$$

39.

C - I	f	x_i	$f_i x_i$
2 - 6	4	4	16
6 - 10	8	8	64
10 - 14	2	12	24
14 - 18	1	16	16
18 - 22	5	20	100
	$\Sigma f_i = 20$		$\Sigma f_i x_i = 220$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{220}{20} = 11$$

40.

C - I	f	Cf_i
0-10	5	5
10-20	8	13
20-30	20	33
30-40	15	48
40-50	7	55
	N=55	

$$L=20$$

$$Cf_i = 13$$

$$h = 10$$

$$f=20$$

$$\frac{N}{2} = \frac{55}{2} = 27.5$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 20 + \left(\frac{27.5 - 13}{20} \right) \times 10$$

$$= 20 + \left(\frac{14.5}{20} \right)$$

$$= 20 + 7.25$$

$$= 27.25$$

41.

C . I	f	x_i	$f_i x_i$
1 - 5	4	3	12
6 - 10	3	8	24
11 - 15	2	13	26
16 - 20	1	18	18
20 - 25	5	23	115
	$\Sigma f_i = 15$		$\Sigma f_i x_i = 195$

$$\bar{X} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{195}{15} = 13$$

42.

C . I	f	Cf_i
100-150	6	6
150-200	3	9
200-250	5	14
250-300	20	34
300-350	10	44
	N=44	

$$L=250$$

$$Cf_i = 14$$

$$h = 50$$

$$f=20$$

$$\frac{N}{2} = \frac{44}{2} = 22$$

$$\begin{aligned} \text{Median} &= L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h \\ &= 250 + \left(\frac{22 - 14}{20} \right) \times 50 \\ &= 250 + \left(\frac{400}{20} \right) \\ &= 250 + 20 \\ &= 270 \end{aligned}$$

43.

C.I	f	Cf_i
50-60	6	6
60-70	9	15
70-80	20	35
80-90	10	45
90-100	5	50
	N=50	

$$L=70$$

$$Cf_i = 15$$

$$h = 10$$

$$f=20$$

$$\frac{N}{2} = \frac{50}{2} = 25$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h$$

$$\begin{aligned} &= 70 + \left(\frac{25 - 15}{20} \right) \times 10 \\ &= 70 + \left(\frac{100}{20} \right) \\ &= 70 + 5 = 75 \end{aligned}$$

44.

C.I	f	Cf_i
50-60	5	5
60-70	8	13
70-80	10	23
80-90	4	27
90-100	3	30
	N=30	

$$L=70$$

$$Cf_i = 13$$

$$h = 10$$

$$f=10$$

$$\frac{N}{2} = \frac{30}{2} = 15$$

$$Median = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 70 + \left(\frac{15 - 13}{10} \right) \times 10 = 70 + \left(\frac{20}{20} \right) = 70 + 1 = 71$$

45.

C.I	f	Cf_i
1-10	5	5
11-20	8	13
21-30	20	33
31-40	15	48
41-50	7	55
	N=55	

$$L=21$$

$$Cf_i = 13$$

$$h = 10$$

$$f=20$$

$$\frac{N}{2} = \frac{55}{2} = 27.5$$

$$Median = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 21 + \left(\frac{27.5 - 13}{20} \right) \times 10 = 21 + \left(\frac{145}{20} \right) = 21 + 7.25 = 28.25$$

46.

C.I	f_i	Cf_i
0-20	6	6
20-40	5	11
40-60	9	20
60-80	4	24
80-100	2	26
	N=26	

$$L=40$$

$$Cf_i = 11$$

$$h = 20$$

$$f=9$$

$$\frac{N}{2} = \frac{26}{2} = 13$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 40 + \left(\frac{13 - 11}{9} \right) \times 20 = 40 + \left(\frac{40}{9} \right) = 40 + 4.4 = 44.44$$

47.

C.I	f_i	Cf_i
20-40	7	7
40-60	15	22
60-80	20	42
80-100	2	44
100-120	4	48
	N=48	

$$L=60$$

$$Cf_i = 22$$

$$h = 20$$

$$f=20$$

$$\frac{N}{2} = \frac{48}{2} = 24$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h$$

$$= 60 + \left(\frac{24 - 22}{20} \right) \times 20$$

$$= 60 + \left(\frac{40}{20} \right) = 60 + 2 = 62$$

48.

C.I	f_i	Cf_i
20 - 40	7	7
40 - 60	15	22
60 - 80	20	42
80 - 100	8	50
	N=50	

$$L=60$$

$$Cf_i = 22$$

$$h = 20$$

$$f=20$$

$$\frac{N}{2} = \frac{50}{2} = 25$$

$$Median = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h$$

$$= 60 + \left(\frac{25 - 22}{20} \right) \times 20$$

$$= 60 + \left(\frac{3}{20} \right) 20$$

$$= 60 + 3$$

$$= 63$$

49.

C.I	f_i	Cf_i
0 - 20	6	6
20 - 40	9	15
40 - 60	10	25
60 - 80	8	33
80 - 100	7	40
	N=40	

$$L=40$$

$$Cf_i = 15$$

$$h = 20$$

$$f=10$$

$$\frac{N}{2} = \frac{40}{2} = 20$$

$$Median = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 40 + \left(\frac{20 - 15}{10} \right) \times 20 = 40 + \left(\frac{5}{10} \right) \times 20 = 40 + 10 = 50$$

50.

C.I	f	Cf_i
5-15	1	1
15-25	3	4
25-35	5	9
35-45	7	16
45-55	2	18
	N=18	

$$L=25$$

$$Cf_i = 4$$

$$h = 10$$

$$f=5$$

$$\frac{N}{2} = \frac{18}{2} = 9$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h$$

$$= 25 + \left(\frac{9 - 4}{5} \right) \times 10$$

$$= 25 + \left(\frac{50}{5} \right)$$

$$= 25 + 10$$

$$= 35$$

51.

C.I	f	Cf_i
5-15	3	3
15-25	4	7
25-35	8	15
35-45	7	22
45-55	3	25
	N=25	

$$L=25$$

$$Cf_i = 7$$

$$h = 10$$

$$f=8$$

$$\frac{N}{2} = \frac{25}{2} = 12.5$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 25 + \left(\frac{12.5 - 7}{8} \right) \times 10 = 25 + \left(\frac{55}{8} \right) = 25 + 6.87 = 31.87$$

52.

C.I	f	Cf_i
15-20	4	4
20-25	5	9
25-30	10	19
30-35	5	24
35-40	6	30
	N=30	

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h$$

$$= 25 + \left(\frac{15 - 7}{8} \right) \times 10$$

$$= 25 + \left(\frac{55}{8} \right) = 25 + 6.87 = 31.87$$

53.

C.I	f	Cf_i
50-52	15	15
53-55	110	125
56-58	135	260
59-61	115	375
62-64	25	400
	N=400	

$$L=55.5$$

$$Cf_i = 125$$

$$h = 2$$

$$f=135$$

$$\frac{N}{2} = \frac{400}{2} = 200$$

$$\text{Median} = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 55.5 + \left(\frac{200 - 125}{135} \right) \times 2 = 55.5 + \left(\frac{150}{135} \right) = 55.5 + 1.11 = 56.61$$

54.

C.I	f	Cf_i
1 - 4	6	6
4 - 7	30	36
7 - 10	40	76
10 - 13	16	92
13 - 16	4	96
16 - 19	4	100
	N=100	

$$L=7$$

$$Cf_i = 36$$

$$h = 3$$

$$f=40$$

$$\frac{N}{2} = \frac{100}{2} = 50$$

$$Median = L + \left(\frac{\frac{N}{2} - CF_i}{f} \right) \times h = 7 + \left(\frac{50 - 36}{40} \right) \times 3 = 7 + \left(\frac{14}{40} \right) \times 3 = 7 + 1.05 = 8.05$$

55.

C.I	f
10-20	6
20-30	4
30-40	12
40-50	3
50-60	5

Here class interval of the mode is 30 - 40

$$L = 30$$

$$f_0 = 4$$

$$f_1 = 12$$

$$f_2 = 3$$

$$h = 10$$

$$MODE = L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$$

$$= 30 + \left[\frac{12 - 4}{2(12) - 4 - 3} \right] \times 10$$

$$= 30 + \left[\frac{8}{17} \right] \times 10$$

$$= 30 + 4.7$$

$$= 34.7$$

56.

C.I	f
5-10	3
10-15	5
15-20	8
20-25	4
25-30	5

Here class interval of the mode is 15 - 20

$$L = 15$$

$$f_0 = 5$$

$$f_1 = 8$$

$$f_2 = 4$$

$$h = 5$$

$$\begin{aligned} \text{Mode} &= L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h \\ &= 15 + \left[\frac{8 - 5}{2(8) - 5 - 4} \right] \times 5 = 15 + \left[\frac{3}{7} \right] \times 5 = 15 + 4.28 = 19.28 \end{aligned}$$

57.

C.I	f
1-3	7
3-5	8
5-7	2
7-9	2
9-11	1

Here class interval of the mode is 3 - 5

$$L = 3$$

$$f_0 = 7$$

$$f_1 = 8$$

$$f_2 = 2$$

$$h = 2$$

$$\begin{aligned} \text{Mode} &= L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h \\ &= 3 + \left[\frac{8 - 7}{2(8) - 7 - 2} \right] \times 2 \\ &= 3 + \left[\frac{1}{7} \right] \times 2 = 3 + 1.42 = 4.42 \end{aligned}$$

58.

C.I	f
0-20	10
20-40	35
40-60	52
60-80	61
80-100	38

Here class interval of the mode is 60 – 80

$$L = 60$$

$$f_0 = 52$$

$$f_1 = 61$$

$$f_2 = 38$$

$$h = 20$$

$$\begin{aligned} \text{Mode} &= L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h \\ &= 60 + \left[\frac{61 - 52}{2(61) - 52 - 38} \right] \times 20 \\ &= 60 + \left[\frac{9}{32} \right] \times 20 \\ &= 60 + 5.625 \\ &= 65.625 \end{aligned}$$

59.

C.I	f
0-10	6
10-20	9
20-30	15
30-40	9
40-50	1

Here class interval of the mode is 20 -30

$$L = 20$$

$$f_0 = 9$$

$$f_1 = 15$$

$$f_2 = 9$$

$$h = 10$$

$$\begin{aligned} \text{Mode} &= L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h \\ &= 20 + \left[\frac{15 - 9}{2(15) - 9 - 9} \right] \times 10 = 20 + \left[\frac{6}{12} \right] \times 10 = 20 + 5 = 25 \end{aligned}$$

60.

C.I	f
0-10	7
10-20	9
20-30	15
30-40	11
40-50	8

Here class interval of the mode is 20 - 30

$$L = 20$$

$$f_0 = 9$$

$$f_1 = 15$$

$$f_2 = 11$$

$$h = 10$$

$$\text{Mode} = L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h = 20 + \left[\frac{15 - 9}{2(15) - 9 - 11} \right] \times 10 = 20 + \left[\frac{6}{10} \right] \times 10 = 20 + 6 = 26$$

61.

C.I	f
0-10	7
10-20	8
20-30	2
30-40	2
40-50	1

Here class interval of the mode is 10 - 20

$$L = 10$$

$$f_0 = 7$$

$$f_1 = 8$$

$$f_2 = 2$$

$$h = 10$$

$$\begin{aligned} \text{Mode} &= L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h \\ &= 10 + \left[\frac{8 - 7}{2(8) - 7 - 2} \right] \times 10 = 10 + \left[\frac{1}{7} \right] \times 10 = 10 + 1.42 = 11.42 \end{aligned}$$

62.

C.I	f
1-3	7
4-6	8
7-9	2
10-12	2
13-15	1

Here class interval of the mode is 4 - 6

$$L = 3.5$$

$$f_0 = 7$$

$$f_1 = 8$$

$$f_2 = 2$$

$$h = 2$$

$$\text{Mode} = L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h = 3.5 + \left[\frac{8 - 7}{2(8) - 7 - 2} \right] \times 2 = 3.5 + \left[\frac{1}{7} \right] \times 2 = 3.5 + 0.28 = 3.78$$

63.

C.I	f
5-15	3
15-25	4
25-35	8
35-45	7
45-55	3

Here class interval of the mode is 25 - 35

$$L = 25$$

$$f_0 = 4$$

$$f_1 = 8$$

$$f_2 = 7$$

$$h = 10$$

$$\text{Mode} = L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$$

$$= 25 + \left[\frac{8 - 4}{2(8) - 4 - 7} \right] \times 10$$

$$= 25 + \left[\frac{4}{5} \right] \times 10$$

$$= 25 + 8$$

$$= 33$$

64.

C.I	f
10-20	3
20-30	9
30-40	6
40-50	7
50-60	5

Here class interval of the mode is 20 - 30

$$L = 20$$

$$f_0 = 3$$

$$f_1 = 9$$

$$f_2 = 6$$

$$h = 10$$

$$\text{Mode} = L + \left[\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$$

$$= 20 + \left[\frac{9 - 3}{2(9) - 3 - 6} \right] \times 10$$

$$= 20 + \left[\frac{6}{9} \right] \times 10$$

$$= 20 + 6.66$$

= 26.66

Unit – 14 Probability

I. Multiple choice questions :

- 1) A) 1
- 2) B) 0
- 3) B) 2
- 4) C) 4
- 5) D) 6
- 6) B) -1.5
- 7) A) $\frac{1}{5}$
- 8) A) $\frac{3}{6}$
- 9) B) 0.95
- 10) B) $\frac{5}{26}$
- 11) B) 0.25
- 12) C) 36
- 13) C) $\frac{1}{4}$
- 14) A) $\frac{2}{6}$
- 15) B) $\frac{21}{28}$
- 16) C) $\frac{4}{12}$
- 17) B) $\frac{1}{365}$
- 18) B) $0 \leq P(E) \leq 1$
- 19) D) 0
- 20) C) 0.5
- 21) A) $\frac{1}{2}$

22) C) 0.7

23) C) 1

24) A) $\frac{1}{5}$

25) B) $\frac{2}{3}$

26) C) $\frac{3}{7}$

II. One Marks Questions :

27) $S = \{T, R, I, A, N, G, L, E\}$ $n(S) = 8$
 $A = \{A, I, E\}$ $n(A) = 3$ $\therefore P(A) = \frac{n(A)}{n(S)} = \frac{3}{8}$

28) $P(A) + P(\underline{A}) = 1$

29) $P(E) + P(\underline{E}) = 1$, $P(\underline{E}) = 1 - 0.05 = 0.95$

30) $P(E) + P(\underline{E}) = 1$, Probability of not raining $= P(\underline{E}) = 1 - 0.75 = 0.25$

31) $P(A) + P(\underline{A}) = 1$, $P(\underline{A}) = 1 - \frac{2}{3} = \frac{1}{3}$

32) $P(B) + P(\underline{B}) = 1$, $P(\underline{B}) = 1 - 0.65 = 0.35$

33) $S = \{1, 2, 3, 4, 5, 6\}$, $n(S) = 6$
 $A = \{6\}$ $n(A) = 1$
 \therefore Probability of getting number 6 $= P(A) = \frac{n(A)}{n(S)} = \frac{1}{6}$

34) $S = \{H, T\}$ $n(S) = 2$
 $A = \{H\}$ $n(A) = 1$
 \therefore Probability of getting head $= P(A) = \frac{n(A)}{n(S)} = \frac{1}{2}$

35) $P(E) + P(\underline{E}) = 1$, Probability of losing the same game $= P(\underline{E}) = 1 - 0.8 = 0.2$

36) $P(\underline{A}) = 1 - P(A)$

$= 1 - 80\%$

$= 1 - 80/100$

$= 1 - 4/5$

$= 1/5$

37) All possible outcomes $= \{HH, HT, TH, TT\}$

$n(S) = 4$

III. Two marks questions :

38) $S = \{ HH, HT, TH, TT \}$ $n(S) = 4$

i) $A = \{ HT, TH \}$ $n(A) = 2$ $\therefore P(A) = \frac{n(A)}{n(S)} = \frac{2}{4} = \frac{1}{2}$

ii) $B = \{ HH, HT, TH \}$ $n(B) = 3$ $\therefore P(A) = \frac{n(B)}{n(S)} = \frac{3}{4}$

39) $S = \{ 1, 2, 3, 4, 5, 6 \}$ $n(S) = 6$

$A = \{ 3, 4, 5 \}$ $n(A) = 3$ $\therefore P(A) = \frac{n(A)}{n(S)} = \frac{3}{6} = \frac{1}{2}$

40) $S = \{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6)$

$(2,1), (2,2), (2,3), (2,4), (2,5), (2,6)$

$(3,1), (3,2), (3,3), (3,4), (3,5), (3,6)$

$(4,1), (4,2), (4,3), (4,4), (4,5), (4,6)$

$(5,1), (5,2), (5,3), (5,4), (5,5), (5,6)$

$(6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \}$ $n(S) = 36$

$A = \{ (3,2), (2,3), (4,1), (1,4) \}$ $n(A) = 4$

$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{4}{36} = \frac{1}{9}$

41) $S = \{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6)$

$(2,1), (2,2), (2,3), (2,4), (2,5), (2,6)$

$(3,1), (3,2), (3,3), (3,4), (3,5), (3,6)$

$(4,1), (4,2), (4,3), (4,4), (4,5), (4,6)$

$(5,1), (5,2), (5,3), (5,4), (5,5), (5,6)$

$(6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \}$

$n(S) = 36$

$A = \{ (4,6), (6,4), (5,5) \}$ $n(A) = 3$

$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{3}{36} = \frac{1}{12}$

42) $S = \{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6)$

$(2,1), (2,2), (2,3), (2,4), (2,5), (2,6)$

$(3,1), (3,2), (3,3), (3,4), (3,5), (3,6)$

$(4,1), (4,2), (4,3), (4,4), (4,5), (4,6)$

$(5,1), (5,2), (5,3), (5,4), (5,5), (5,6)$

$(6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \}$

$n(S) = 36$

$A = \{ (4,4), (4,5), (5,4), (5,5), (4,6), (6,4), (6,5), (5,6), (6,6) \}$

$n(A) = 9$

$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{9}{36} = \frac{1}{4}$

43)

$P(A) + P(\underline{A}) = 1$ $\frac{1}{2}P(\underline{A}) + P(\underline{A}) = 1$ $\Rightarrow P(\underline{A}) = \frac{2}{3}$	$\frac{P(A)}{P(\underline{A})} = \frac{1}{2}$ $P(\underline{A}) = 2P(A)$ $\Rightarrow P(A) = \frac{1}{2}P(\underline{A})$
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44) $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$ $n(S) = 8$

$$A = \{2, 4, 6, 8\} \quad n(A) = 4 \quad \therefore P(A) = \frac{n(A)}{n(S)} = \frac{4}{8} = \frac{1}{2}$$

45) $S = \{2, 3, 4, 5, 6, \dots, 25\}$ $n(S) = 24$

i) $n(A) = \{2, 4, 6, 8, \dots, 24\}$ $n(A) = 9$

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{9}{24}$$

ii) $n(B) = \{4, 9, 16, 25\}$ $n(B) = 4$

$$\therefore P(B) = \frac{n(B)}{n(S)} = \frac{4}{24}$$

46) $n(S) = 6 + 5 + 4 = 15$

i) $n(A) = 6 + 5 = 11$

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{11}{15}$$

ii) $n(B) = 6$

$$\therefore P(B) = \frac{n(B)}{n(S)} = \frac{6}{15} = \frac{2}{5}$$

47) $n(S) = 36$ Number of defective mangoes = $36 \times \frac{1}{4} = 9$

$$\Rightarrow \text{Number of good mangoes} = 36 - 9 = 27$$

$$n(A) = 27$$

$$\therefore \text{Probability of drawing a good mango} = P(A) = \frac{n(A)}{n(S)} = \frac{27}{36}$$

$$48) P(A) + P(\bar{A}) = 1$$

$$P(A) : P(\bar{A}) = 5 : 11$$

$P(A) + P(\bar{A}) = 1$ $\frac{5}{11}P(\bar{A}) + P(\bar{A}) = 1$ $\Rightarrow P(\bar{A}) \frac{60}{11} = 1$ $\Rightarrow P(\bar{A}) = \frac{11}{60}$ $\therefore P(A) = \frac{5}{60}$	$\frac{P(A)}{P(\bar{A})} = \frac{5}{11}$ $\Rightarrow P(A) = P(\bar{A}) \frac{5}{11}$
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$$49) \text{ Probability of drawing a defective watch} = P(A) = \frac{50}{500} = \frac{1}{10}$$

$$50) S = \{1, 2, 3, 4, 5, 6\} \quad n(S) = 6$$

$$A = \{2, 4, 5, 6\} \quad n(A) = 4 \quad P(A) = \frac{n(A)}{n(S)} = \frac{4}{6} = \frac{2}{3}$$

$$51) S = \{(1,1), (1,2), (1,3), (1,4), (1,5), (1,6) \\ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6) \\ (3,1), (3,2), (3,3), (3,4), (3,5), (3,6) \\ (4,1), (4,2), (4,3), (4,4), (4,5), (4,6) \\ (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \\ (6,1), (6,2), (6,3), (6,4), (6,5), (6,6)\} \quad n(S) = 36$$

$$A = \{(1,5), (5,1), (2,4), (4,2), (3,3)\} \quad n(A) = 5$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{5}{36}$$

$$52) S = \{HH, HT, TH, TT\} \quad n(S) = 4$$

$$i) A = \{HH\} \quad n(A) = 1 \quad \therefore P(A) = \frac{n(A)}{n(S)} = \frac{1}{4}$$

$$ii) B = \{HT, TH\} \quad n(B) = 2 \quad \therefore P(B) = \frac{n(B)}{n(S)} = \frac{2}{4} = \frac{1}{2}$$

$$53) S = \{1, 2, 3, 4, 5, 6\} \quad n(S) = 6$$

$$a) A = \{2, 4, 6\} \quad n(A) = 3 \quad P(A) = \frac{n(A)}{n(S)} = \frac{3}{6} = \frac{1}{2}$$

$$b) B = \{1, 4\} \quad n(B) = 2 \quad P(B) = \frac{n(B)}{n(S)} = \frac{2}{6} = \frac{1}{3}$$

$$54) S = \{A, B, C, D, E, I\} \quad n(S) = 6$$

$$A = \{A, E, I\} \quad n(A) = 3,$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{3}{6} = \frac{1}{2}$$

$$55) \quad n(B) = 6 \quad n(R) = ? \quad n(S) = ?$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{3}{8} = \frac{6}{n(S)} \Rightarrow n(S) = 16 \quad \therefore n(R) = 16 - 6 = 10$$

$$P(R) = \frac{n(R)}{n(S)}$$

$$P(R) = \frac{5}{8}$$

$$56) \quad S = \{1, 2, 3, 4, 1, 5\} \quad n(S) = 6$$

$$A = \{1, 1, 4\} \quad n(A) = 3 \quad P(A) = \frac{n(A)}{n(S)} = \frac{3}{6} = \frac{1}{2}$$

$$57) \quad n(S) = 20 \quad A = \{1, 8\} \quad n(A) = 2$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{2}{20} = \frac{1}{10}$$

IV. Three marks questions

$$58) \quad S = \{1, 2, 3, 4, 5, 6\} \quad n(S) = 6$$

$$i) \quad A = \text{Greater than } 2 = \{3, 4, 5, 6\} \quad n(A) = 4 \therefore P(A) = \frac{n(A)}{n(S)} = \frac{4}{6} = \frac{2}{3}$$

$$ii) \quad B = \text{Less than or equal to } 2 = \{1, 2\} \quad n(B) = 2 \therefore P(B) = \frac{n(B)}{n(S)} = \frac{2}{6} = \frac{1}{3}$$

$$iii) \quad C = \text{Not more than } 2 \text{ is same as 'less than or equal to } 2 = \{1, 2\} \quad n(C) = 2 \therefore$$

$$P(C) = \frac{n(C)}{n(S)} = \frac{2}{6} = \frac{1}{3}$$

$$59) \quad S = \{HH, HT, TH, TT\} \quad n(S) = 4$$

$$i) \quad A = \{HH, HT, TH\} \quad n(A) = 3 \quad \therefore P(A) = \frac{n(A)}{n(S)} = \frac{3}{4}$$

$$ii) \quad B = \{HH\} \quad n(B) = 1 \quad P(B) = \frac{n(B)}{n(S)} = \frac{1}{4}$$

$$iii) \quad C = \{TT\} \quad n(C) = 1 \quad P(C) = \frac{n(C)}{n(S)} = \frac{1}{4}$$

$$60) \quad S = \{5, 6, 7, 8, \dots, 30\} \quad n(S) = 26$$

$$i) \quad A = \{6, 12, 18, 24, 30\} \quad n(A) = 5 \quad P(A) = \frac{n(A)}{n(S)} = \frac{5}{26}$$

$$ii) \quad B = \{9, 16, 25\} \quad n(B) = 3 \quad \therefore P(B) = \frac{n(B)}{n(S)} = \frac{3}{26}$$

$$iii) \quad C = \{6, 9, 12, 15, 18, 21, 24, 27, 30\} \quad n(C) = 9 \therefore P(C) = \frac{n(C)}{n(S)} = \frac{9}{26}$$

$$61) \quad n(S) = 3 + 5 + 8 = 16$$

$$a) \quad A = \text{Getting a red ball} \quad n(A) = 3$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{3}{16}$$

b) B= Not getting a white ball $n(B)=11$,

$$\therefore P(B) = \frac{n(B)}{n(S)} = \frac{11}{16}$$

62) $S = \{1,2,3,4,\dots,20\}$ $n(S)=20$

i) $A = \{1,4,9,16\}$ $n(A) = 4$ $\therefore P(A) = \frac{n(A)}{n(S)} = \frac{4}{20}$

ii) $B = \{6,12,18\}$ $n(B)=3$ $\therefore P(B) = \frac{n(B)}{n(S)} = \frac{3}{20}$

63) $P(W)+P(B)+P(R) = 1$

$$\frac{3}{10} + \frac{2}{5} + P(R) = 1$$

$$P(R) = \frac{3}{10}$$

$$P(B) = \frac{2}{5} \because n(B)=20$$

$$\frac{n(B)}{n(S)} = \frac{2}{5} \Rightarrow \frac{20}{n(S)} = \frac{2}{5} \Rightarrow n(S)=50$$

64) $n(S) = 50$,

i) A= less than 34 $n(A)=8$ $\therefore P(A) = \frac{n(A)}{n(S)} = \frac{8}{50}$

ii) B= Between 71-90, $n(B)=11$ $\therefore P(B) = \frac{n(B)}{n(S)} = \frac{11}{50}$

iii) C= more than 90, $n(C)=8$ $\therefore P(C) = \frac{n(C)}{n(S)} = \frac{8}{50}$
